

PolinSAR Training Course 2023

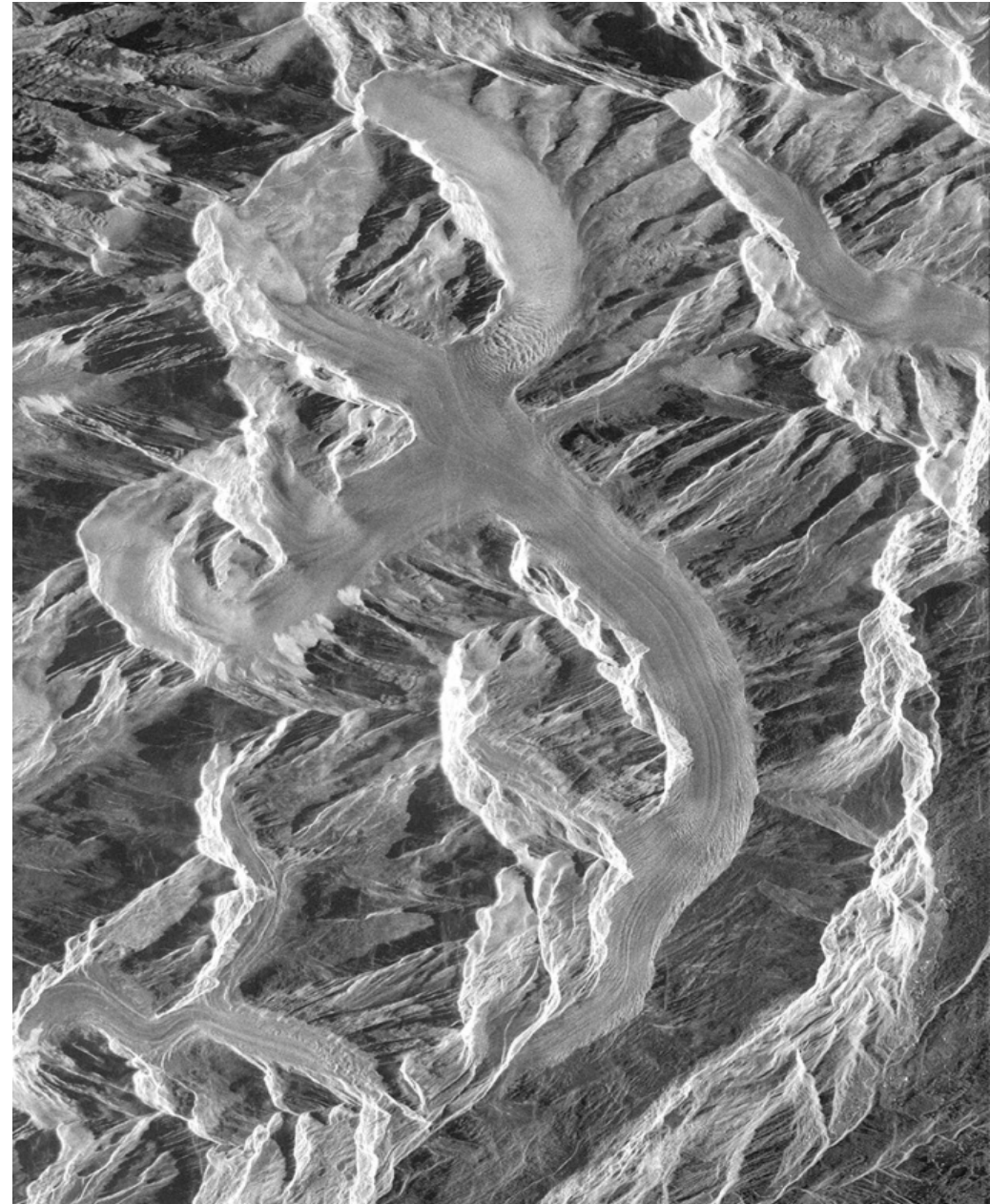
Application: Snow Height Estimation

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Environmental Engineering, ETH, Zurich**

Introduction

- Why is SAR good for snow parameter estimation?
- Introduction of the co-pol phase difference (CPD)
- TanDEM-X a co-pol system
- Testsite Great Aletschglacier
- Propagation model to estimate snow height



Why Radar Techniques for Snow?

- Optical methods sample only the snow surface
- Microwave penetrate into snow
- High frequency required to avoid total penetration: 5 - 50 GHz (note: stronger atmosphere influence)

Typical interactions of microwave and snow and ice:

- Total penetration ($T \ll 0^\circ\text{C}$, $n \ll 10$ GHz)
- Total reflection at the surface ($T \geq 0^\circ\text{C}$)
- Volume scattering ($T < 0^\circ\text{C}$, $n > 5$ GHz, depth > 2 m)

Interferometric applications for snow and ice:

- Multipass coherence decay: Snowfall / Melting
- Single pass: DEM-comparison based on surface reflection (deep firn, glacier mass balance)
- D-InSAR: freezing ground deformation, additional scatterers, complex path delays, atmosphere
- Polarimetric Phase differences (co-pol phase differences - CPD)



Liebe 1983,
IEEE Trans. Antennas Propag.

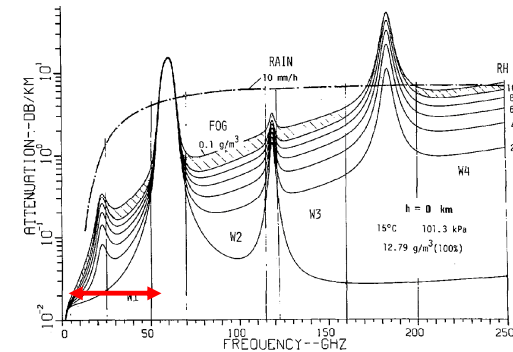
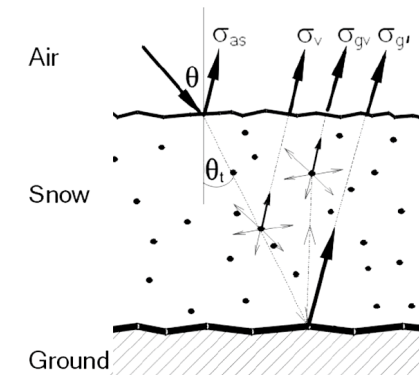
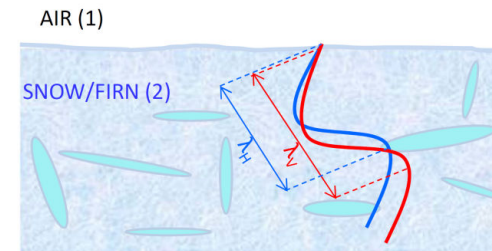


Fig. 1. Specific attenuation at sea level over the frequency range 1-250 GHz for various relative humidities (0 to 100 percent), including fog (0.1 g/m³) and rain ($R = 10$ mm/h).



Rott et al,
2010, *IEEE Proc.*



Parrella,
PolInSAR
2013
Leinss et al. 2016,
The Cryosphere

Co-Polarimetric Phase Differences

$$[S] = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \rightarrow \vec{k}_{3L} = \begin{bmatrix} S_{HH} \\ \sqrt{2} \cdot S_{XX} \\ S_{VV} \end{bmatrix}$$

Lexicographic Scattering Vector
 $S_{HV} = S_{VH} = S_{XX}$

Covariance Matrix: $[C_3] := \langle \vec{k}_{3L} \cdot \vec{k}_{3L}^* \rangle =$

$$\begin{bmatrix} \langle |S_{HH}|^2 \rangle & \sqrt{2} \langle S_{HH} S_{HV}^* \rangle & \langle S_{HH} S_{VV}^* \rangle \\ \sqrt{2} \langle S_{HV} S_{HH}^* \rangle & 2 \langle |S_{HV}|^2 \rangle & \sqrt{2} \langle S_{HV} S_{VV}^* \rangle \\ \langle S_{VV} S_{HH}^* \rangle & \sqrt{2} \langle S_{VV} S_{HV}^* \rangle & \langle |S_{VV}|^2 \rangle \end{bmatrix}$$

Co-Pol Phase Difference:

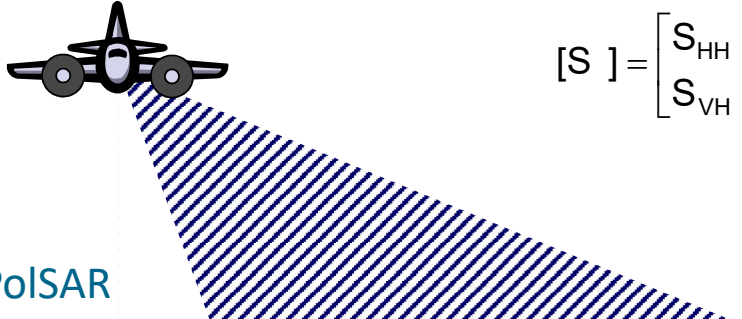
$$\varphi_{CPD} = \arctan \frac{\text{Im}\{\langle S_{VV} S_{HH}^* \rangle\}}{\text{Re}\{\langle S_{VV} S_{HH}^* \rangle\}}$$

[C] is by definition hermitian positive semi-definite matrices (i.e. have positive eigenvalues)

Types of Coherences



PolSAR



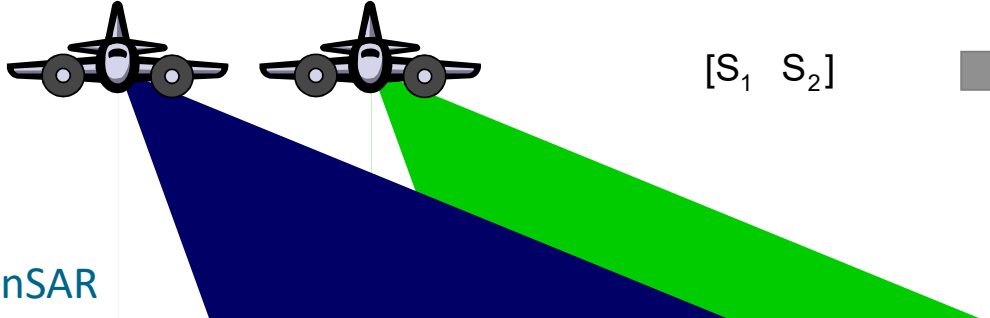
$$[S] = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix}$$

➔

Polarimetric Coherences

$$\tilde{\gamma}(S_{ij} S_{mn}) = \frac{\langle S_{ij} S_{mn}^* \rangle}{\sqrt{\langle S_{ij} S_{ij}^* \rangle \langle S_{mn} S_{mn}^* \rangle}}$$

InSAR



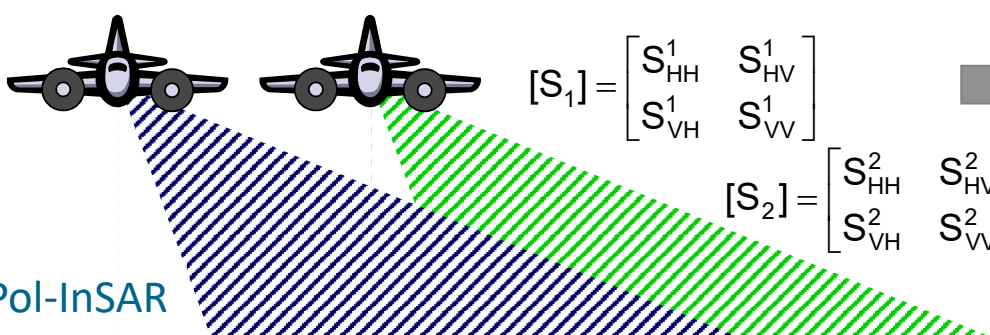
$$[S_1 \ S_2]$$

➔

Interferometric Coherences

$$\tilde{\gamma}(S_1 \ S_2) = \frac{\langle S_1 \ S_2^* \rangle}{\sqrt{\langle S_1 \ S_1^* \rangle \langle S_2 \ S_2^* \rangle}}$$

Pol-InSAR



$$[S_1] = \begin{bmatrix} S_{HH}^1 & S_{HV}^1 \\ S_{VH}^1 & S_{VV}^1 \end{bmatrix}$$

$$[S_2] = \begin{bmatrix} S_{HH}^2 & S_{HV}^2 \\ S_{VH}^2 & S_{VV}^2 \end{bmatrix}$$

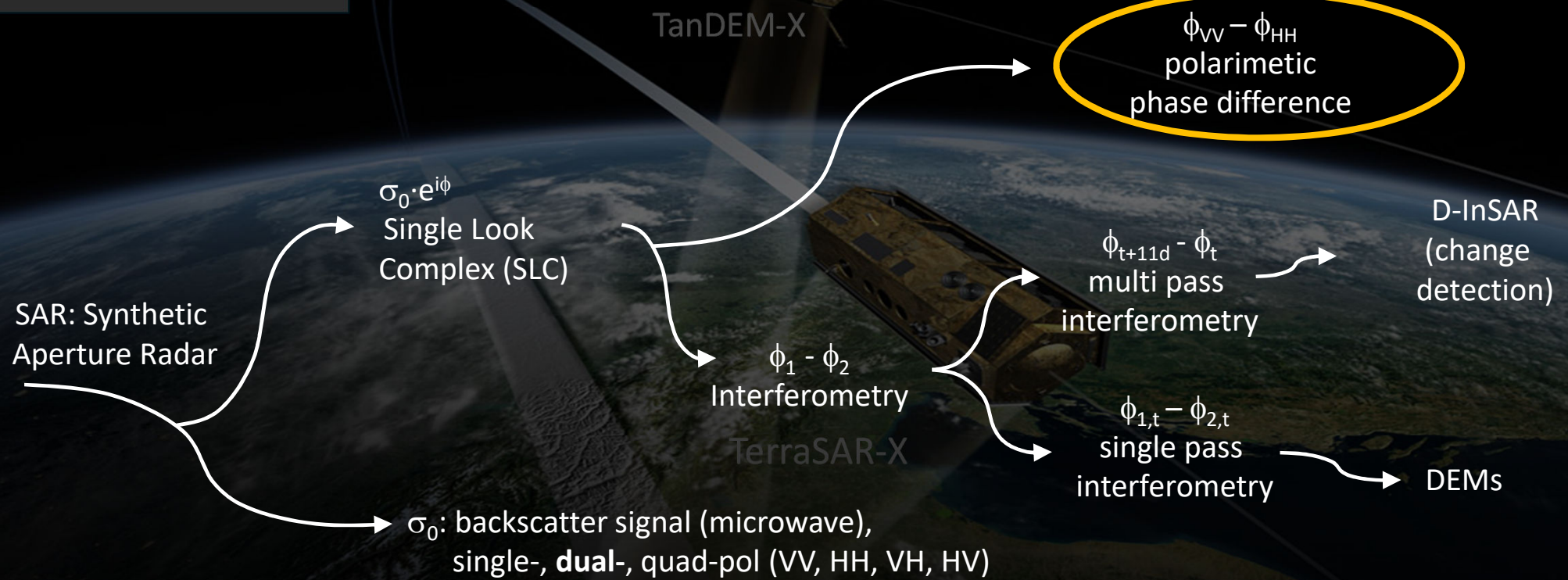
➔

Polarimetric / Interferometric Coherences

$$\tilde{\gamma}(S_{ij}^1 \ S_{mn}^2) = \frac{\langle S_{ij}^1 \ S_{mn}^{2*} \rangle}{\sqrt{\langle S_{ij}^1 \ S_{ij}^{1*} \rangle \langle S_{mn}^2 \ S_{mn}^{2*} \rangle}}$$

TerraSAR-X and TanDEM-X

A fantastic playground with many options

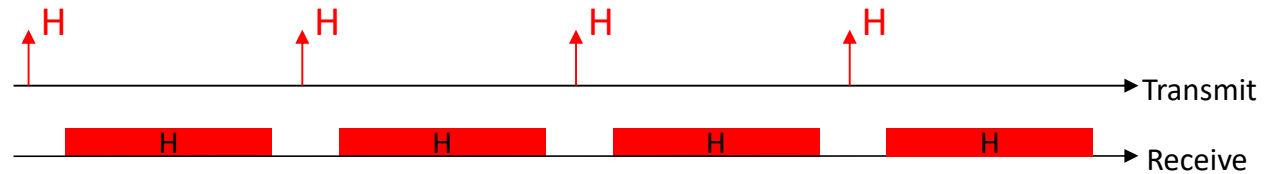


- X-Band: $f = 9.65$ GHz, $\lambda = 3$ cm, Resolution: 3 m, Repeat cycle: 11 days
- Monostatic **multi-pass** Interferometry: $\Delta t = 11$ days
- Bistatic **single-pass** Interferometry: $\Delta t = 0$

Polarization Modes @ TerraSAR-X/TanDEM-X

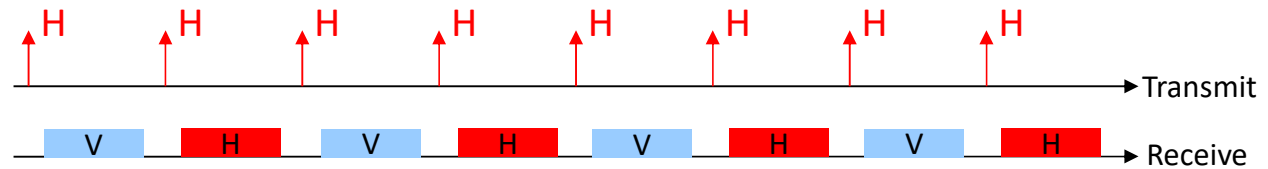
Single Polarization

- 1 polarization channel, {HH, VV}
- stripmap, spotlight, ScanSAR



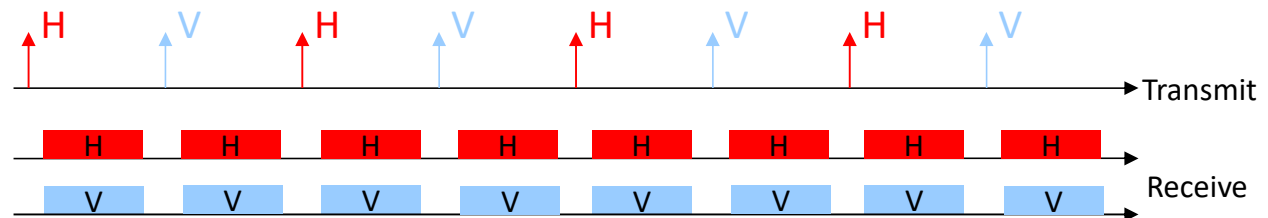
Dual Polarization

- 2 polarization channels, {HH/VV, HH/HV, VV/HV}
- stripmap, spotlight
- coherent pol. phase
- smaller elevation beam

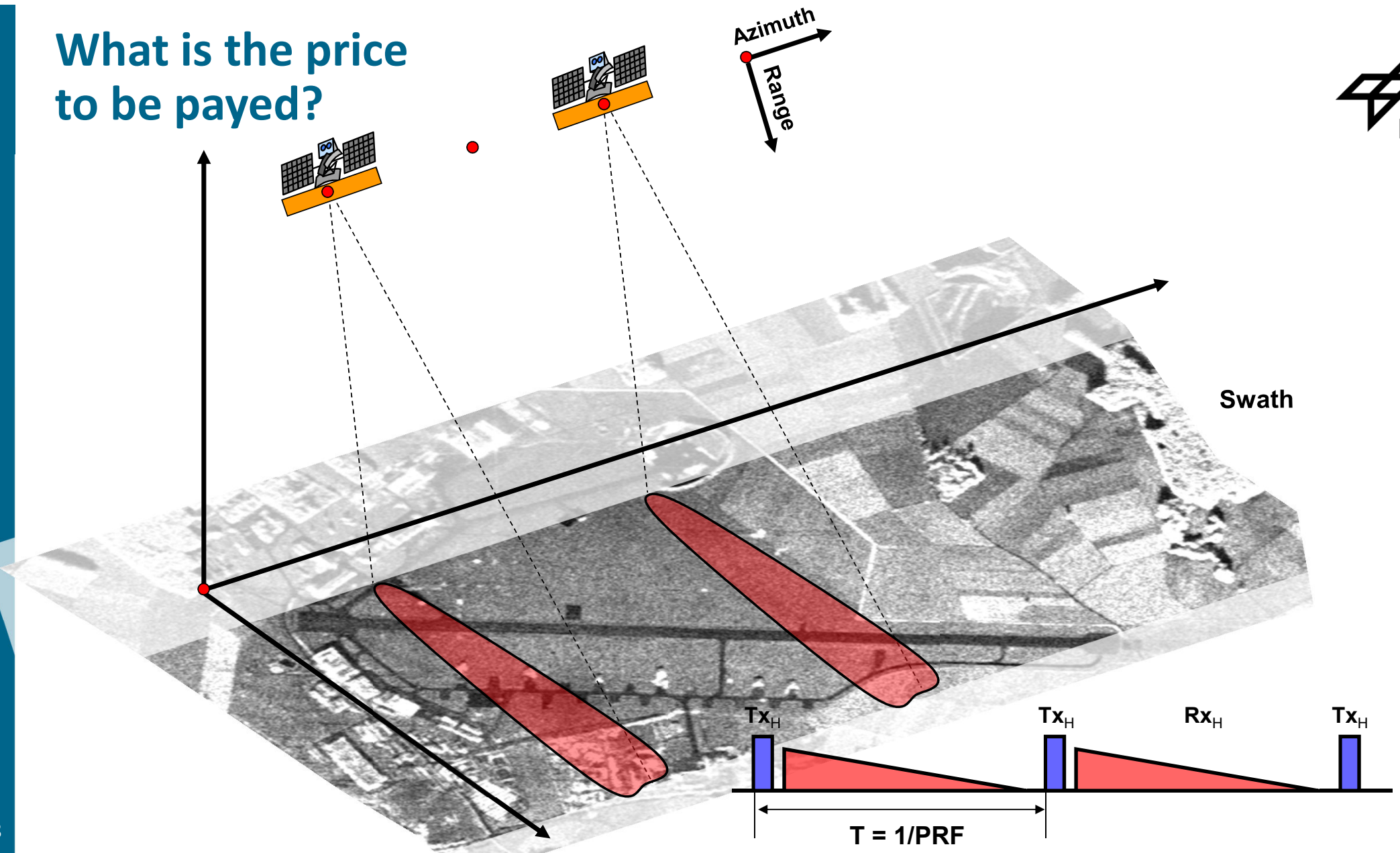


Quad Polarization

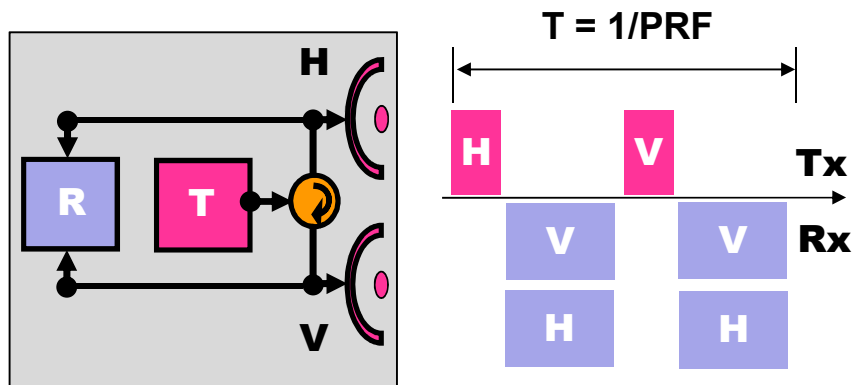
- All 4 pol. channels
- Stripmap
- coherent pol. Phase
- smaller elevation beam
- Experimental product



What is the price to be payed?



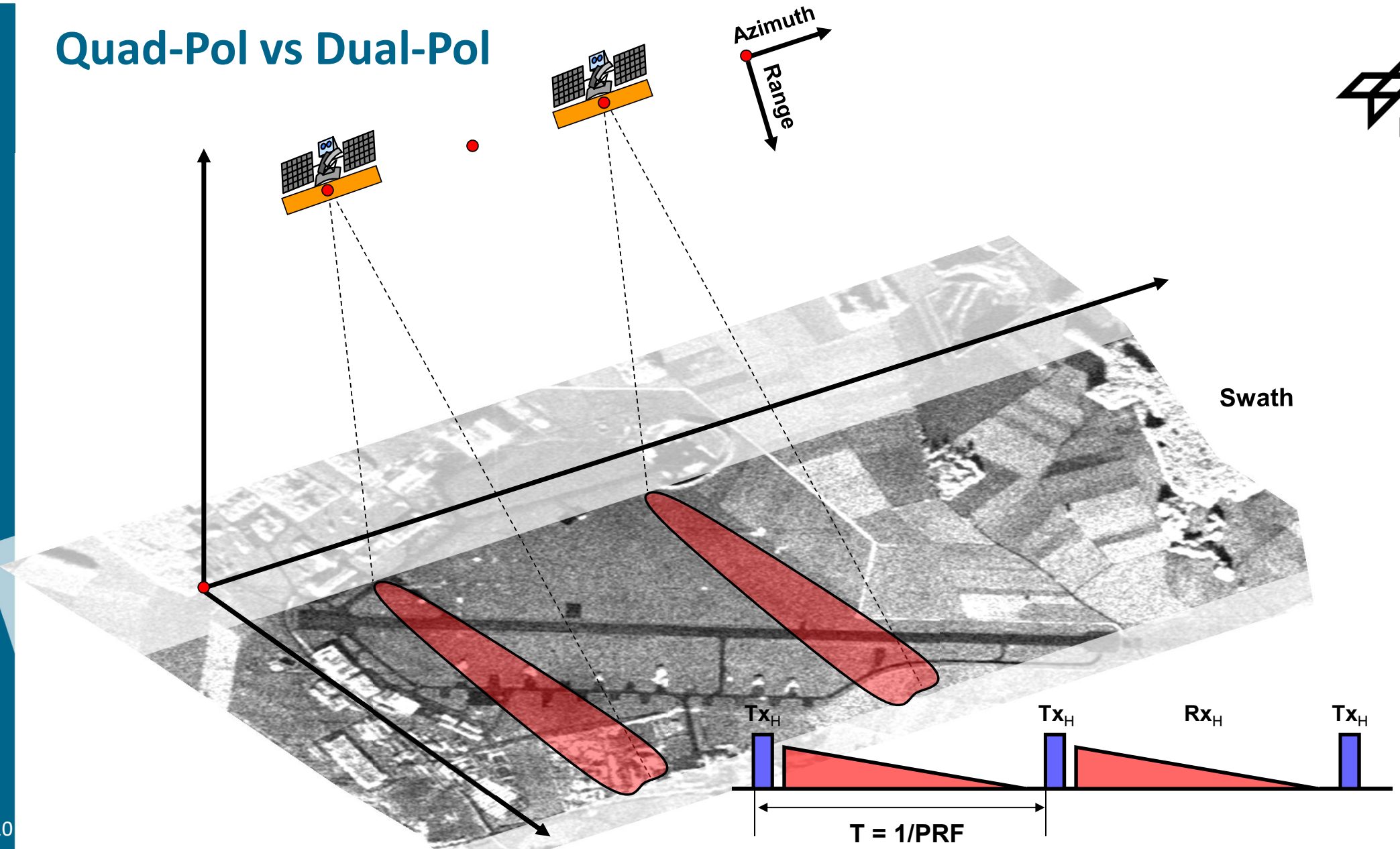
Quad Polarimetric Observation



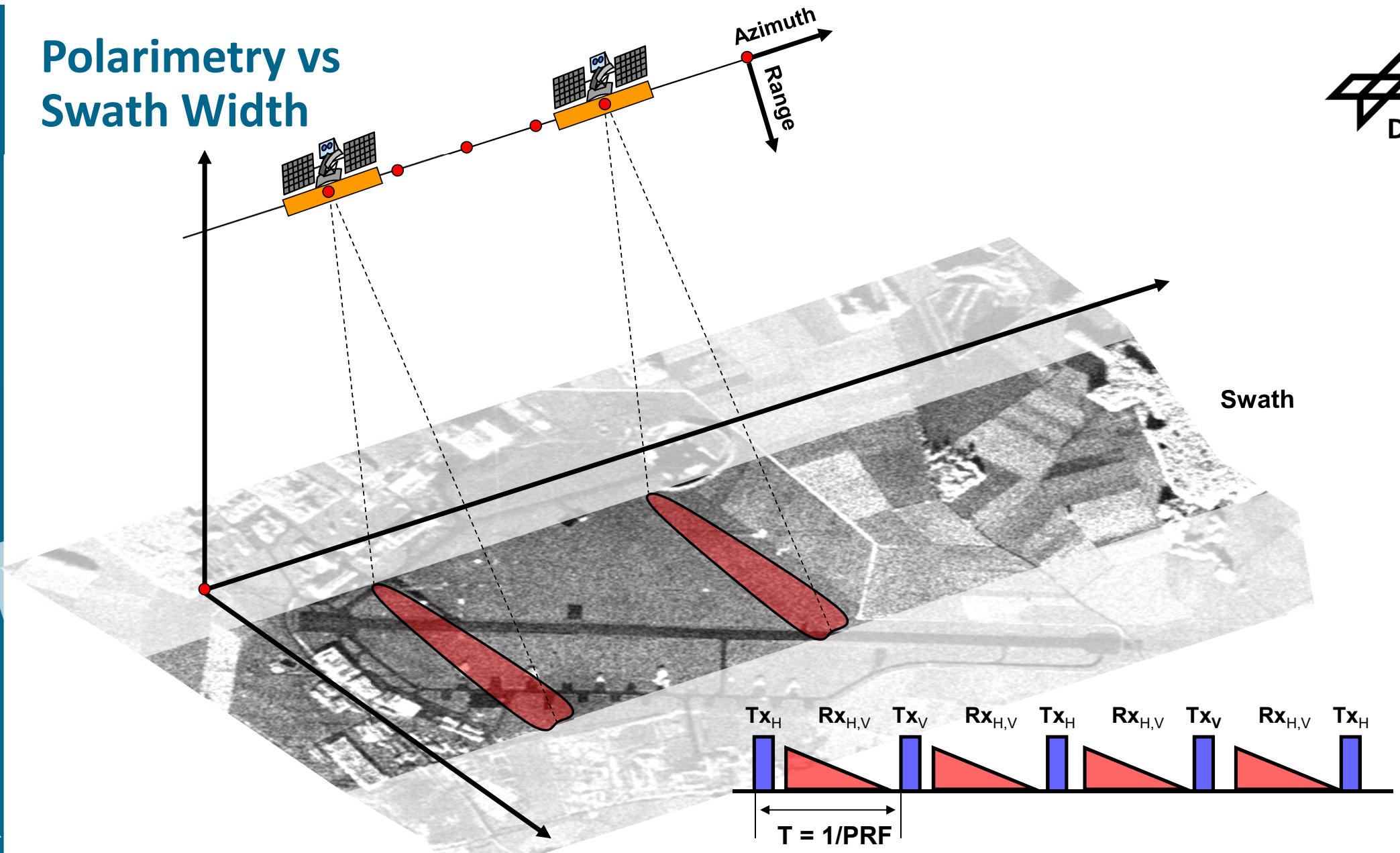
Quad Pol

H	$\begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$	H	$\begin{bmatrix} E_H^R \\ E_V^R \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix} = \begin{bmatrix} S_{HH} \\ S_{VH} \end{bmatrix}$
V	$\begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$	V	$\begin{bmatrix} E_H^R \\ E_V^R \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \begin{bmatrix} S_{HV} \\ S_{VV} \end{bmatrix}$

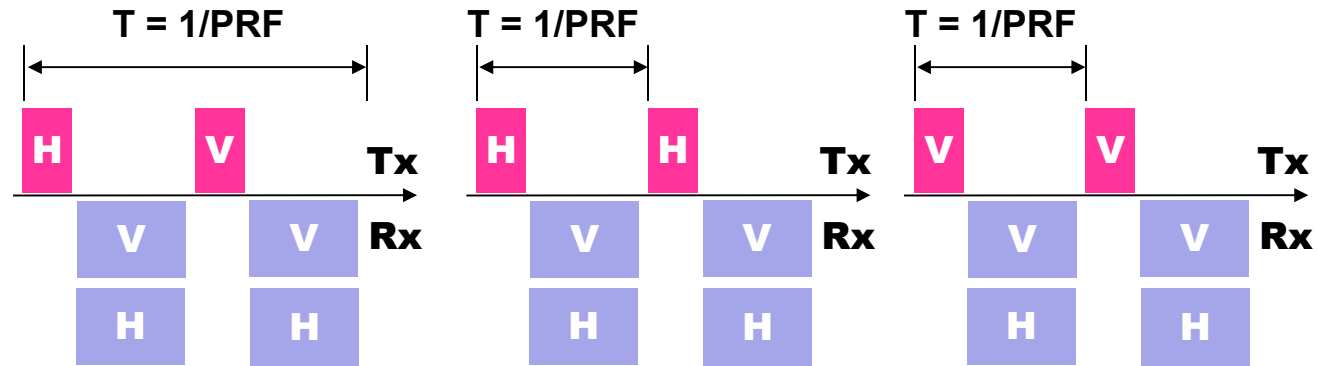
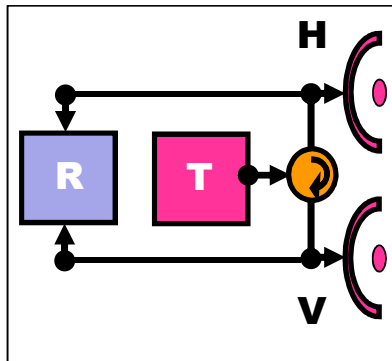
Quad-Pol vs Dual-Pol



Polarimetry vs Swath Width



Quad vs Dual Polarimetric Observations



Quad Pol

H	$\begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$	H	$\begin{bmatrix} E_H^R \\ E_V^R \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix}$	$\begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix} = \begin{bmatrix} S_{HH} \\ S_{VH} \end{bmatrix}$
V	$\begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$	H	$\begin{bmatrix} E_H^R \\ E_V^R \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix}$	$\begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \begin{bmatrix} S_{HV} \\ S_{VV} \end{bmatrix}$

Dual Pol H

H	$\begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$	H	$\begin{bmatrix} E_H^R \\ E_V^R \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix}$	$\begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix} = \begin{bmatrix} S_{HH} \\ S_{VH} \end{bmatrix}$
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Dual Pol V

V	$\begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$	H	$\begin{bmatrix} E_H^R \\ E_V^R \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix}$	$\begin{bmatrix} E_H^T \\ E_V^T \end{bmatrix} = \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} 0 \\ 1 \end{bmatrix} = \begin{bmatrix} S_{HV} \\ S_{VV} \end{bmatrix}$
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Dual Polarimetry – 2nd Order Descriptors



$$[C_3] = \langle \vec{k}_{3L} \cdot \vec{k}_{3L}^+ \rangle = \begin{bmatrix} C_{11} & C_{12} & C_{13} \\ C_{21} & C_{22} & C_{23} \\ C_{31} & C_{32} & C_{33} \end{bmatrix}$$

3D Coherence (Covariance) Matrix
9 Parameters

$$[C_2] = \langle \vec{k}_{2D} \cdot \vec{k}_{2D}^+ \rangle = \left\langle \begin{bmatrix} S_A \\ S_B \end{bmatrix} \begin{bmatrix} S_A^* & S_B^* \end{bmatrix} \right\rangle = \begin{bmatrix} \langle |S_A|^2 \rangle & \langle S_A S_B^* \rangle \\ \langle S_B S_A^* \rangle & \langle |S_B|^2 \rangle \end{bmatrix}$$

2D Covariance (Coherence) Matrix

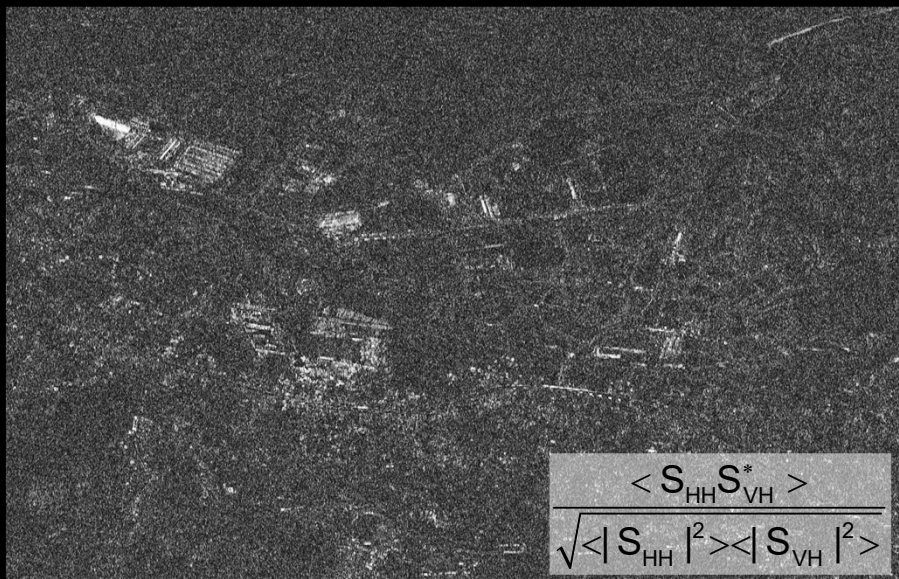
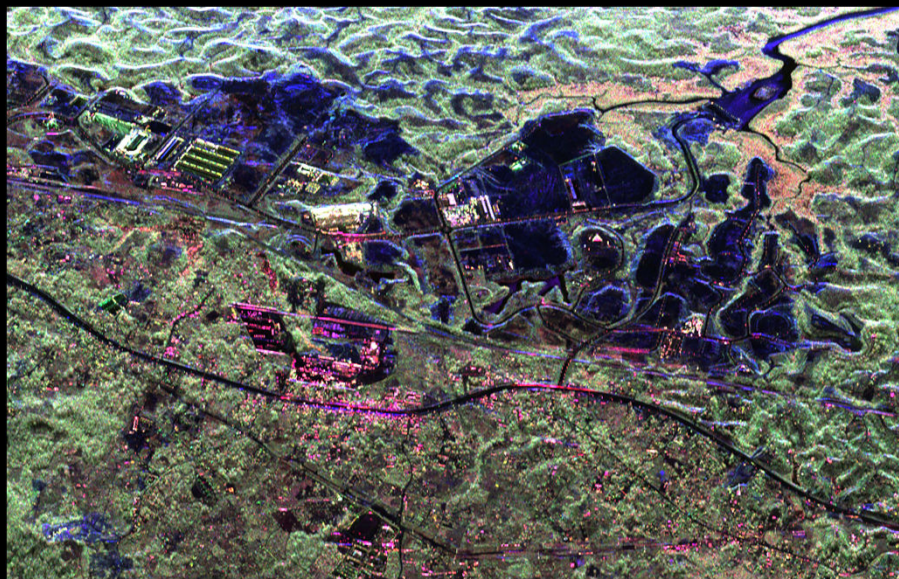
4 Parameters

$$[C_2] = [M][C_3][M]^T \quad \text{with} \quad [M] = \begin{bmatrix} m_{11} & m_{12} & m_{13} \\ m_{21} & m_{22} & m_{23} \end{bmatrix}$$

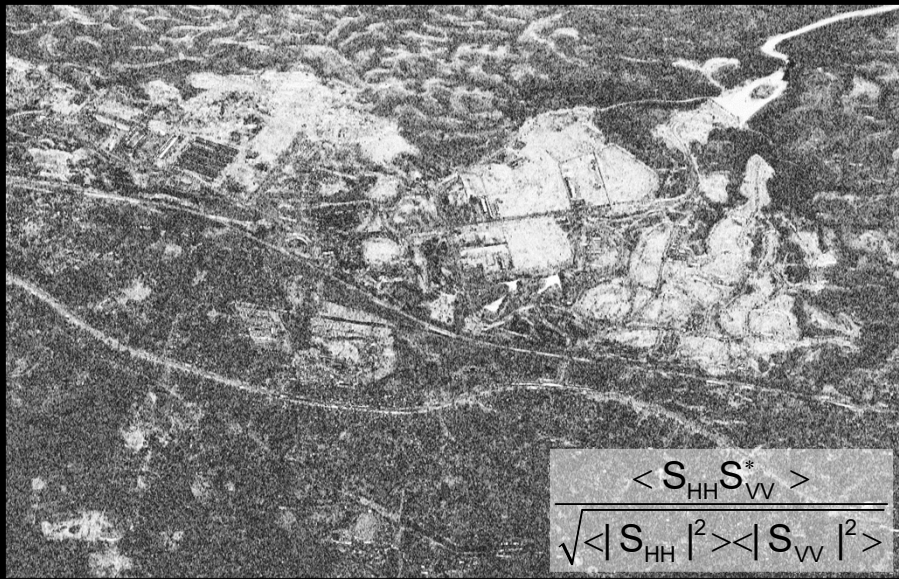
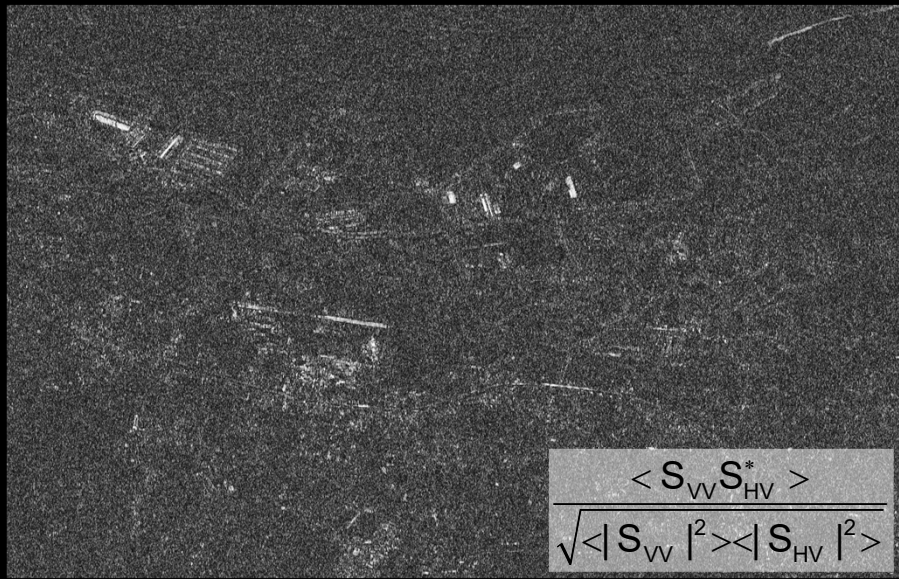
Case 1: HH-VH $[M] = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \Rightarrow [C_2] = \begin{bmatrix} \langle |S_{HH}|^2 \rangle & \langle S_{HH} S_{VH}^* \rangle \\ \langle S_{VH} S_{HH}^* \rangle & \langle |S_{HV}|^2 \rangle \end{bmatrix}$

Case 2: VV-HV $[M] = \begin{bmatrix} 1 & -1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \Rightarrow [C_2] = \begin{bmatrix} \langle |S_{VV}|^2 \rangle & \langle S_{VV} S_{HV}^* \rangle \\ \langle S_{HV} S_{VV}^* \rangle & \langle |S_{HV}|^2 \rangle \end{bmatrix}$

Case 3: HH-VV $[M] = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} \Rightarrow [C_2] = \begin{bmatrix} \langle |S_{HH}|^2 \rangle & \langle S_{HH} S_{VV}^* \rangle \\ \langle S_{HH} S_{VV}^* \rangle & \langle |S_{VV}|^2 \rangle \end{bmatrix}$



$$\frac{\langle S_{HH} S_{VH}^* \rangle}{\sqrt{\langle |S_{HH}|^2 \rangle \langle |S_{VH}|^2 \rangle}}$$



$$\frac{\langle S_{VV} S_{HV}^* \rangle}{\sqrt{\langle |S_{VV}|^2 \rangle \langle |S_{HV}|^2 \rangle}}$$

$$\frac{\langle S_{HH} S_{VV}^* \rangle}{\sqrt{\langle |S_{HH}|^2 \rangle \langle |S_{VV}|^2 \rangle}}$$

Dual Polarimetry – 2nd Order Descriptors



$$[C_3] = \langle \vec{k}_{3L} \cdot \vec{k}_{3L}^+ \rangle = \begin{bmatrix} C_{11} & C_{12} & C_{13} \\ C_{21} & C_{22} & C_{23} \\ C_{31} & C_{32} & C_{33} \end{bmatrix}$$

3D Coherence (Covariance) Matrix
9 Parameters

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2D Covariance (Coherence) Matrix

4 Parameters

$$[C_2] = [M][C_3][M]^T \quad \text{with} \quad [M] = \begin{bmatrix} m_{11} & m_{12} & m_{13} \\ m_{21} & m_{22} & m_{23} \end{bmatrix}$$

Case 1: HH-VH $[M] = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \Rightarrow [C_2] = \begin{bmatrix} \langle |S_{HH}|^2 \rangle & \langle S_{HH} S_{VH}^* \rangle \\ \langle S_{VH} S_{HH}^* \rangle & \langle |S_{HV}|^2 \rangle \end{bmatrix} = \begin{bmatrix} \langle |S_{HH}|^2 \rangle & 0 \\ 0 & \langle |S_{HV}|^2 \rangle \end{bmatrix}$

Case 2: VV-HV $[M] = \begin{bmatrix} 1 & -1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \Rightarrow [C_2] = \begin{bmatrix} \langle |S_{VV}|^2 \rangle & \langle S_{VV} S_{HV}^* \rangle \\ \langle S_{HV} S_{VV}^* \rangle & \langle |S_{HV}|^2 \rangle \end{bmatrix} = \begin{bmatrix} \langle |S_{VV}|^2 \rangle & 0 \\ 0 & \langle |S_{HV}|^2 \rangle \end{bmatrix}$

Case 3: HH-VV $[M] = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} \Rightarrow [C_2] = \begin{bmatrix} \langle |S_{HH}|^2 \rangle & \langle S_{HH} S_{VV}^* \rangle \\ \langle S_{HH} S_{VV}^* \rangle & \langle |S_{VV}|^2 \rangle \end{bmatrix}$

2-dim Polarimetry: 2nd Order Statistical Parameters



$$[T_3] := \langle \vec{k}_{3P} \cdot \vec{k}_{3P}^+ \rangle \quad \Rightarrow \quad [T_3] = [U_3][\Lambda_3][U_3]^{-1}$$

$$[\Lambda_3] = \begin{bmatrix} \lambda_1 & 0 & 0 \\ 0 & \lambda_2 & 0 \\ 0 & 0 & \lambda_3 \end{bmatrix} \quad [U_3] = \begin{bmatrix} | & | & | \\ \vec{e}_1 & \vec{e}_2 & \vec{e}_3 \\ | & | & | \end{bmatrix}$$

$$P_i := \frac{\lambda_i}{\sum \lambda_i} \quad \vec{e}_i = \begin{bmatrix} \cos \alpha_i \exp(j\varphi_{i1}) \\ \sin \alpha_i \cos \beta \exp(j\varphi_{i2}) \\ \sin \alpha_i \sin \beta \exp(j\varphi_{i3}) \end{bmatrix}$$

$$[T_2] := \langle \vec{k}_2 \cdot \vec{k}_2^+ \rangle \quad \Rightarrow \quad [T_2] = [U_2][\Lambda_2][U_2]^{-1}$$

$$[\Lambda_2] = \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} \quad [U_2] = \begin{bmatrix} | & | \\ \vec{e}_1 & \vec{e}_2 \\ | & | \end{bmatrix}$$

$$P_i := \frac{\lambda_i}{\sum \lambda_i} \quad \vec{e}_i = \begin{bmatrix} \cos \alpha_i \exp(j\varphi_{i1}) \\ \sin \alpha_i \exp(j\varphi_{i2}) \end{bmatrix}$$

$$\alpha_1 ; \alpha_2 = \frac{\pi}{2} - \alpha_1$$

$$H := \sum_{i=1}^3 P_i \log_3 P_i \quad A := \frac{P_2 - P_3}{P_2 + P_3} \quad \alpha := \sum_{i=1}^3 P_i \alpha_i$$

Entropy Anisotropy Alpha Angle

$$H := \sum_{i=1}^2 P_i \log_2 P_i$$

Entropy
randomness

$$A := \frac{P_1 - P_2}{P_1 + P_2}$$

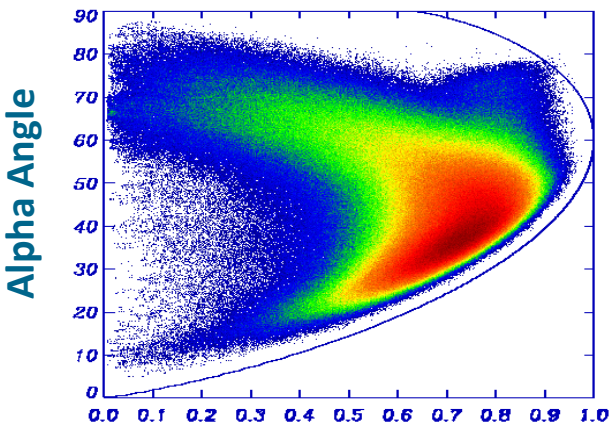
Anisotropy

$$\alpha := \sum_{i=1}^2 P_i \alpha_i$$

Alpha Angle
scat.mechan.

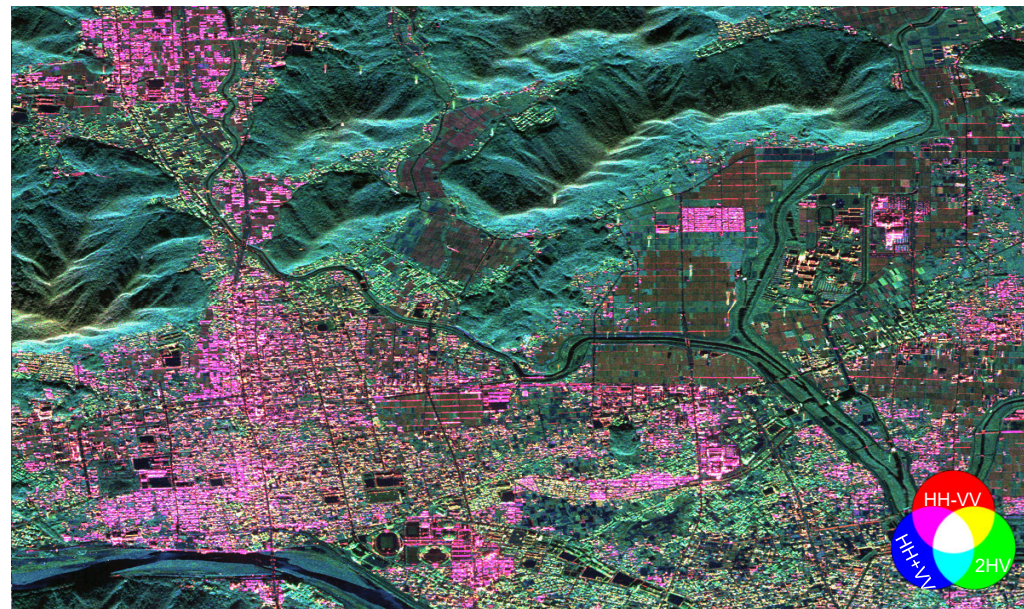
2-dim Polarimetry – 2nd Order

Example X-band from PI-SAR Test Site: Gifu



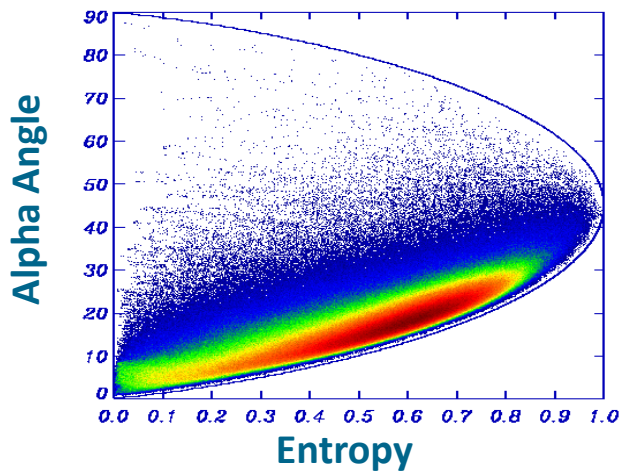
Quad Pol

Entropy



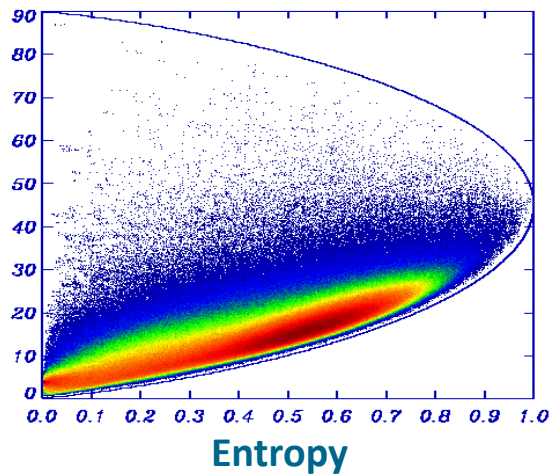
PI-SAR / Test Site: Gifu, Japan

Dual Pol Case 1: Tx: H



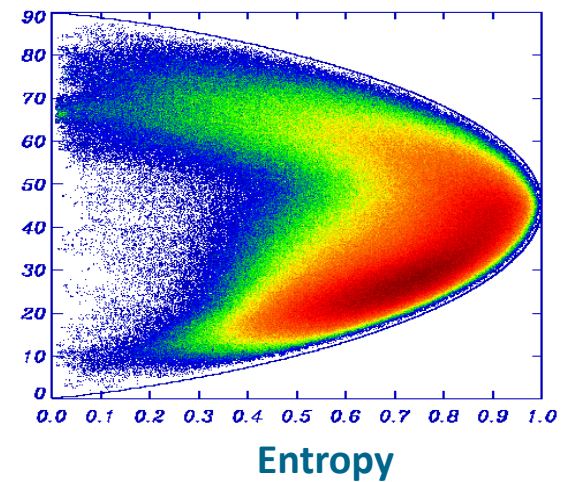
Entropy

Dual Pol Case 2: Tx: V



Entropy

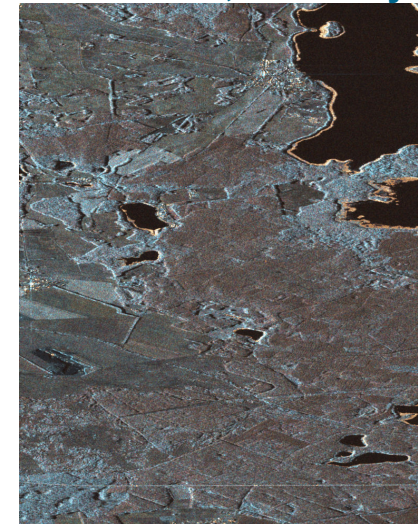
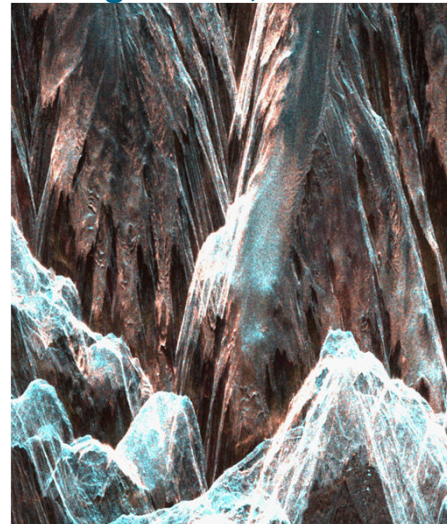
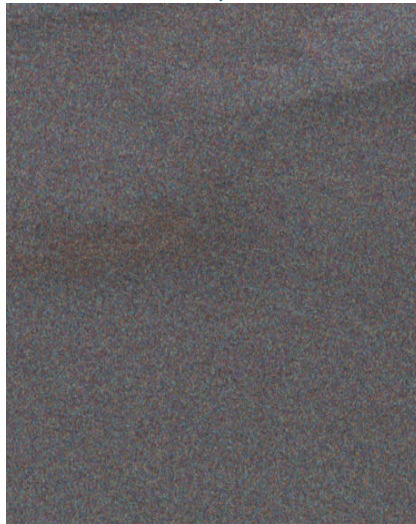
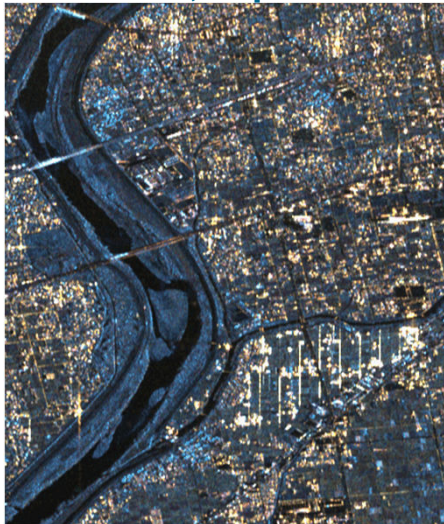
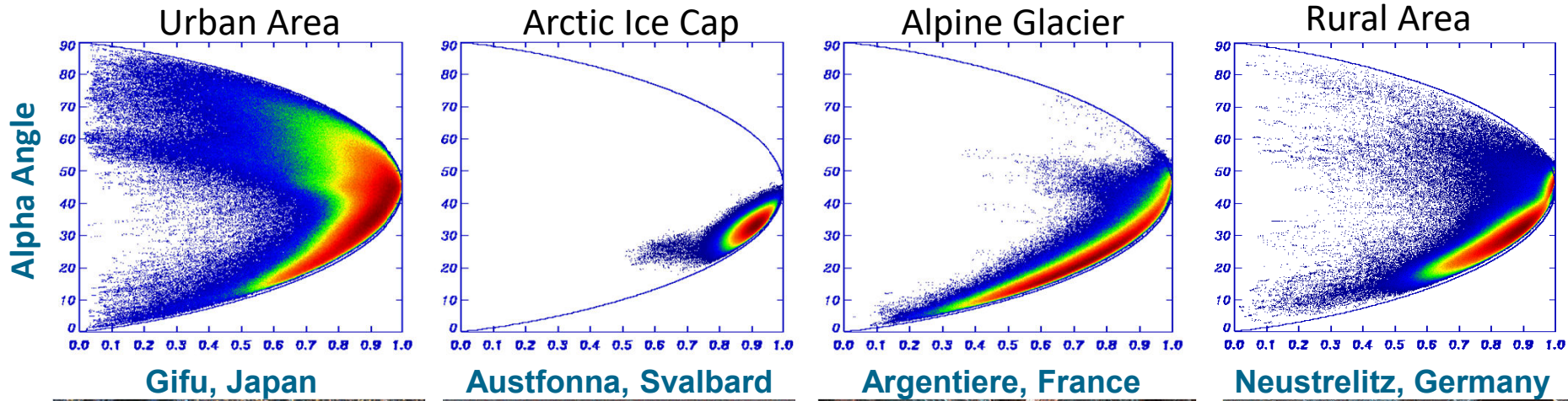
Dual Pol Case 3: Tx: H & V



Entropy

2-dim Polarimetry – 2nd Order

Example from TerraSAR-X for different surface types



TanDEM-X: The Great Aletsch Glacier and Available Data



The Great Aletsch Glacier

- ✓ Length 23 km
- ✓ Surface 86 km³
- ✓ From ~1800 m to ~3500 m altitude
- ✓ Negative mass balance since 1881
- ✓ Front retreats up to 4 m/year
- ✓ Equilibrium Line at 3000 m

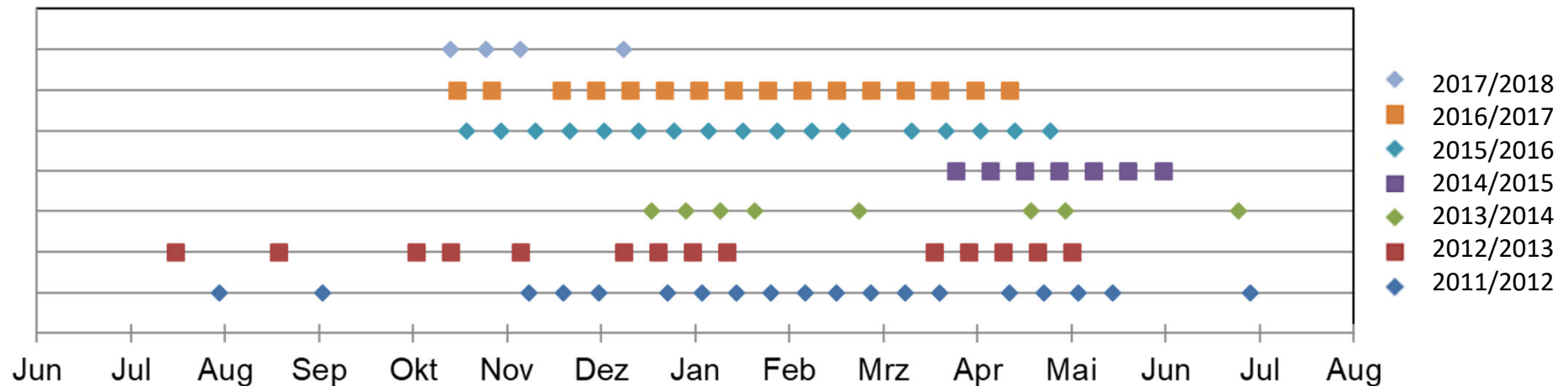


Map of Switzerland, Aletsch is marked

Source: Map.geo.admin.ch (Schweizerische Eidgenossenschaft), Date: 25.06.18

SAR Data

- ✓ TanDEM-X time series
- ✓ Dual-Pol (HH and VV)
- ✓ 7-year time period (2011-2018)
- ✓ 86 acquisitions from same orbit
- ✓ rg x az = 1,76 x 6,6 m resolution
- ✓ Incidence angle $\theta_{inc} = 31,6^\circ$



Great Aletsch Glacier / Grosser Aletschgletscher

- 23 km long
- Covers 80 square kilometers
- over 800 meters thick ice
- 15 cubic kilometers of ice
- 20% of the entire Swiss Ice mass

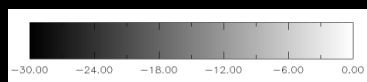
- expected to lose 90% of it's mass until 2100.

Jouvet et al. J. Glac. (2011)

L. Leinss

Aletschgletscher, Switzerland

2011 - 2012 Time series σ_{HH}^0



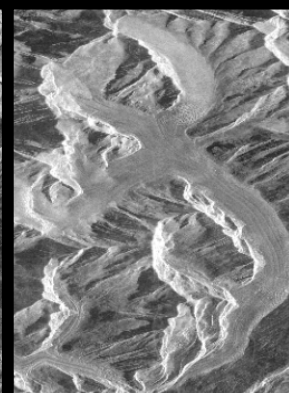
28. Nov 2011



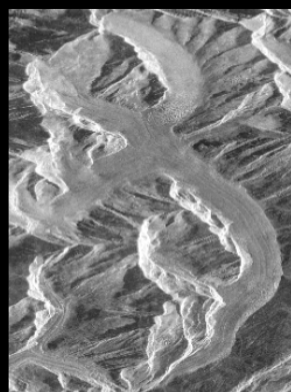
09. Dec 2011



20. Dec 2011



11. Jan 2012



22. Jan 2012



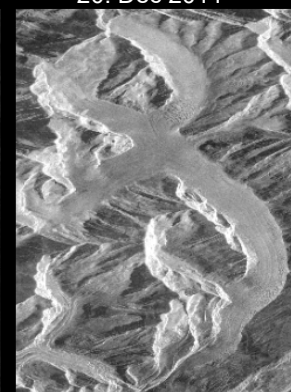
02. Feb 2012



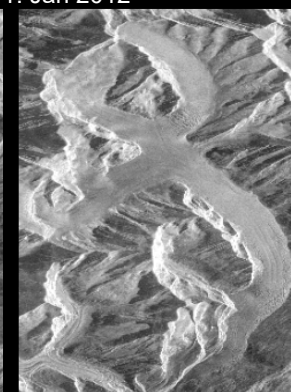
24. Feb 2012



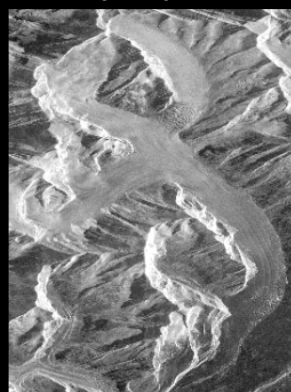
06. Mar 2012



17. Mar 2012



28. Mar 2012



08. Apr 2012



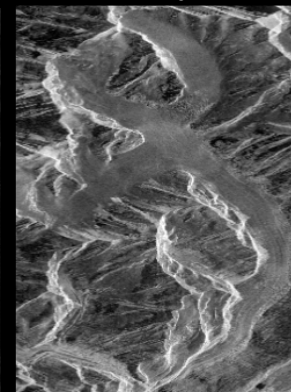
30. Apr 2012



11. May 2012



22. May 2012



02. Jun 2012



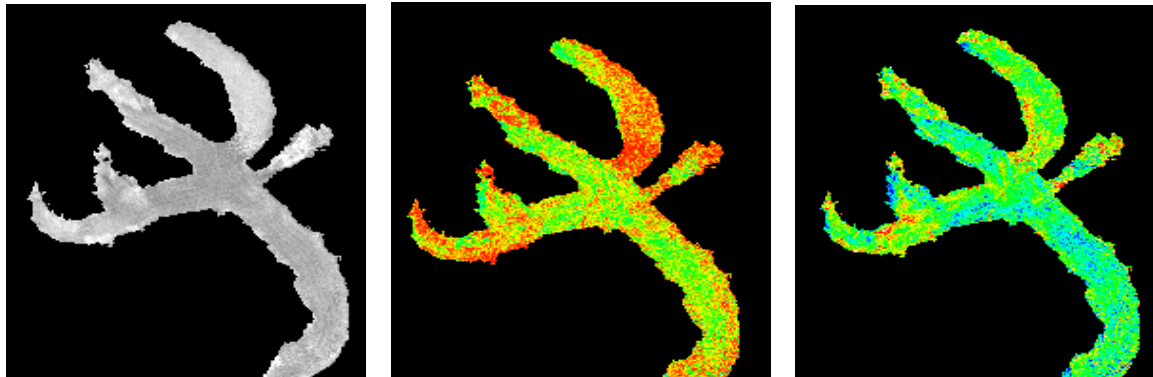
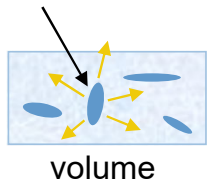
16. Jul 2012

Polarimetric Analysis: Sensitivity to Seasonal Dynamics



✓ Wet and dry glacier conditions

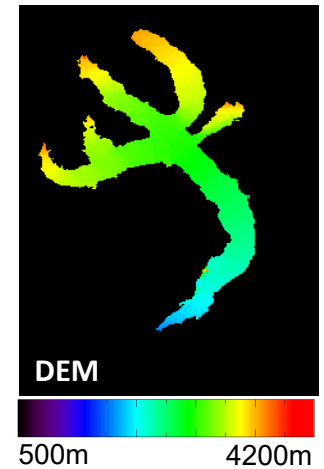
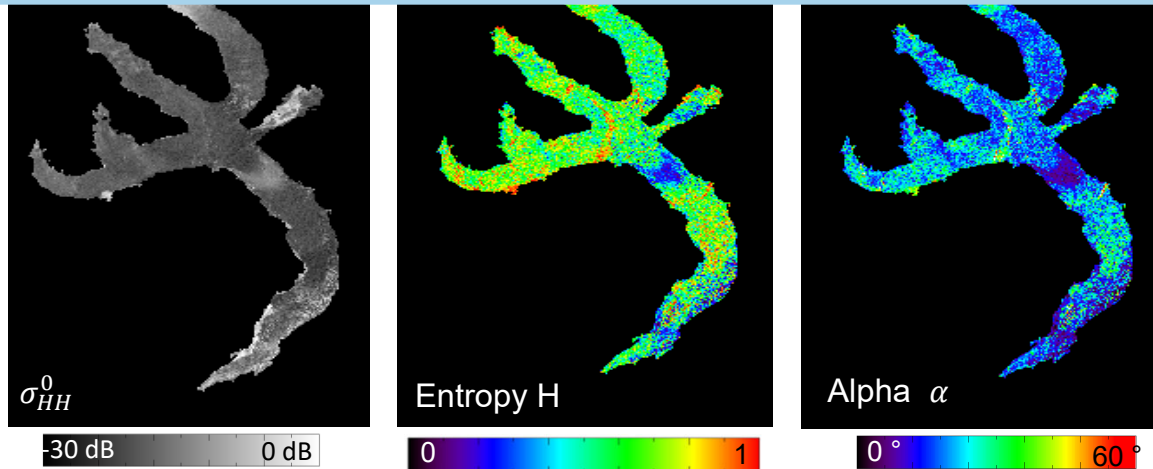
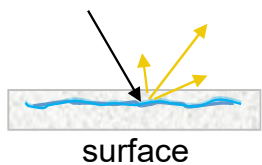
Winter image
08.02.2013



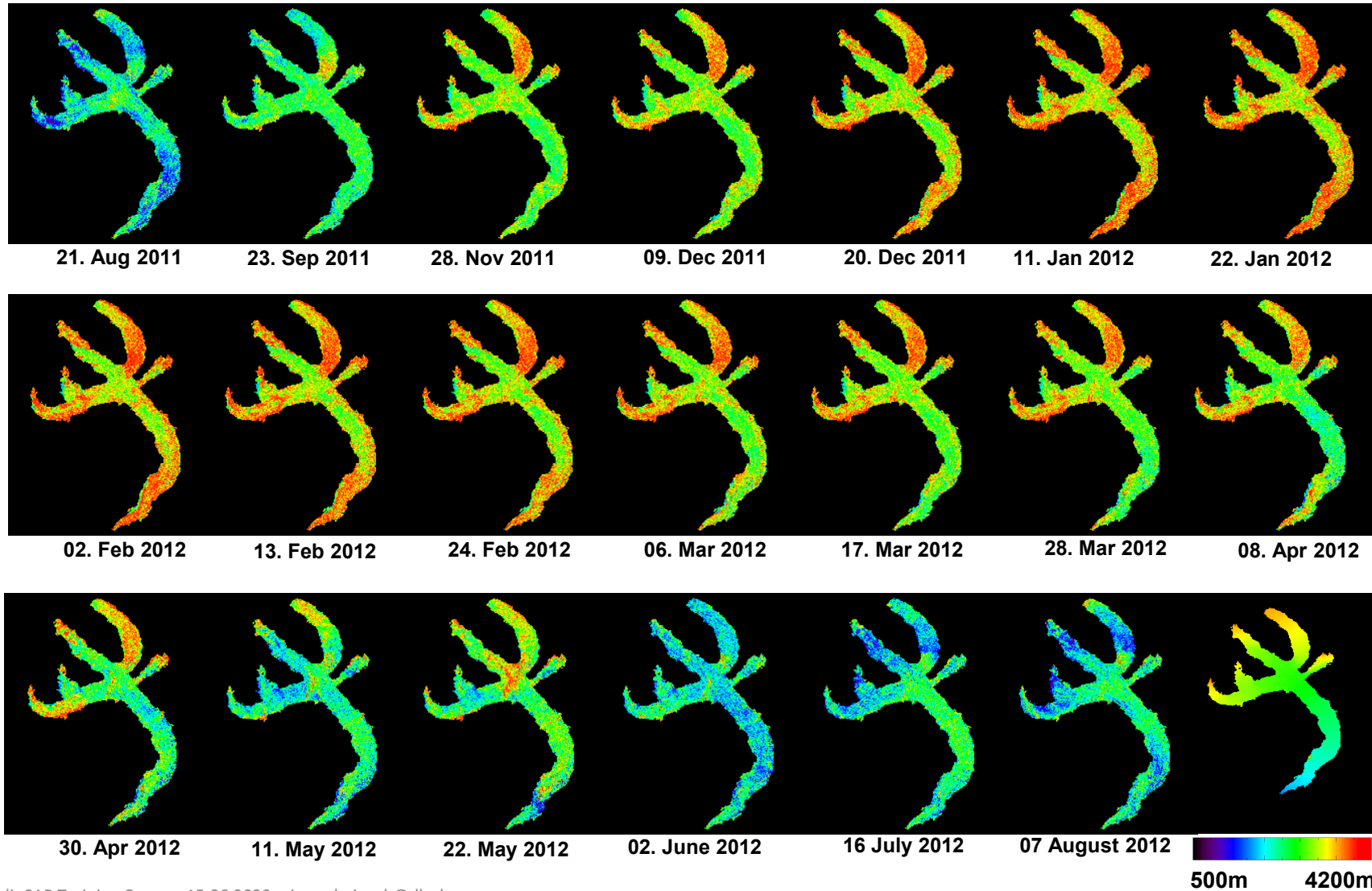
Scattering mechanisms vary with snow/ice conditions...

...but also within a single scene!

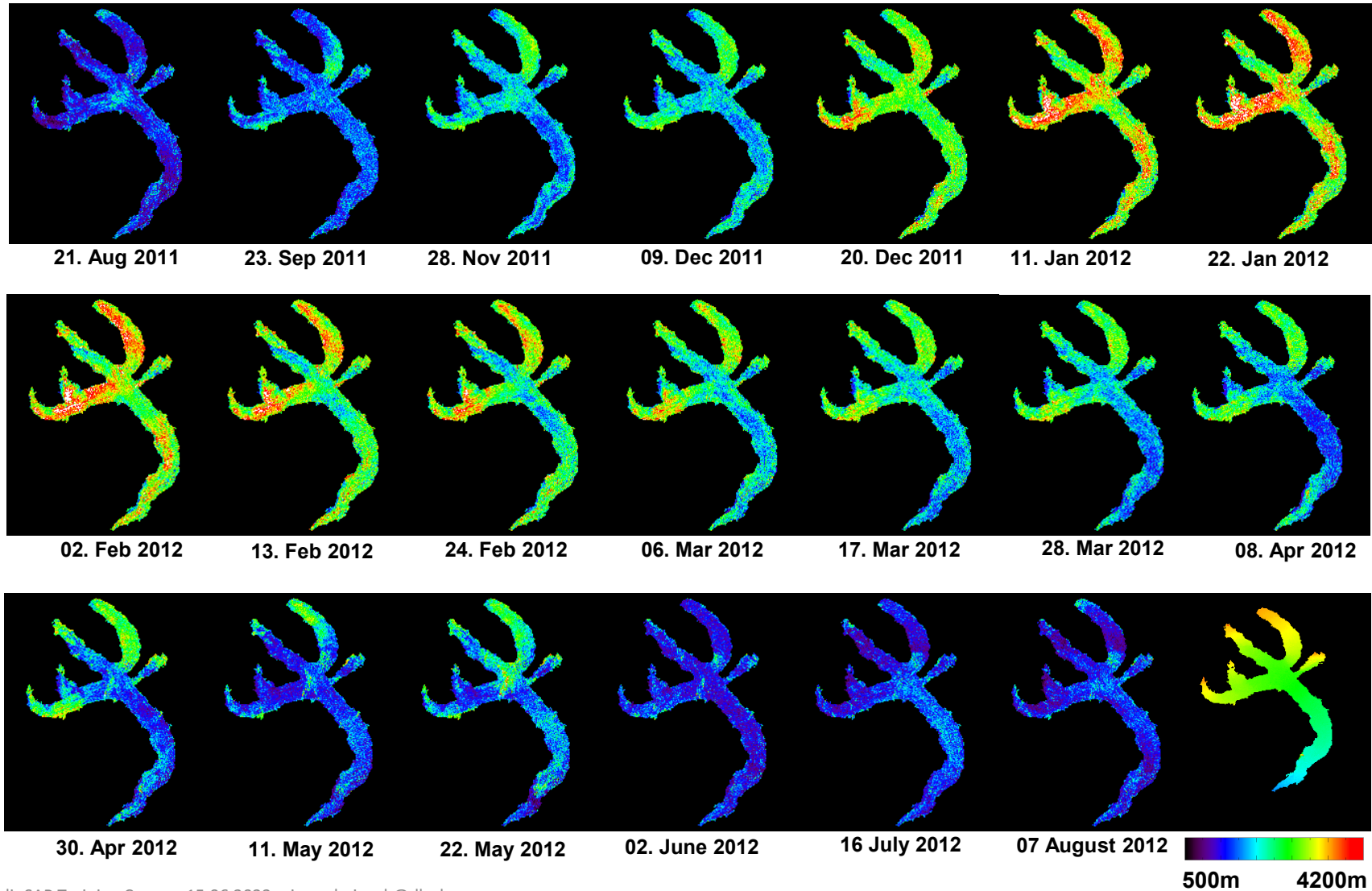
Summer image
09.05.2013



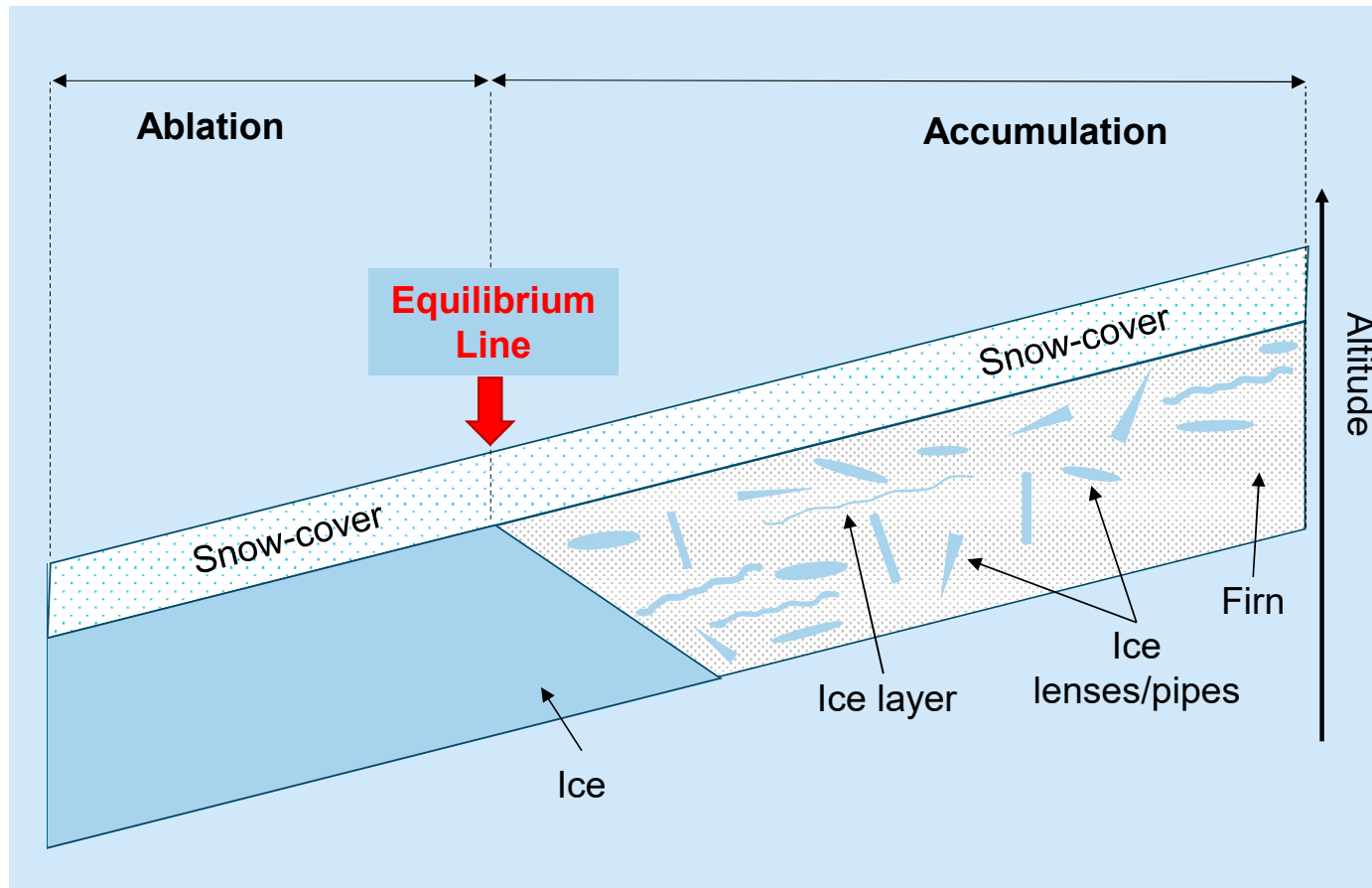
Entropy Time Series 2011/012



Alpha Angle Time Series 2011/012

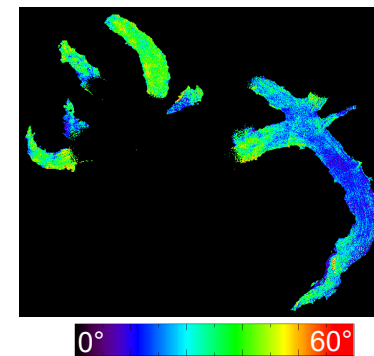
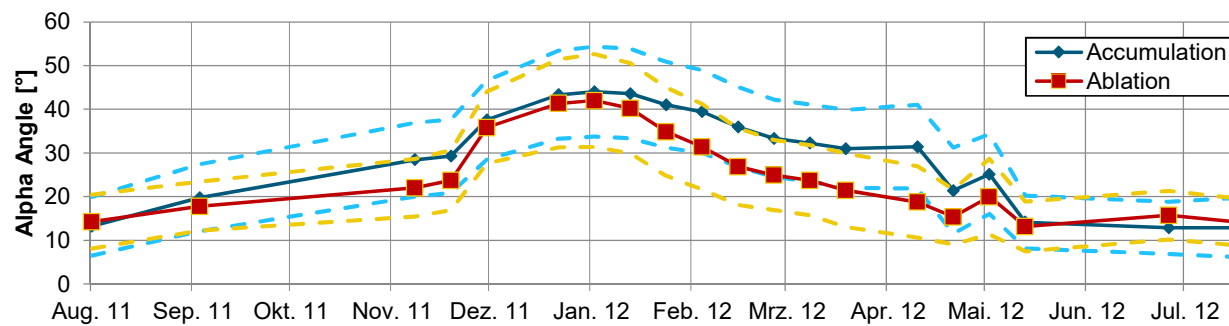
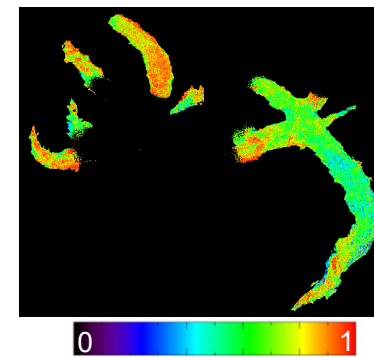
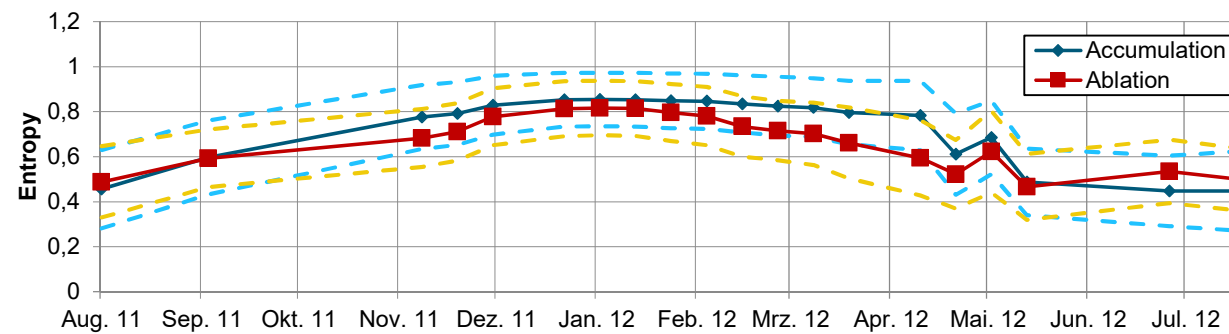
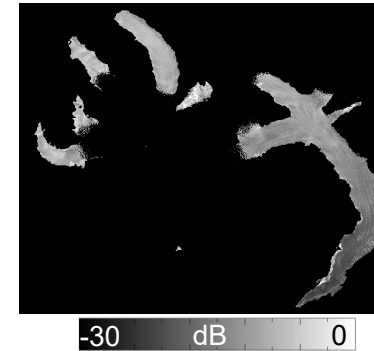
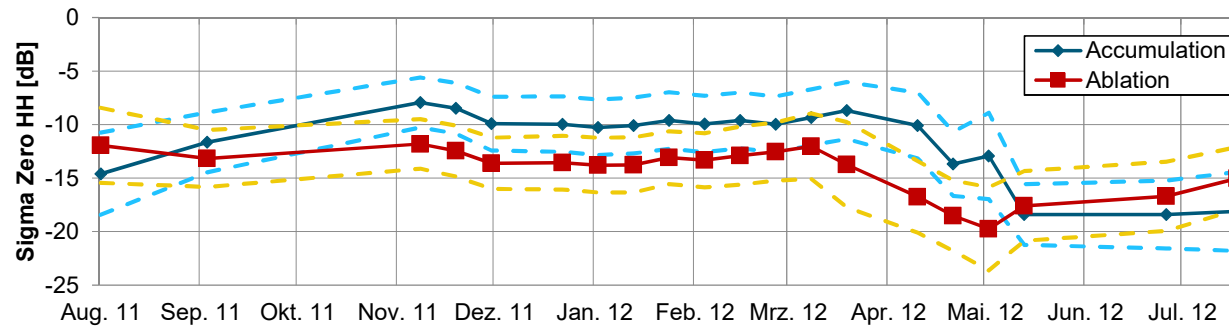


Basics of Glaciology

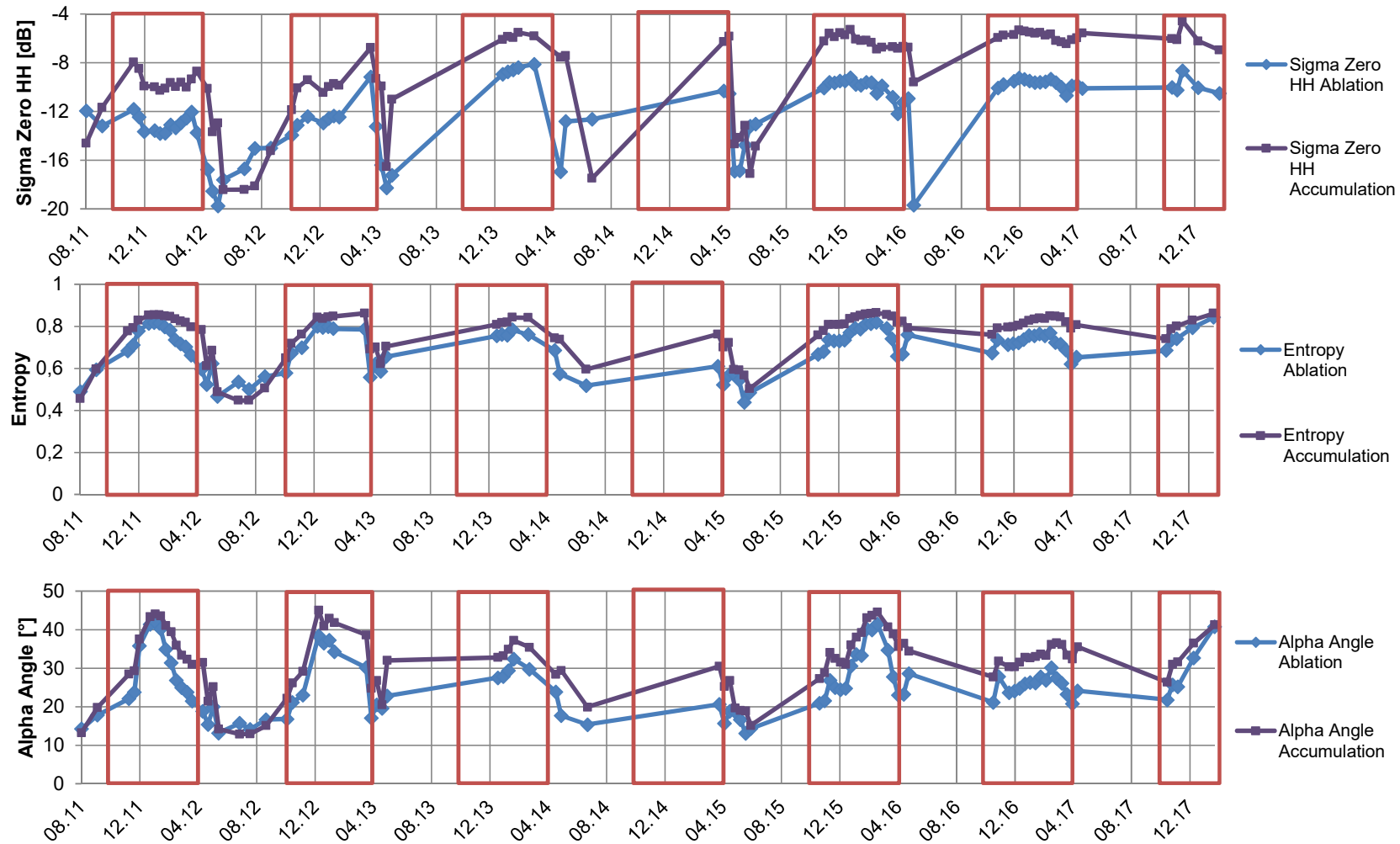


The **equilibrium-line (ELA) altitude** is a **line** on the **glacier** where accumulation equals ablation

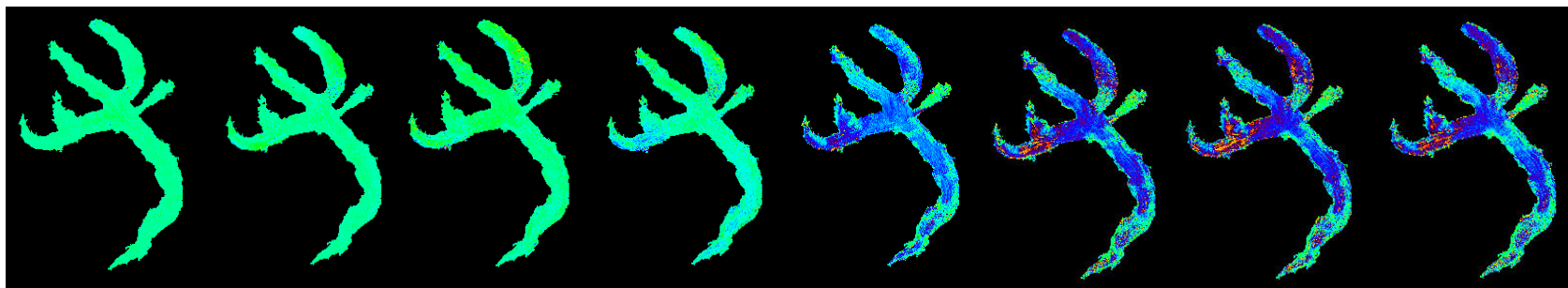
Polarimetric Analysis: Seasonal Dynamics of Glacier Zones



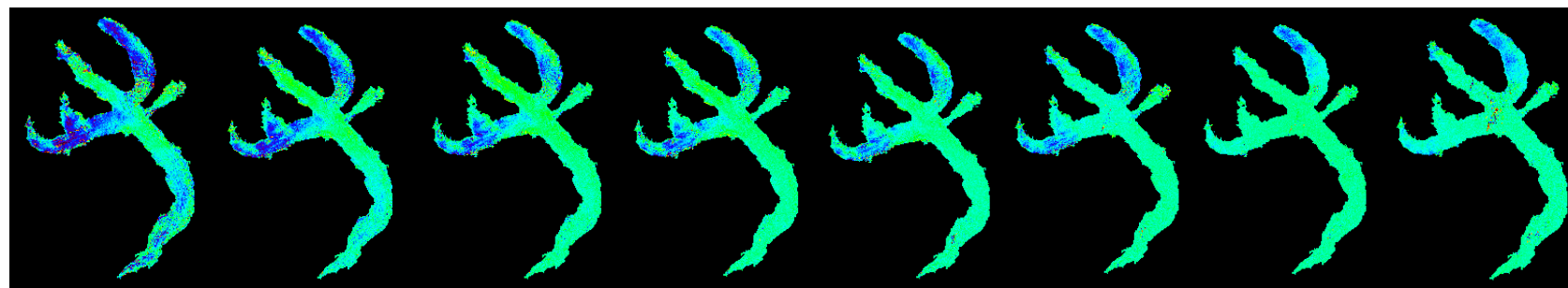
Polarimetric Analysis: Interannual Dynamics of Glacier Zones



Polarimetric Phase Diff. and Snow Accumulation



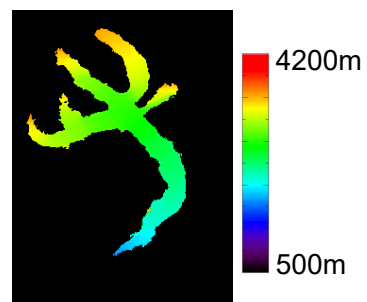
21. Aug 2011 23. Sep 2011 28. Nov 2011 09. Dec 2011 20. Dec 2011 11. Jan 2012 22. Jan 2012 02. Feb 2012



24. Feb 2012 06. Mar 2012 17. Mar 2012 28. Mar 2012 08. Apr 2012 30. Apr 2012 11. May 2012 22. May 2012

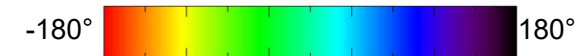


02. Jun 2012 16. Jul 2012



✓ Polarimetric Phase difference ϕ_{VV-HH}

$$\phi_{VV-HH} = \angle(\langle S_{VV} S_{HH}^* \rangle)$$

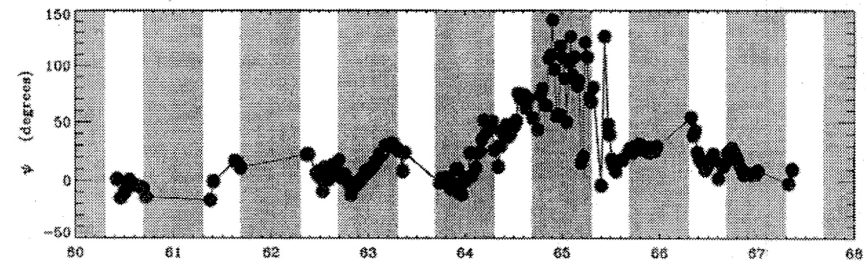


Why is snow depth proportional to $(\phi_{VV} - \phi_{HH})$?



- Fresh snow causes the highest phase differences
-> Also observed by [Chang, 1993] at 95 GHz.

Chang, P. et al. «Polarimetric backscatter from fresh and metamorphic snowcover at millimeter wavelengths», *IEEE Transactions on Antennas and Propagation*, , **1996**, 44



- Oriented particles within a volume cause polarization dependent propagation speeds [Cloude, 2000], [Parrella, 2013] & [Leinss, 2016].

Cloude et al. «The Remote Sensing of Oriented Volume Scattering Using Polarimetric Radar Interferometry.», *Proceedings of ISAP*, Fukuoka, Japan, **2000**.

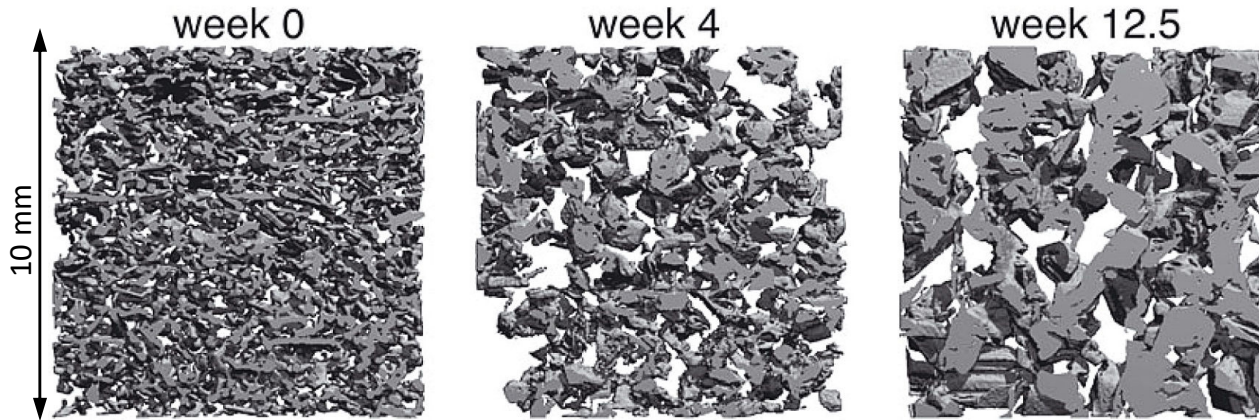
Parrella, G. “On the Interpretation of L- and P-band PolSAR Signatures of Polithermal Glaciers”, *POLInSAR*, **2013**

Leinss, S. “Anisotropy of seasonal snow measured by polarimetric phase differences in radar time series. *The Cryosphere* **2016**”

- Recrystallization of snow changes the shape and orientation of ice grains in a snow cover driven by a vertical temperature gradient. [Riche, 2013]

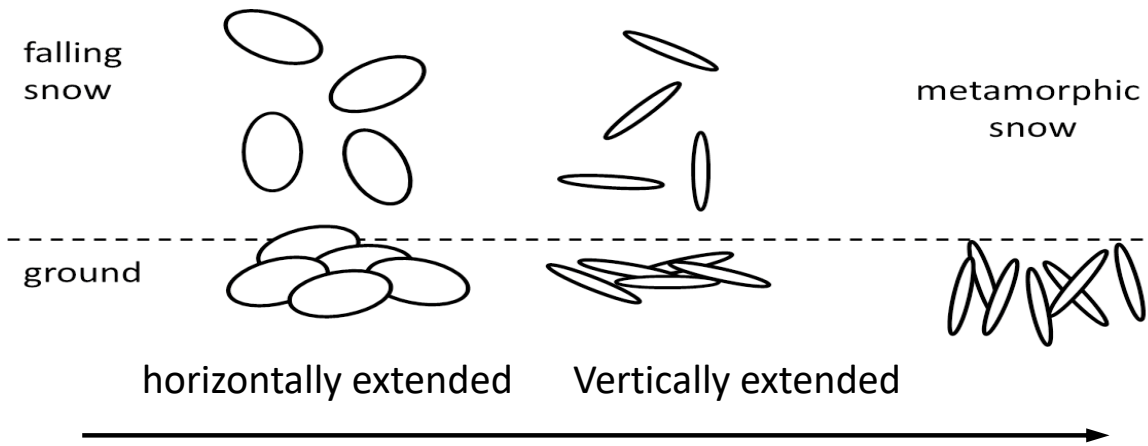
Riche, F. et al. “Evolution of crystal orientation in snow during temperature gradient metamorphism”, *Journal of Glaciology*, **2013**, 59, 47-55

Why is snow depth proportional to $(\phi_{VV} - \phi_{HH})$?



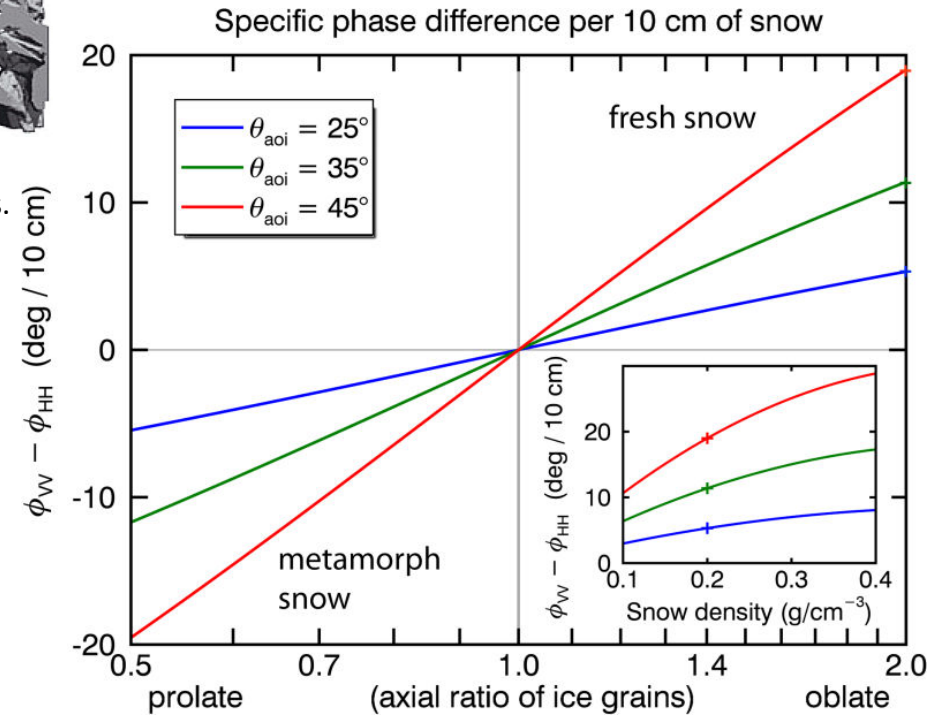
> 11 recrystallization cycles after 12 weeks.

Simplification for model:



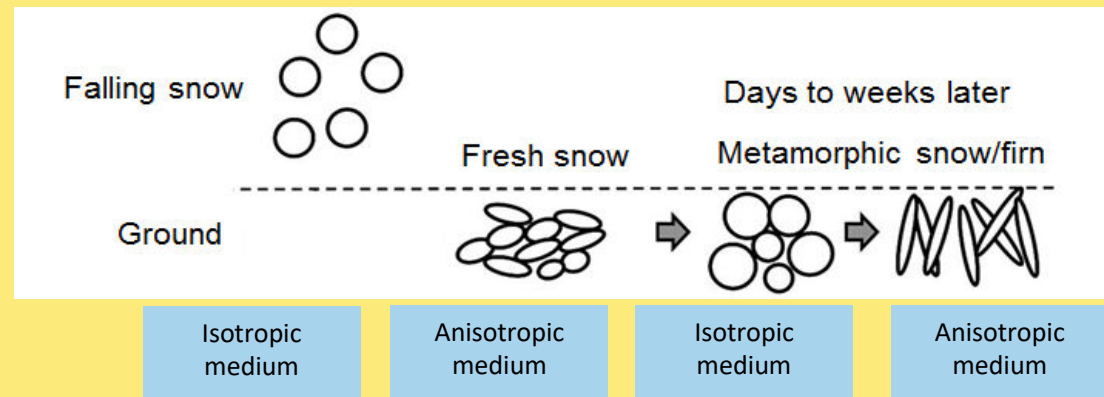
Recrystallization speed depends on temp. gradient dT/dz

Riche, F. et al. "Evolution of crystal orientation in snow during temperature gradient metamorphism", *Journal of Glaciology*, **2013**, 59, 47-55



Parrella, G. "On the Interpretation of L- and P-band PolSAR Signatures of Polithermal Glaciers", *POLinSAR* **2013**

Propagation Model to Invert Snow Accumulation

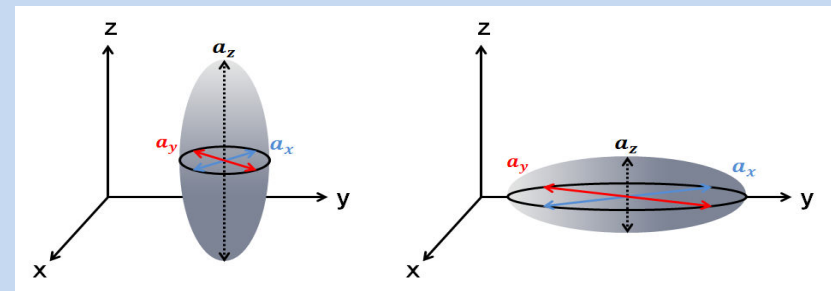


Modelling anisotropic snow

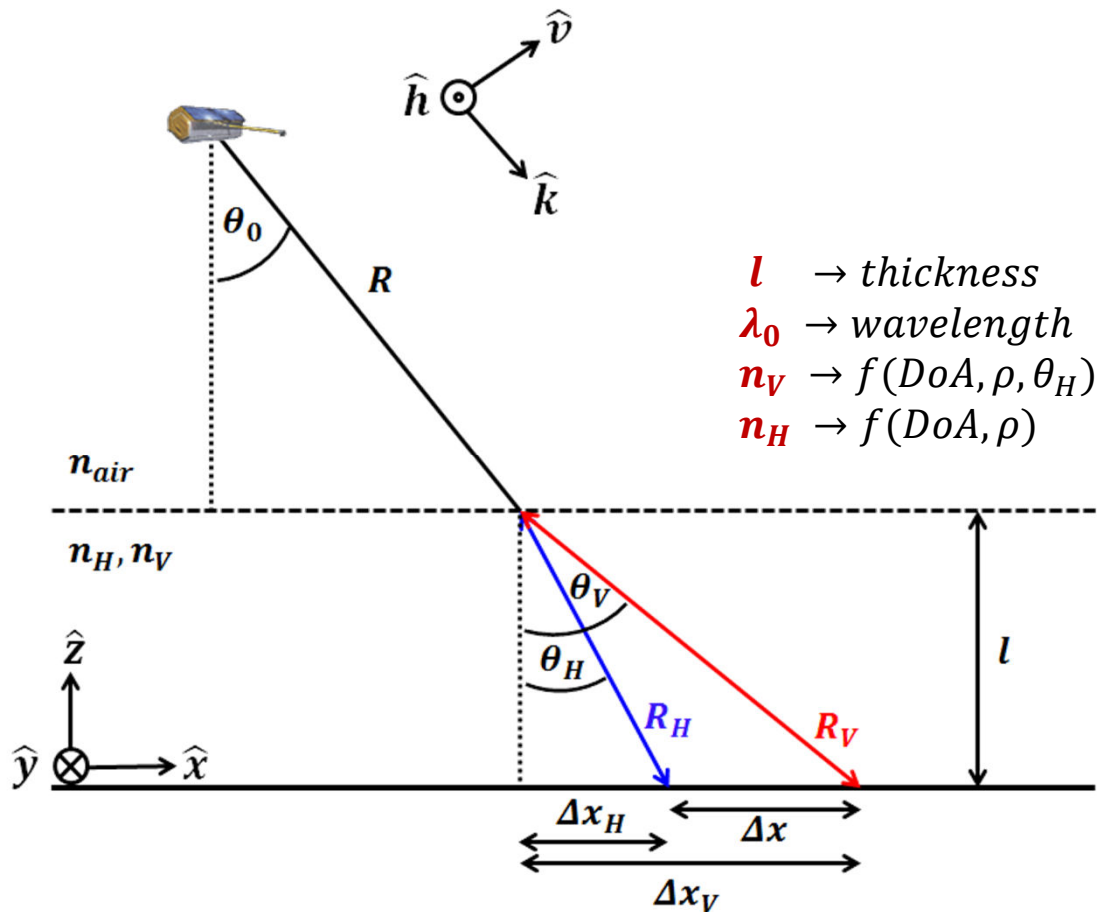
- ✓ Two phase mixture of air and ice inclusions
- ✓ Spheroidal grains described by degree of anisotropy $DoA = \frac{a_z}{a_x}$
- ✓ Effective permittivity components depend on DoA and volume fraction (density)

$$\epsilon_{eff,x,y,z} = \epsilon_{air} + \varphi_{vol} \epsilon_{ice} \frac{\epsilon_{ice} - \epsilon_{air}}{\epsilon_{air} + (1 - \varphi_{vol}) N_{x,y,z} (\epsilon_{ice} - \epsilon_{air})}$$

- ✓ Refractive indices $n_{x,y}$ and n_z ($n^2 = \epsilon_r$)



Propagation Model to Invert Snow Accumulation



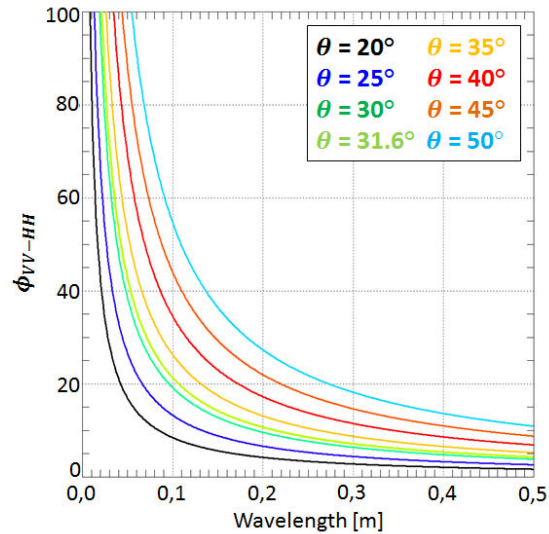
- ✓ Transformation from $(x,y,z) \rightarrow (H,V)$ coordinate system
- ✓ H component $n_H = n_{x,y}$
- ✓ V component $n_V = \sqrt{n_x^2 \cos^2 \theta_H + n_z^2 \sin^2 \theta_H}$

$$\phi_{VV-HH} = 2 \frac{2\pi}{\lambda_0} (n_V R_V - n_H R_H)$$

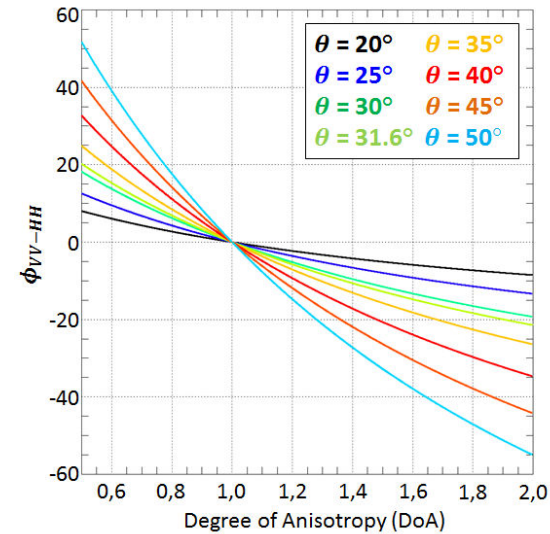
$$R_V = \frac{\cos \theta_V}{l} \quad R_H = \frac{\cos \theta_H}{l}$$

$$\phi_{VV-HH} = 2 \frac{2\pi \cdot l}{\lambda_0} \left(\frac{n_V}{\cos \theta_V} - \frac{n_H}{\cos \theta_H} \right)$$

Propagation Model: Sensitivity Analysis

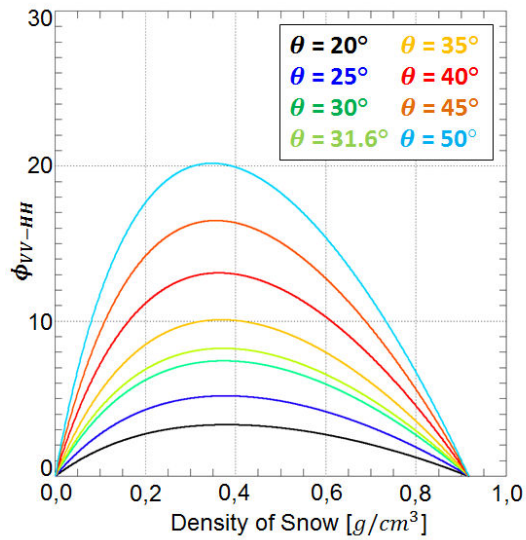


✓ Sensitivity increases with frequency

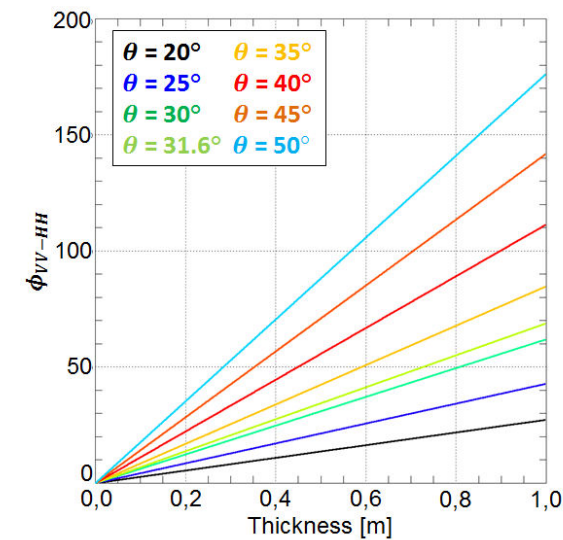


$\rho = 0,2 \text{ g/cm}^3$
 $DoA = 0,8$
 $l = 0,1\text{m}$
 $\lambda = 0,031\text{m}$

✓ More sensitive for higher anisotropy



✓ Increasing until medium is too dense



✓ Linear dependency on thickness

- build to analyze the backscatter signal from snow
- part of phase-A study for CoReH2O

SnowScat

Automatic Weather Station
Air Temp., Precipitation,
Snow Depth

AWS
500 m

17 subsectors
(azimuth samples)

5 subsectors

sector 1

four incidence angles
 $q = 30^\circ, 40^\circ, 50^\circ, 60^\circ$

Snow density,
SWE

Fully **Polarimetric Coherent** Real Aperture Radar.
Acquisition rate: **4 hours**.
Frequency: 9.2 ... 17.8 GHz

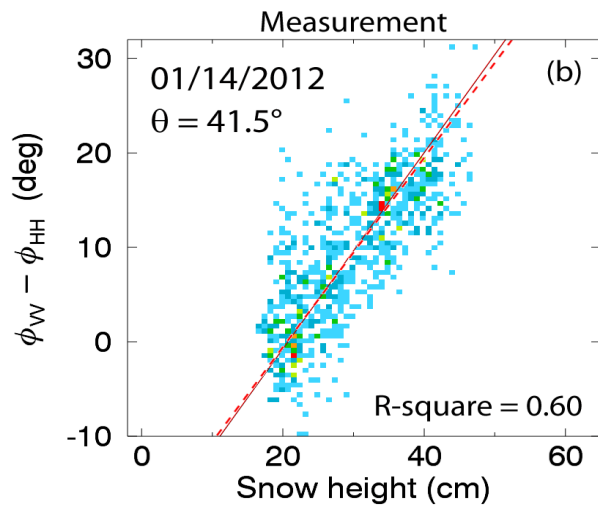
snow pit

„Gamma Water Instrument“
(SWE)

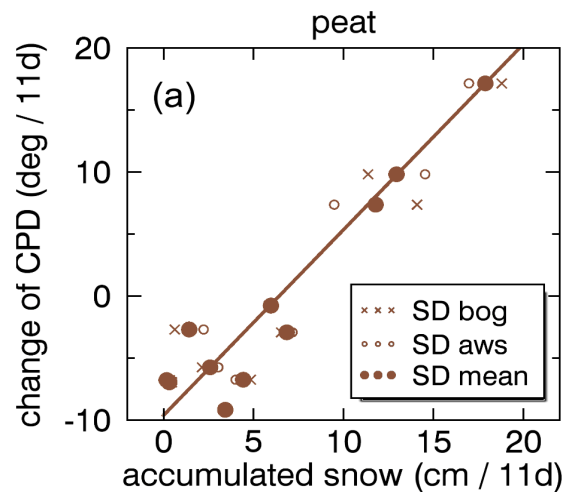
Test site: Finland, Sodankylae

Detection of Fresh Snow

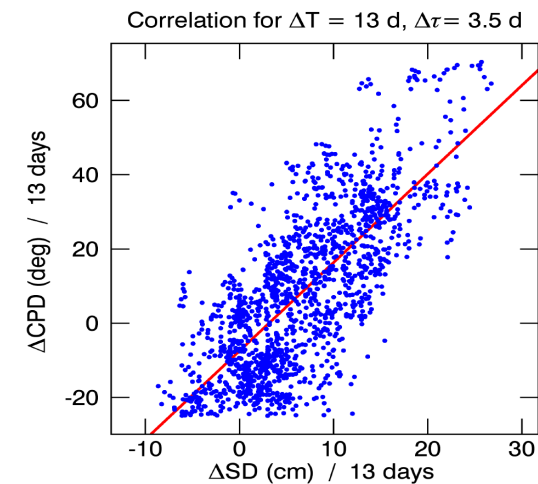
The anisotropic character of fresh snow can be used to determine the amount of fresh snow within the last few days.



- TerraSAR-X:
Total snow height after
30 days of snowfall
(spatial correlation)



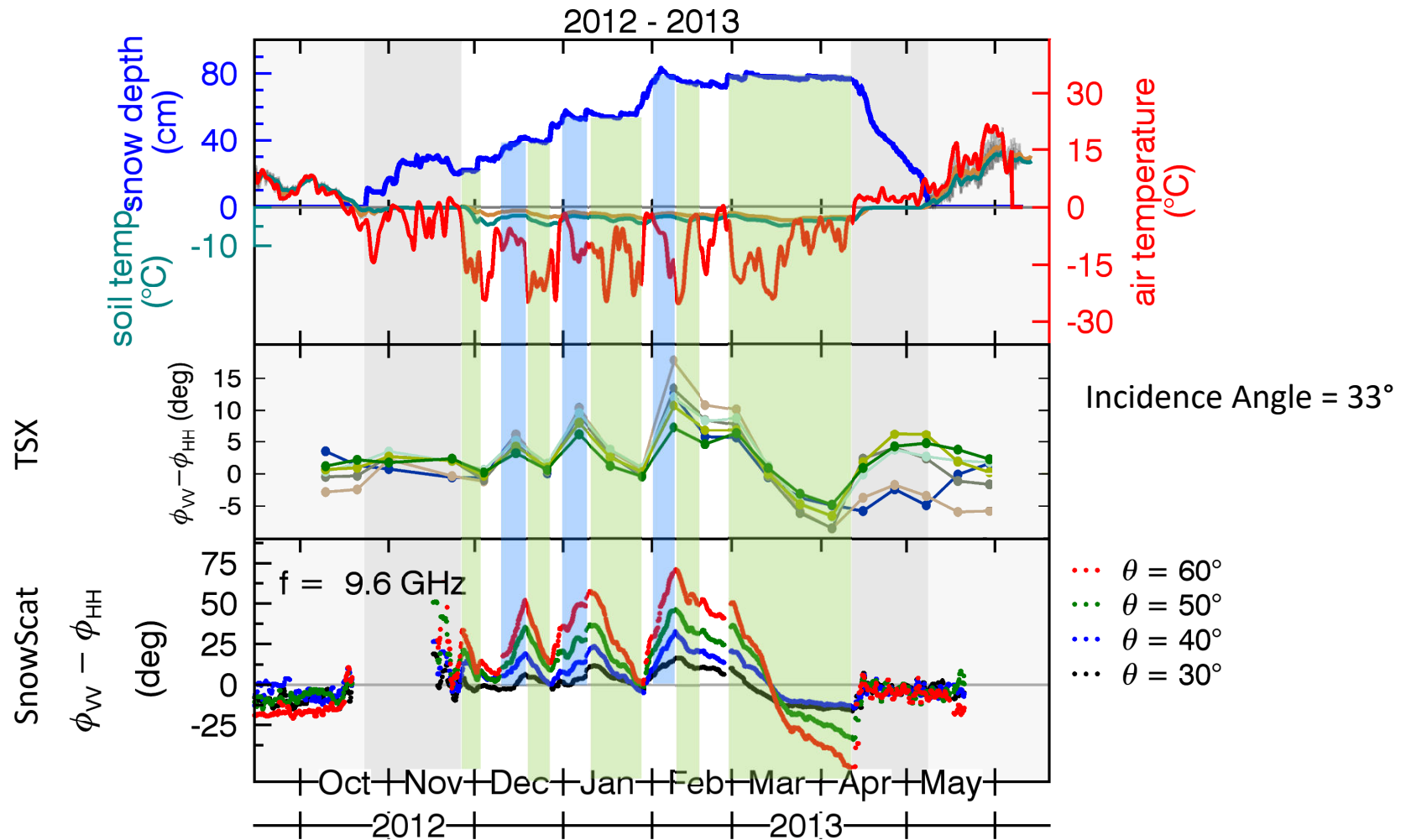
- TerraSAR-X:
Change of snow height
within 11 days
(temporal correlation)



- SnowScat:
Change of snow height
within 13 days.
(temporal correlation)

Leinss et al., «Snow Height Determination by Polarimetric Phase Differences in X-Band SAR Data» JSTARS vol. 7, no.7 (2014)

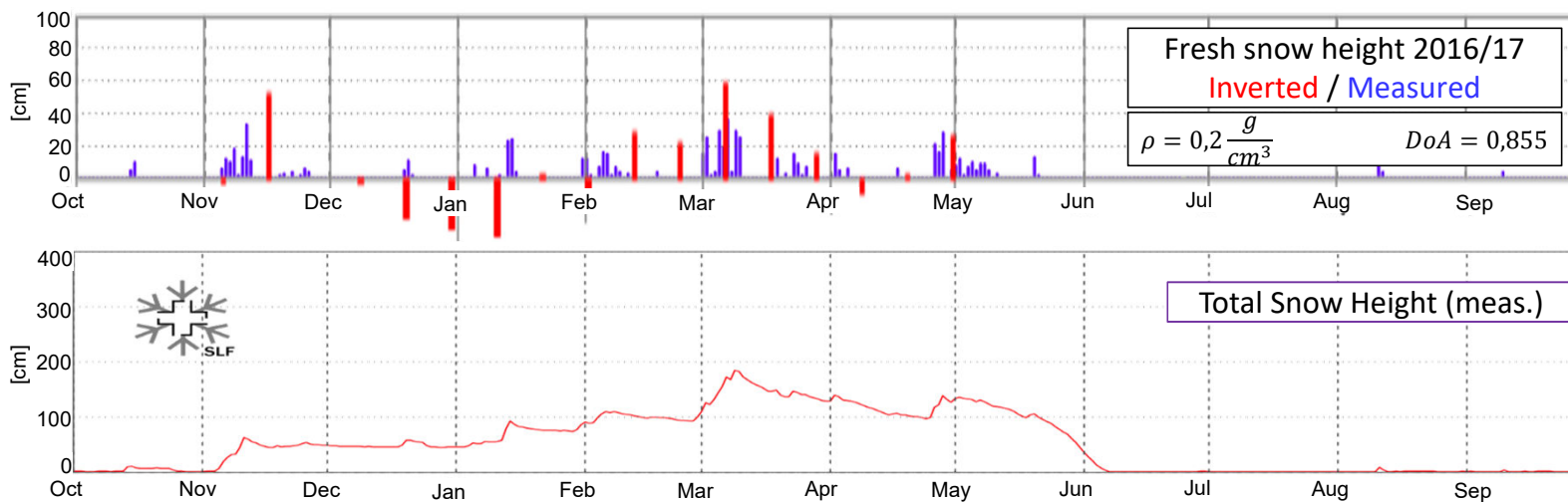
Time series: TSX and SnowScat



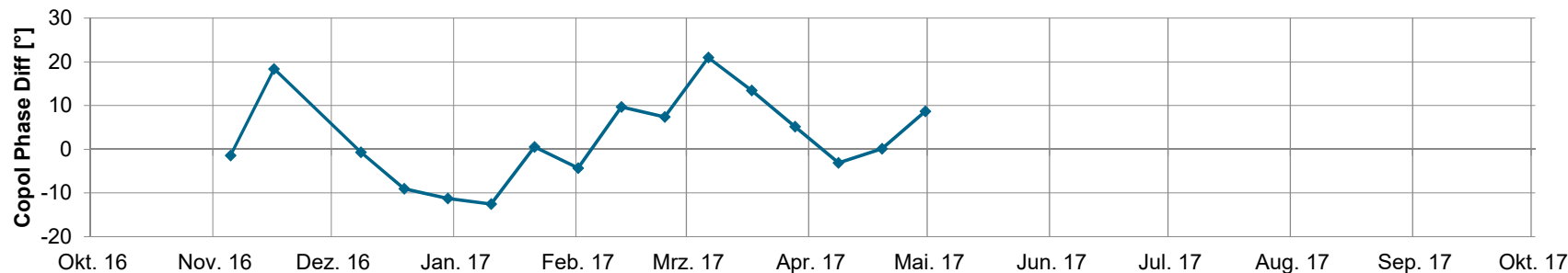
SnowScat shows same result, but with > 50x better temporal resolution

Available Ground Measurements

- ✓ With ϕ_{VV-HH} and Propagation Model the aim is to monitor snow accumulation of the Aletsch Glacier
- ✓ Ground measurements provided by the Institute for Snow and Avalanche Research (SLF)
- ✓ Automatic station at 2500 m provides:
 - ✓ Fresh snow height
 - ✓ Total snow height (daily)
 - ✓ Wind speed and direction
 - ✓ Air and snow surface temperature

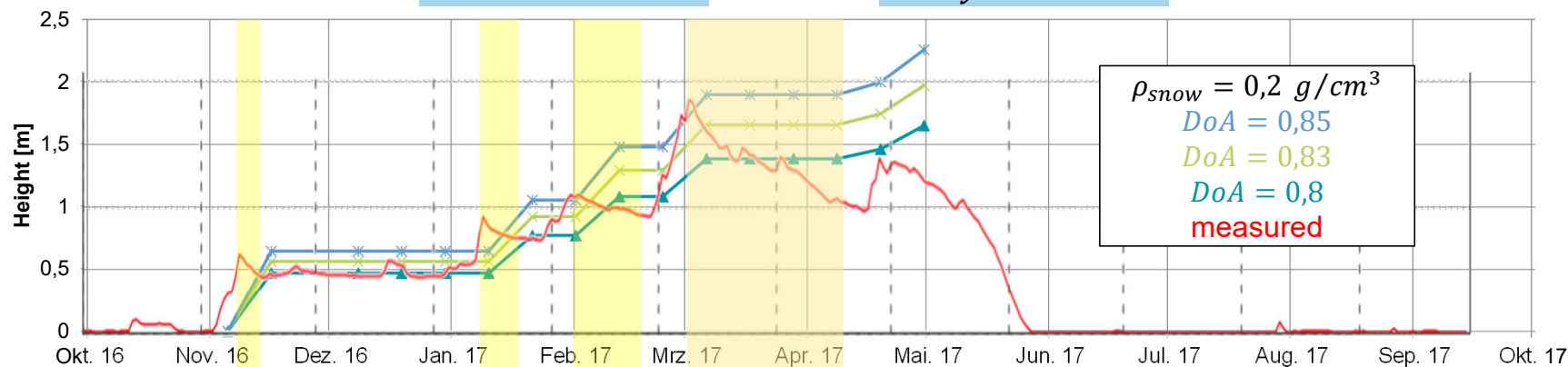


Inversion of Total Snow Height (2016-17)

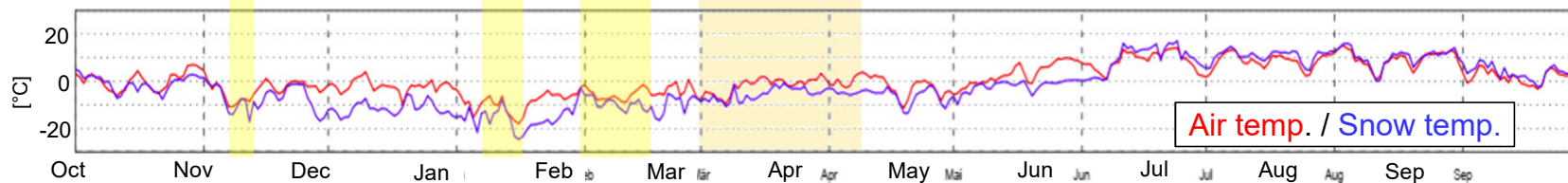


$\phi_{VV-HH} \uparrow$
 \Rightarrow fresh snow,
 l increases

$\phi_{VV-HH} \downarrow$
 \Rightarrow snow ages,
 l stays the same

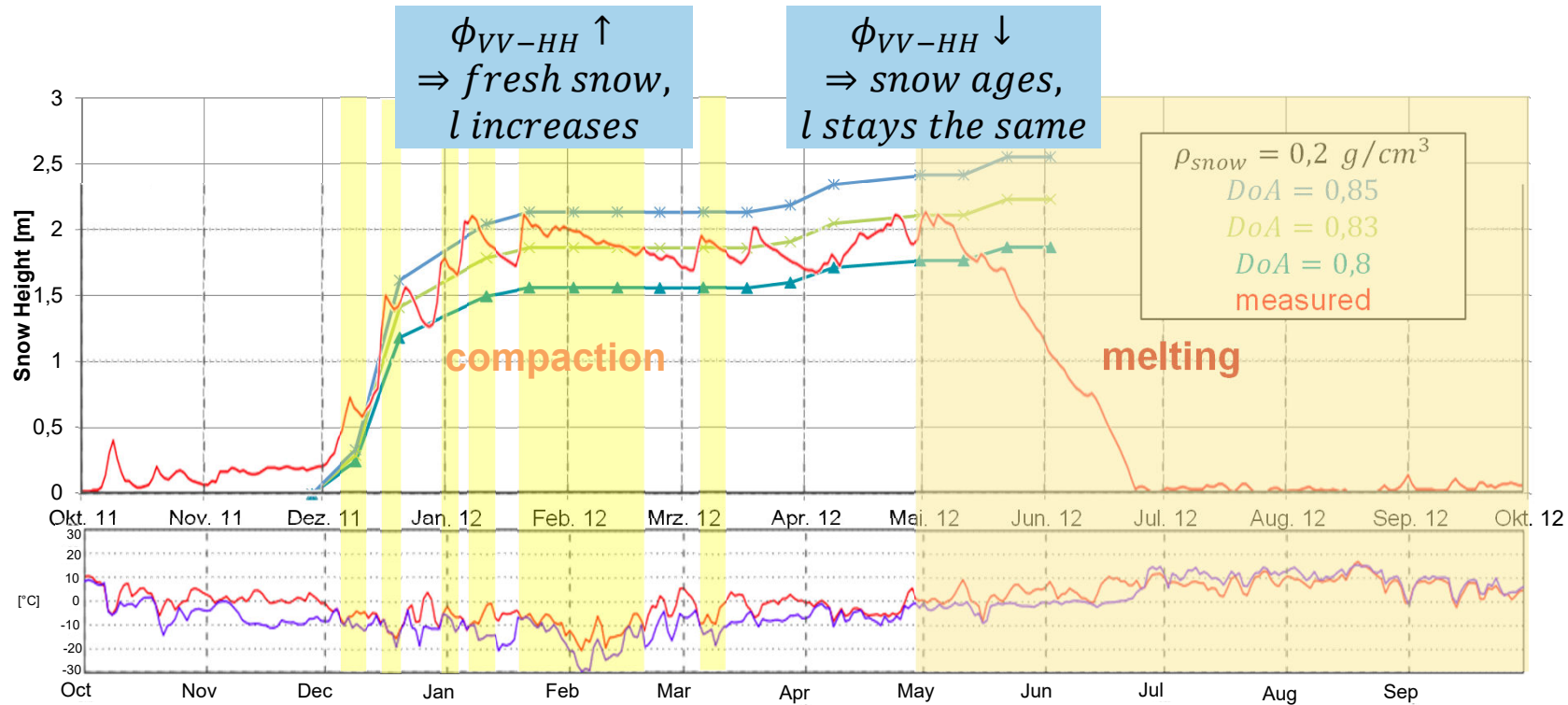
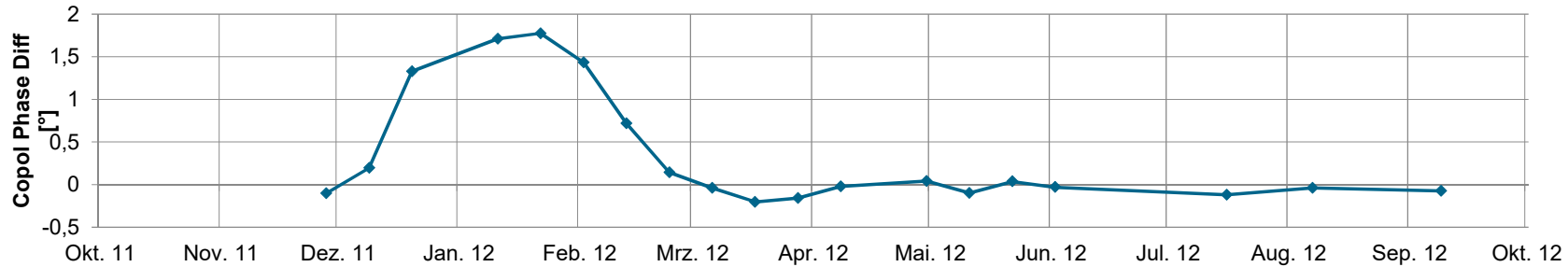


$\rho_{snow} = 0,2 \text{ g/cm}^3$
 $DoA = 0,85$
 $DoA = 0,83$
 $DoA = 0,8$
 measured



Air temp. / Snow temp.

Tentative Total Snow Height Estimation (2011-12)



Limitations of Snow Height Estimation Approach

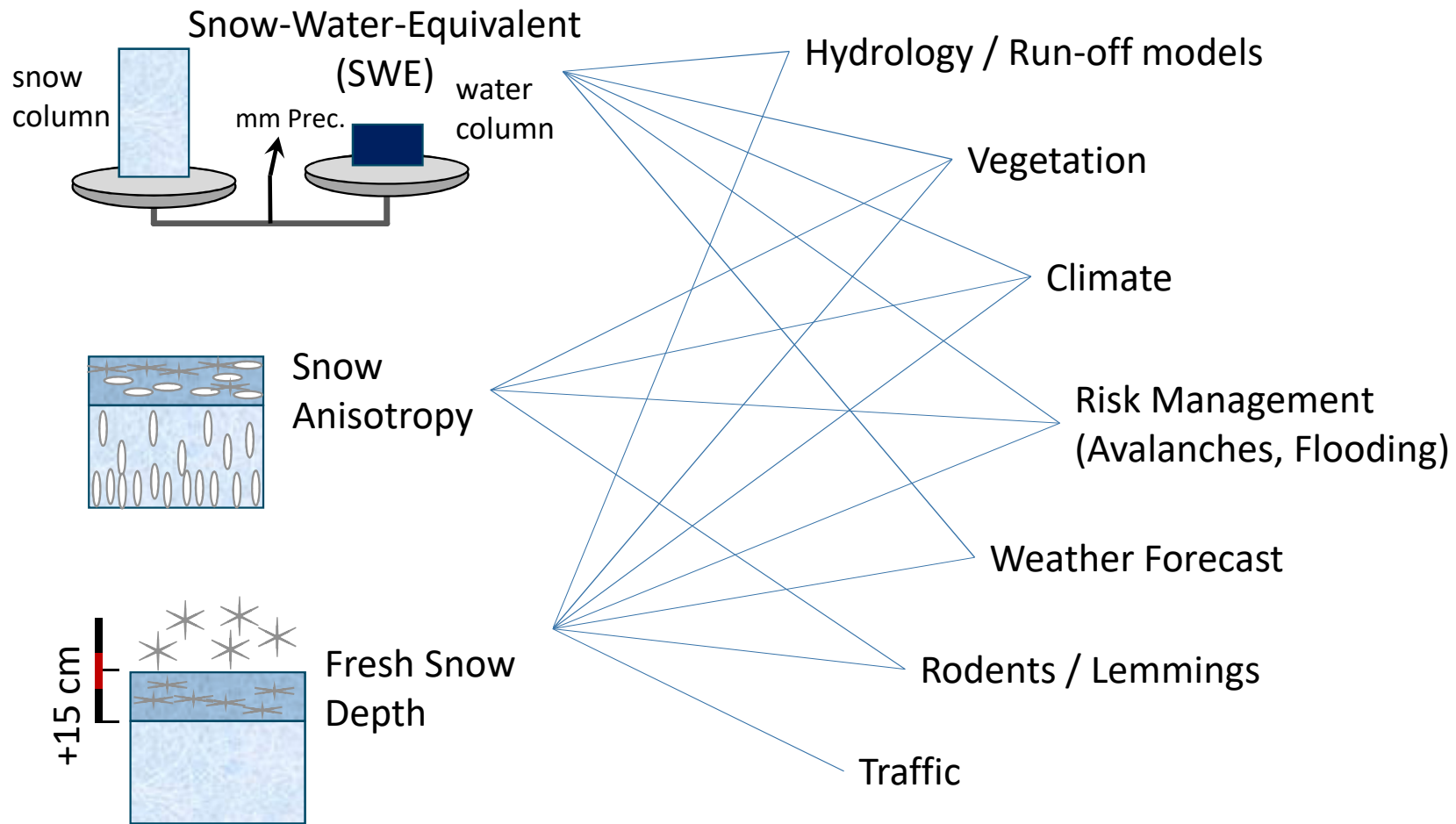
Snow Melting if $T > 0^{\circ}\text{C}$

- ✓ Snow melting dependent on several parameters
 - ✓ **Temperature**
 - ✓ **Snowpack density**
 - ✓ **Rain**
 - ✓ **Mass of the snowpack**

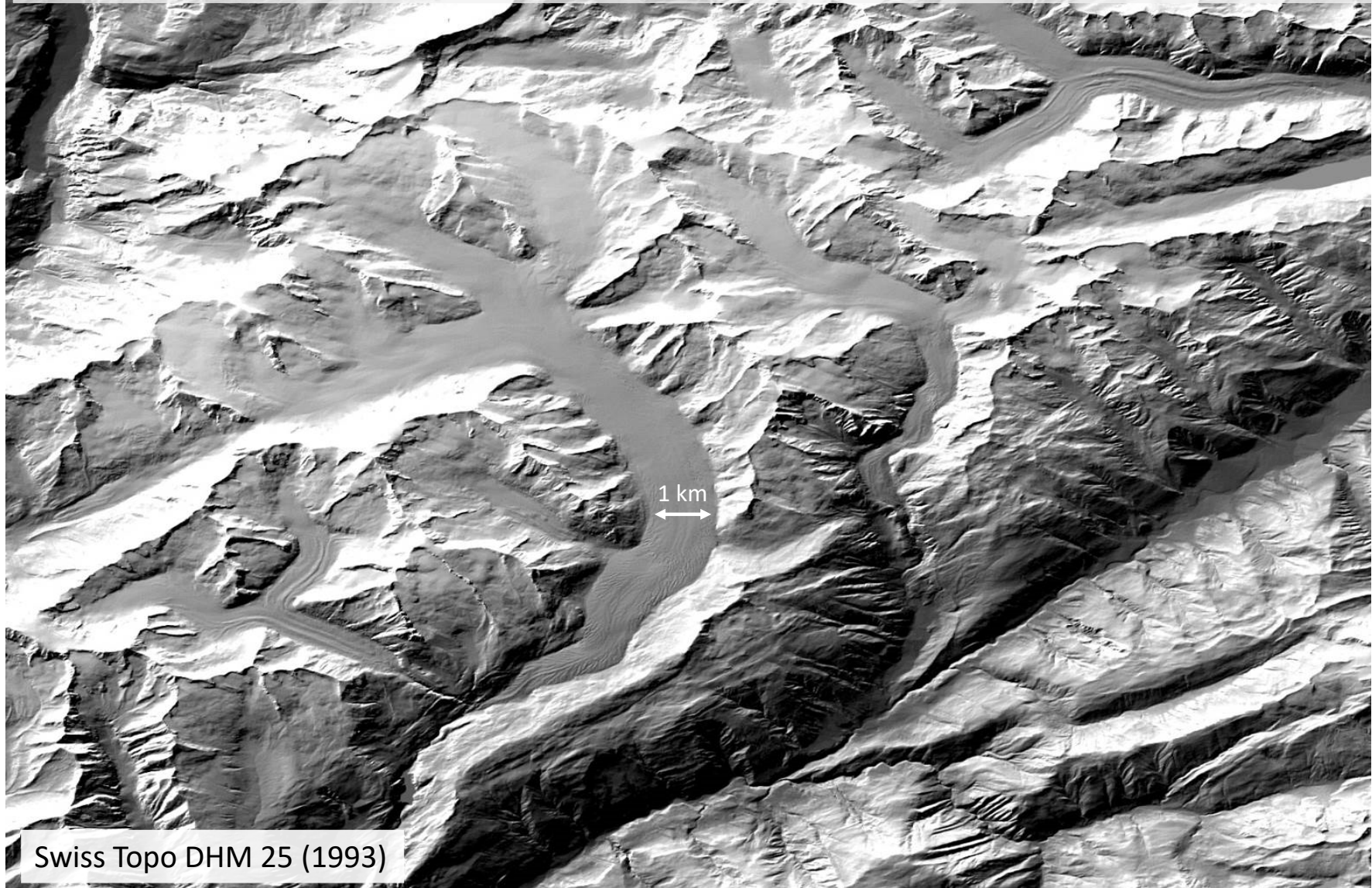
Snow Compaction over Time

- ✓ Snow drift (wind changes density)
- ✓ Snow metamorphism (grains change shape and orientation)
- ✓ Deformation strain (snow compression by its own weight)

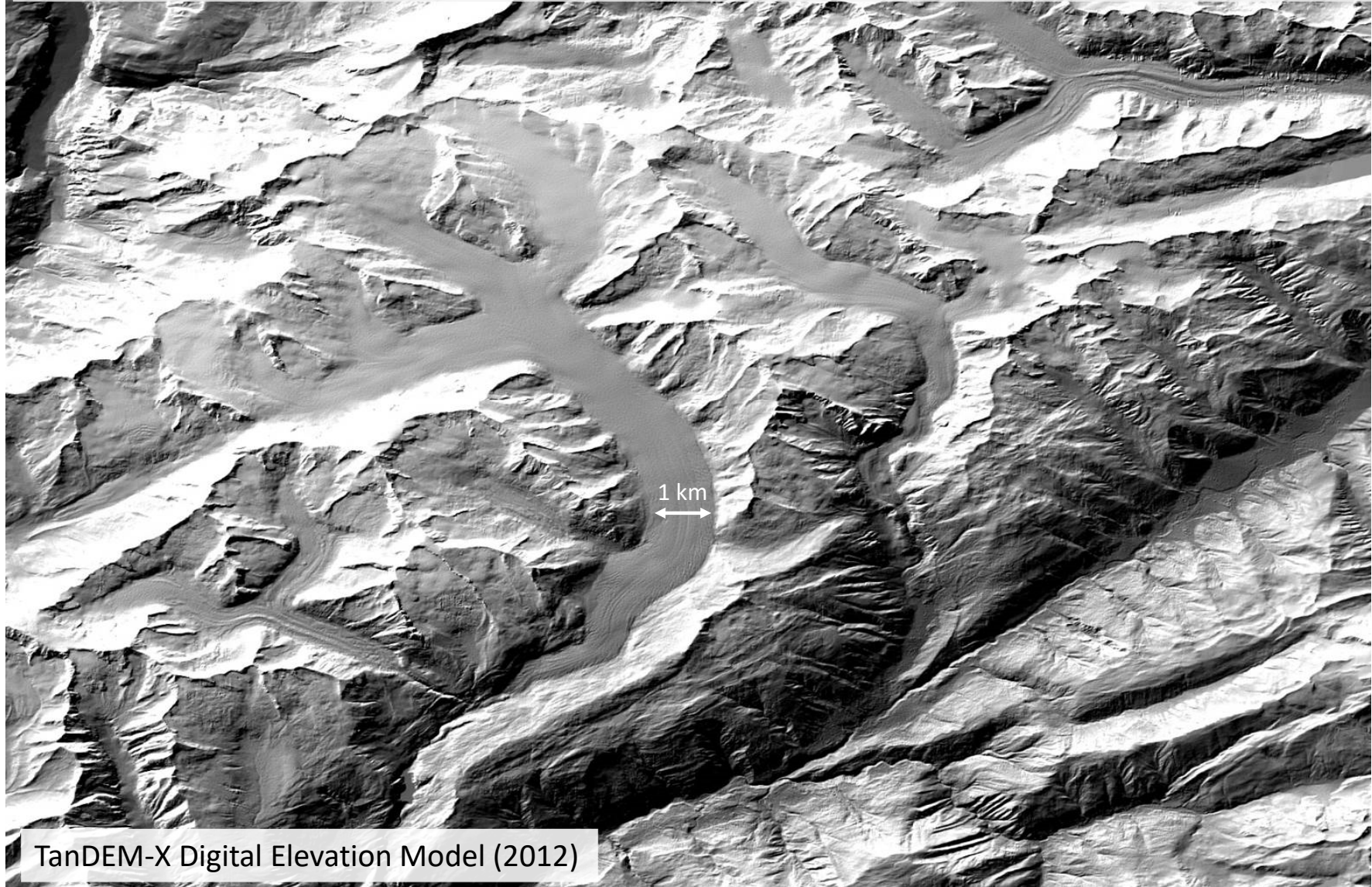
Why are snow parameters important?



Great Aletsch Glacier: Mass loss estimated with a DEM



Great Aletsch Glacier: Mass loss estimated with a DEM



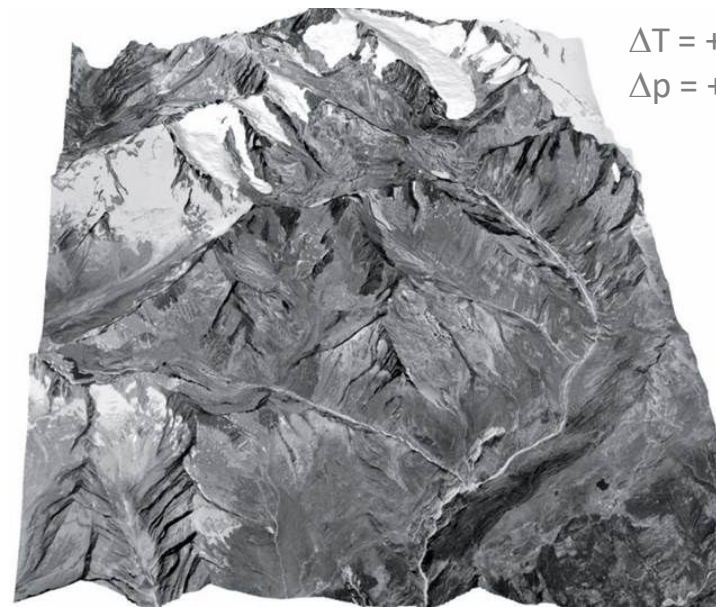
Modeled glacier evolution until 2100



$\Delta T = +4.4^\circ$,
 $\Delta p = +1\%$



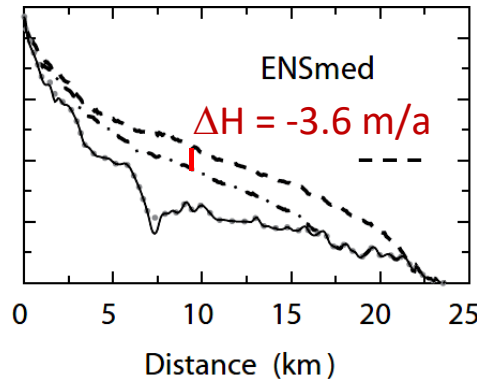
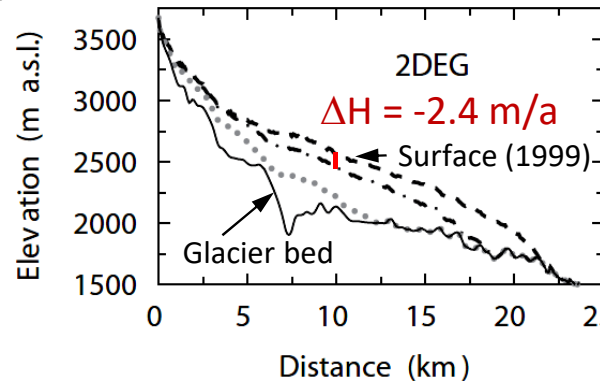
initial state (1999)



Forced 2DEG (2100)

Jouvet et al. J. Glac. (2011)

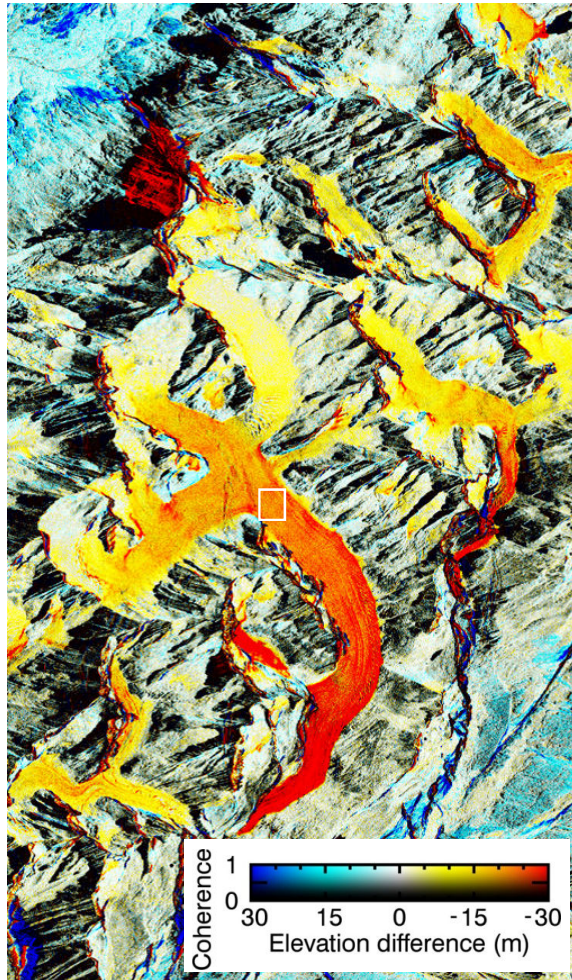
- 3D glacier dynamic model.
- Calibrated with climate data and field observations from 1880 - 1999.
- Forced by different climate scenarios.



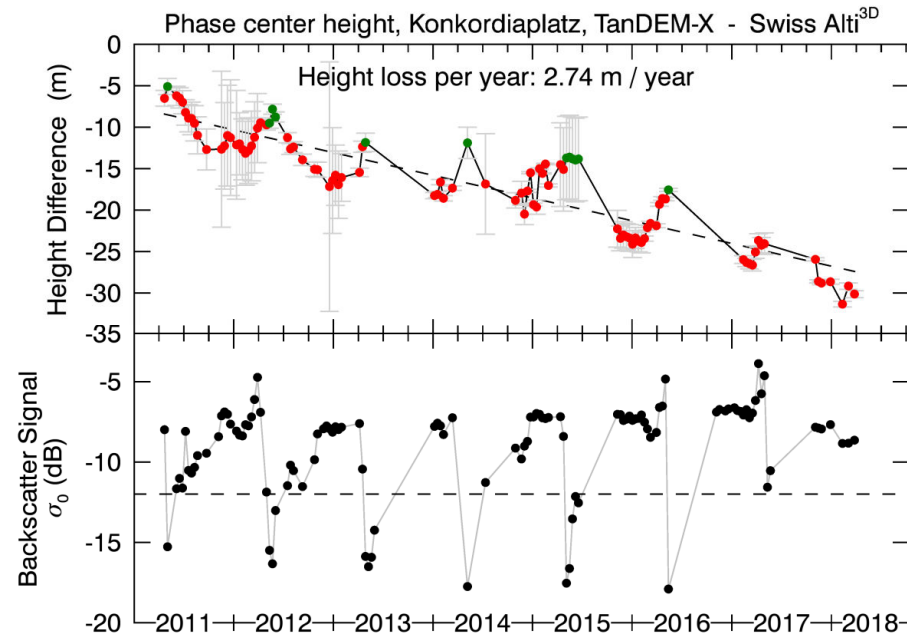
Surface elevation: 1999, --- 2050,2100

Height loss of Aletschgletscher 2011 - 2018

TanDEM-X vs. SwissAlti3D (2009)



08.11.2015



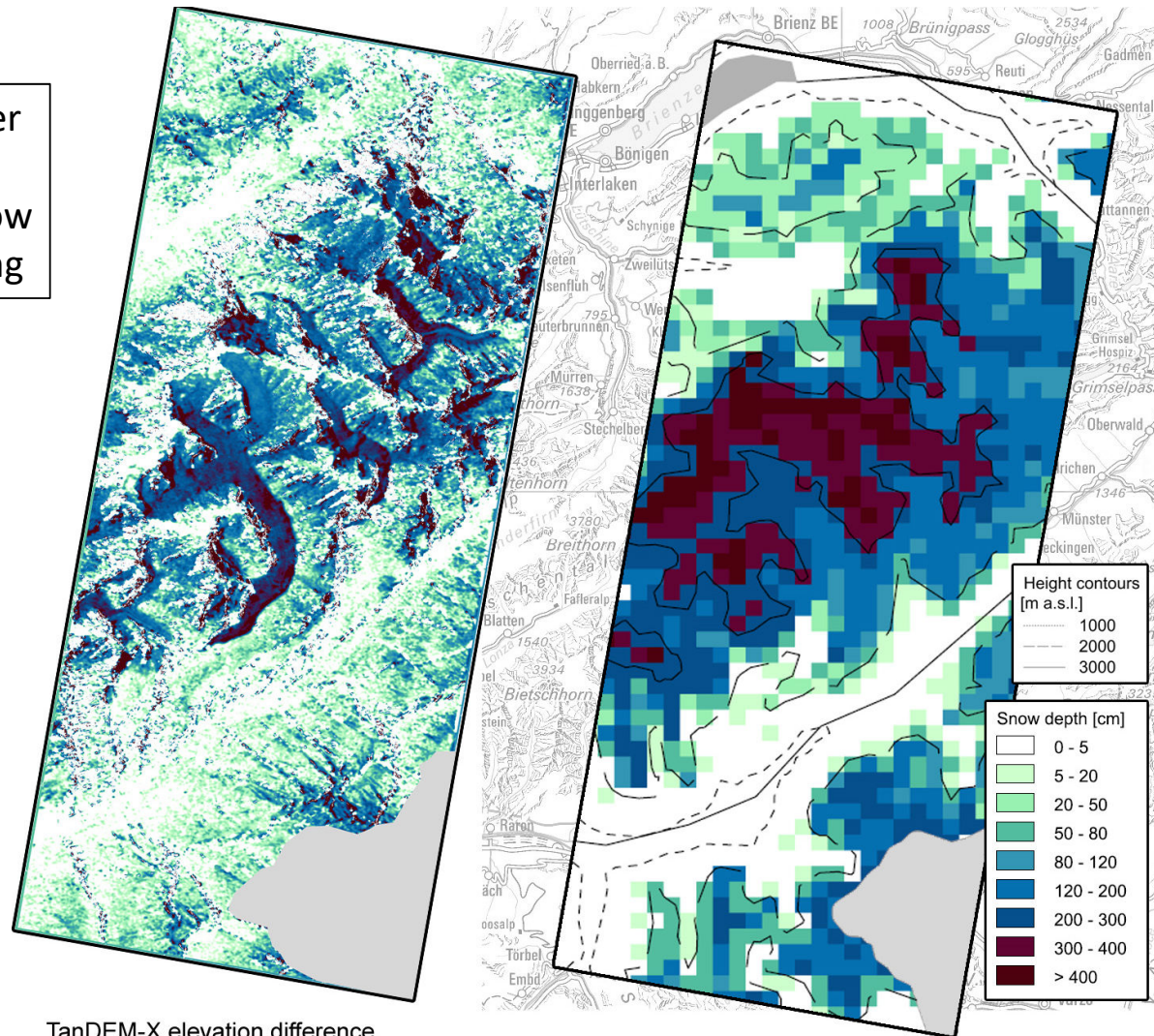
- Agreement with results of climate scenarios:
DEG2: -2.1 m / year (political aim)
ENSmed: -3.6 m / year (business as usual)
- Periodic seasonal changes
- Height increase at the onset of snow melt (wet snow detected by low backscatter)

L. Leinss

Snow Depth determined by DEM Differencing



summer
vs.
wet snow
in spring

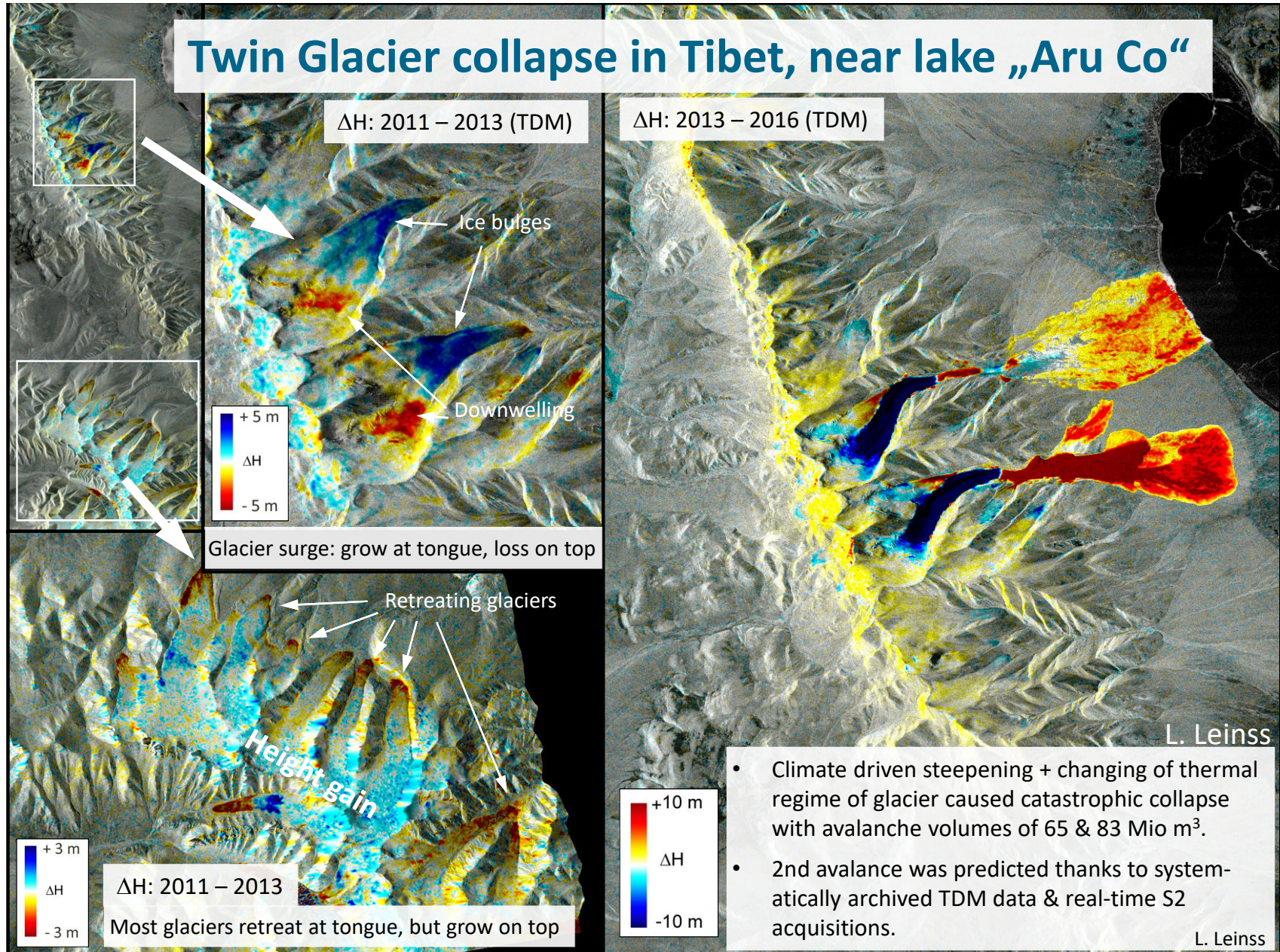


TanDEM-X elevation difference,
02.06.2012 vs. 27.07.2012

SLF, snow depth map, 31.05.2012

L. Leinss

Twin Glacier collapse in Tibet, near lake „Aru Co“



L. Leinss

- Climate driven steepening + changing of thermal regime of glacier caused catastrophic collapse with avalanche volumes of 65 & 83 Mio m³.
- 2nd avalanche was predicted thanks to systematically archived TDM data & real-time S2 acquisitions.

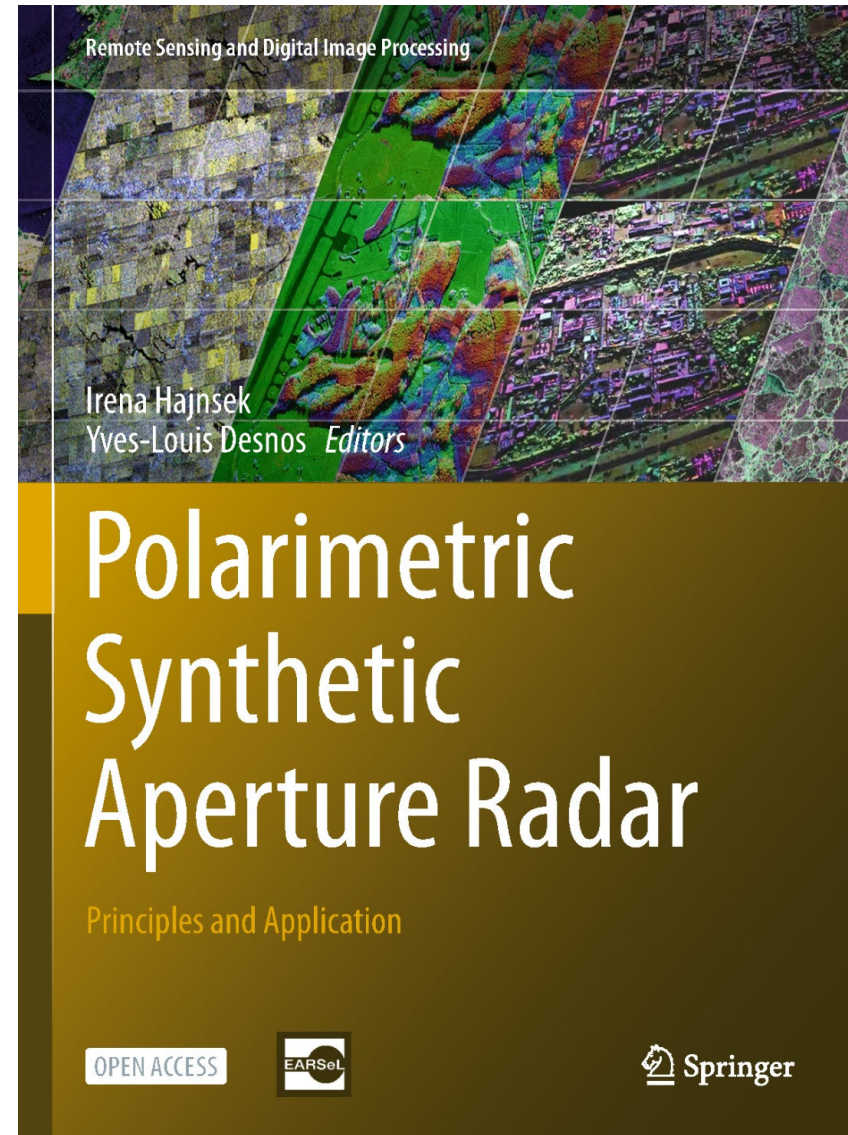
L. Leinss

Polarimetric Applications

<https://link.springer.com/book/10.1007%2F978-3-030-56504-6>

Open Access Book

- Basic Principles of SAR Polarimetry
- Forest Applications
- Agriculture Wetland Applications
- Cryosphere Applications
- Urban Applications
- Ocean Applications



I am happy to answer your
question?