

# Introduction to SAR Polarimetry (Lecture D2T2)

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SAR & Hyperspectral multi-modal Imaging  
and sigNal processing,  
Electromagnetic modeling



# Rennes - Brittany



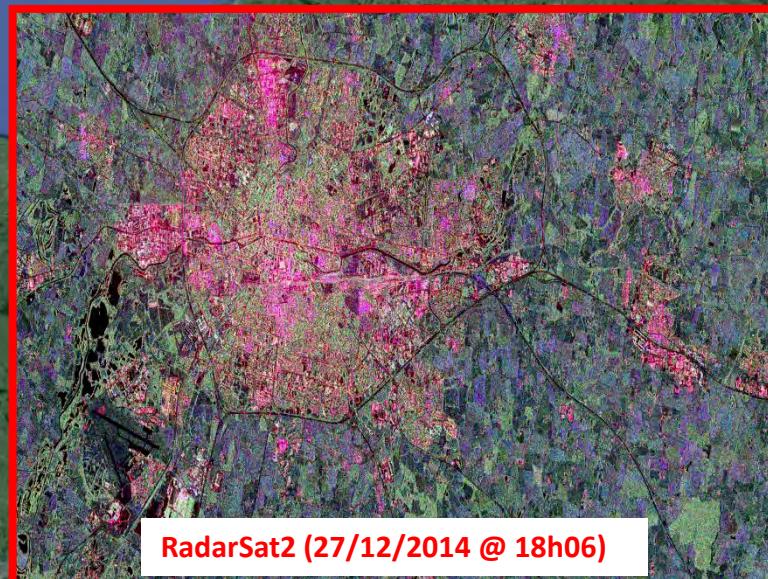
→ 7th ADVANCED TRAINING COURSE ON LAND REMOTE SENSING

4–9 September 2017 | Szent István University | Gödöllő, Hungary

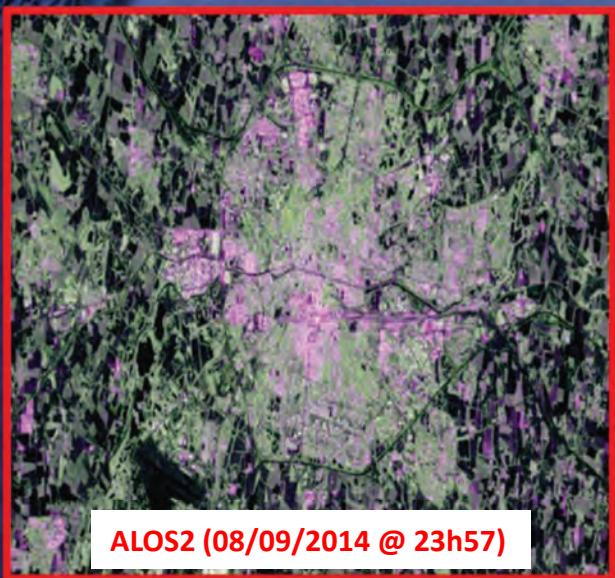
# Rennes - Brittany



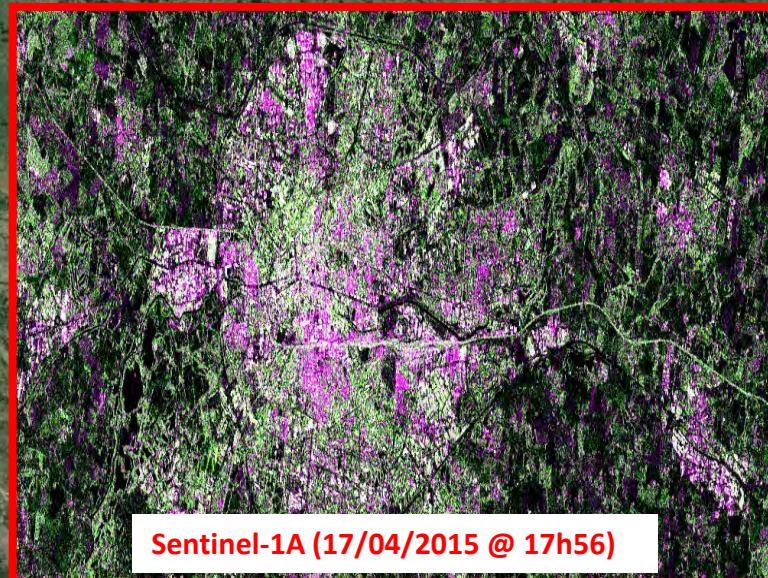
ALOS1 (30/04/2008 @ 22h34)



RadarSat2 (27/12/2014 @ 18h06)



ALOS2 (08/09/2014 @ 23h57)



Sentinel-1A (17/04/2015 @ 17h56)



## Objective

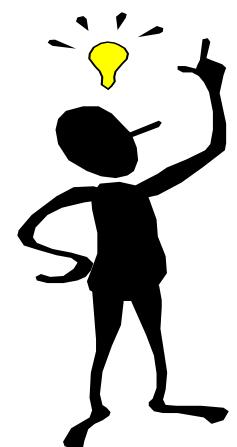
To provide

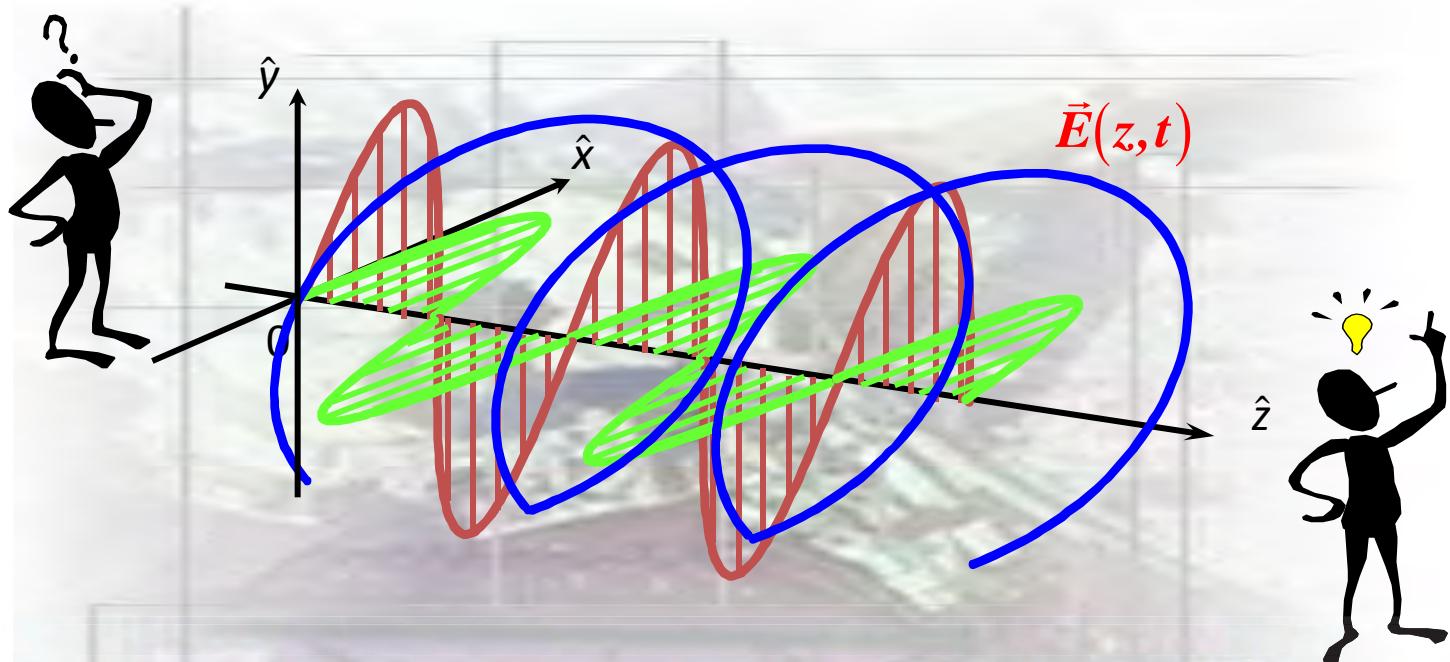
**the minimum, but necessary,  
amount of knowledge required**

**to understand**

**scientific works on**

**SAR Polarimetry (PolSAR)**





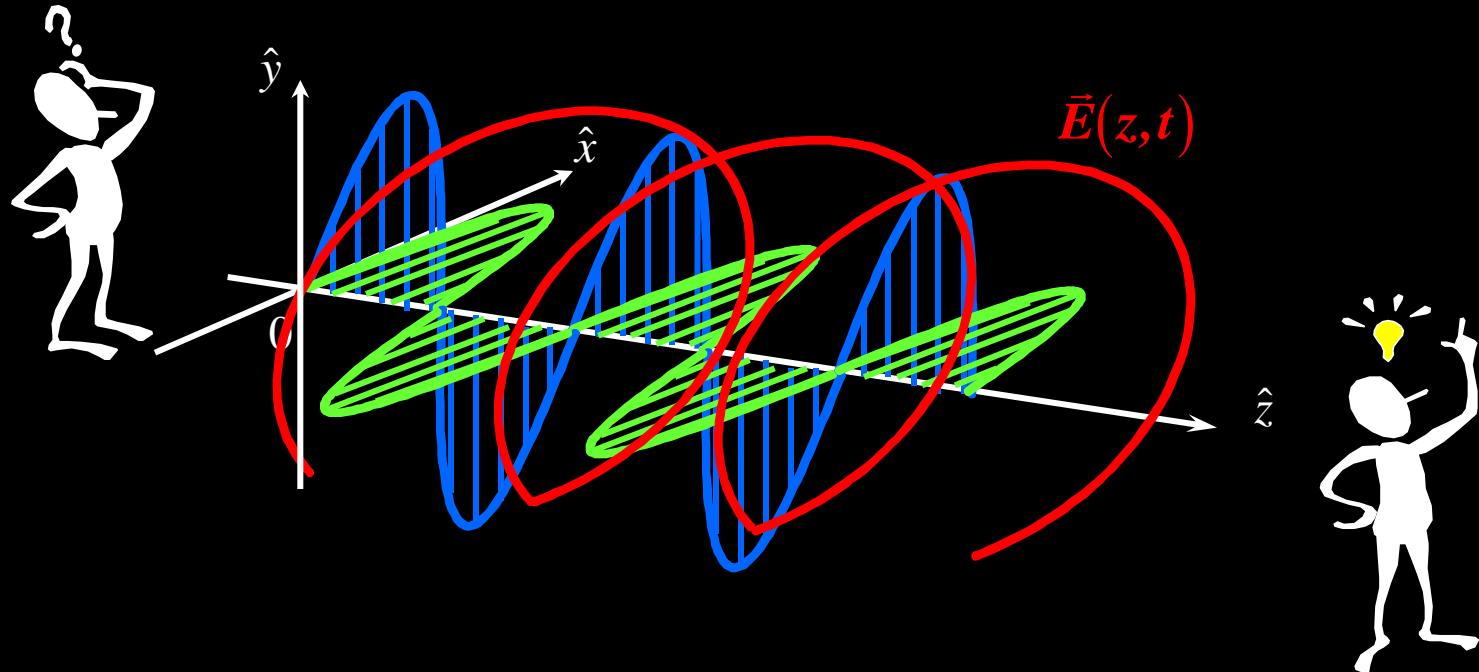
# GENERAL INTRODUCTION

# RADAR POLARIMETRY



- A bit of History
- Airborne and Space-borne Polarimetric SAR Sensors
- Software / Toolbox
- Learning / Training / Results

# Radar Polarimetry



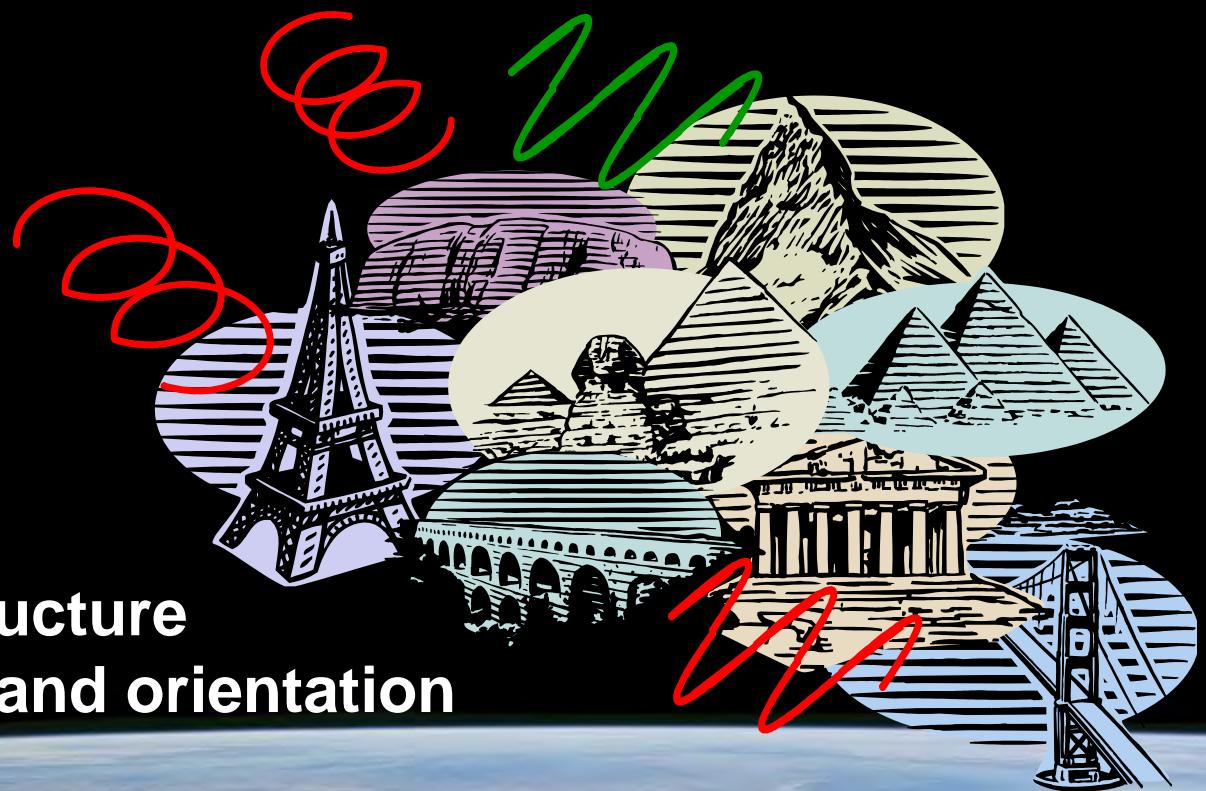
Radar Polarimetry (**Polar** : polarisation **Metry**: measure)  
is the science of acquiring, processing and analysing  
the polarization state of an electromagnetic field

Radar Polarimetry deals with the full vector  
nature of polarized electromagnetic waves

# Radar Polarimetry



The POLARISATION information  
Contained in the waves backscattered  
from a given medium is highly related to:



its geometrical structure  
reflectivity, shape and orientation

its geophysical properties such as humidity, roughness, ...

# SAR Polarimetry Applications



Forest Vegetation

- Forest Height
- Forest Biomass
- Forest Structure
- Canopy Extinction
- Underlying Topography

- Forest Ecology
- Forest Management
- Ecosystem Change
- Carbon Cycle



Agriculture

- Soil Moisture Content
- Soil roughness
- Height of Vegetation Layer
- Extinction of Vegetation Layer
- Moisture of Vegetation Layer

- Farming Management
- Water Cycle
- Desretification



Snow and Ice

- Topography
- Penetration Depth / Density
- Snow Ice Layer
- Snow Ice Extinction
- Water Equivalent

- Ecosystem Change
- Water Cycle
- Water Management



Urban Areas

- Geometric Properties
- Dielectric Properties

- Urban Monitoring



Courtesy of Dr. I. Hajnsek

## A Bit Of History



## Radar Polarimetry

# Discovery of the Phenomena of Polarized Electromagnetic Energy

AD 1000

Use of the polarized skylight to locate a hidden sun



Crystal of calcite  
Iceland Spar  
Sunstone



Bartholinus



1669  
First known  
Quantitative work  
on light observation



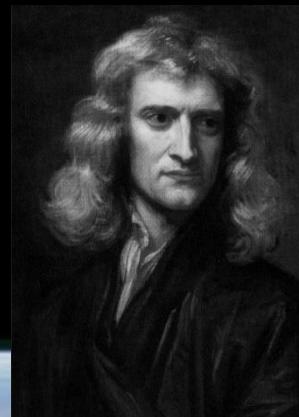
Huygens

Discovery of the double  
refraction in calcite

1677  
Wave nature  
of light discovery  
Explanation of the  
double refraction

Corpuscular model or  
« longitudinal » waves

1704  
Corpuscular  
Model of light



Newton

1808

Discovery of the polarization of light  
(intrinsic property of light and not of crystals)



Malus  
X-1795

# Non Exhaustive Chronological List of the Main Pionners who contributed to the discovery of Polarization leading to Radar Polarimetry

Brewster



1816

Fresnel



1820

Faraday



1832

Stokes



1852

Maxwell



1873

Helmholtz



1881

Rayleigh



1881

Kirchhoff



1883

« Transverse » nature  
of light waves

Electromagnetic  
theory of light



# Non Exhaustive Chronological List of the Main Pionners who contributed to the discovery of Polarization leading to Radar Polarimetry

Brewster



1816

Hertz



1886

Fresnel



1820

Faraday



1832

Stokes



1852

Maxwell



1873

Helmholtz



1881

Rayleigh



1881

Kirchhoff



1883

Drude



1889

Sommerfeld



1896

Poincaré



1892

Lie



1897

Lorentz



1908

Marconi

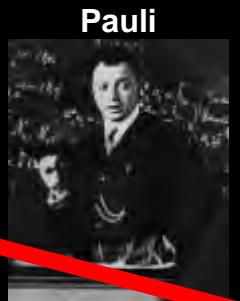


1922

Wiener



# Non Exhaustive Chronological List of the Main Pionners who contributed to the discovery of Polarization leading to Radar Polarimetry



Pauli



Deschamp



Born



Wolf



Kennaugh

1950

1951

1954

1954

1952



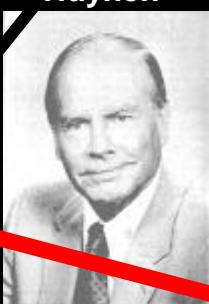
# Non Exhaustive Chronological List of the Main Pionners who contributed to the discovery of Polarization leading to Radar Polarimetry

Kennaugh



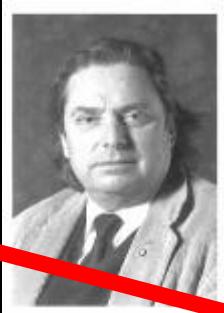
1952

Huynen



1970

W. M. Boerner



1980

The

Radar Polarimetric  
Triptych

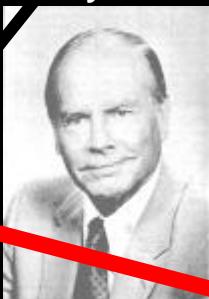
# Non Exhaustive Chronological List of the Main Pionners who contributed to the discovery of Polarization leading to Radar Polarimetry

Kennaugh



1952

Huynen



1970

W. M. Boerner



K. Raney



J.J. Van Zyl



A. Freeman



R. Touzi



J.S. Lee



T. Ainsworth



S.R. Cloude



E. Pottier



P. Dubois



Y. Yamaguchi



C. Lopez

1980



H. Mott



E. Lueneburg



E. Krogager



A. Moreira



Y.L. Desnos



Z. Czyz



K. Papathanassiou



I. Hajnsek



T. Le Toan



L. Ferro-Famil #E. Pottier (06/2017)



J.C. Souyris

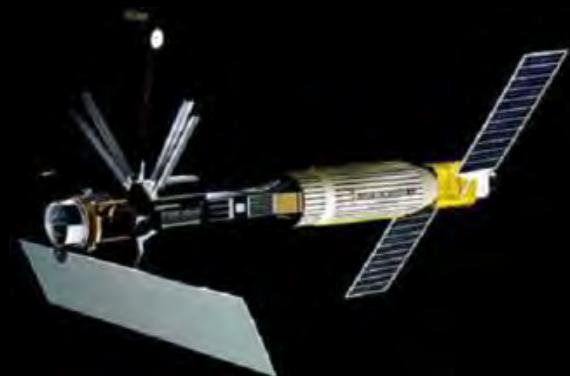
**1990 - 2000**  
**Radar Polarimetry**  
**Scientific Progress**

# Polarimetric Radar (SAR)

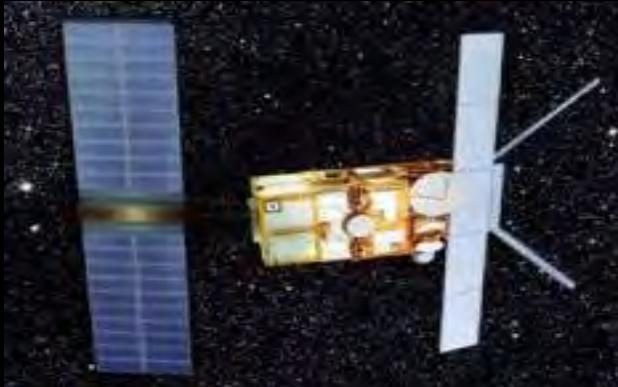


## Spaceborne Sensors

# Space-borne Sensors



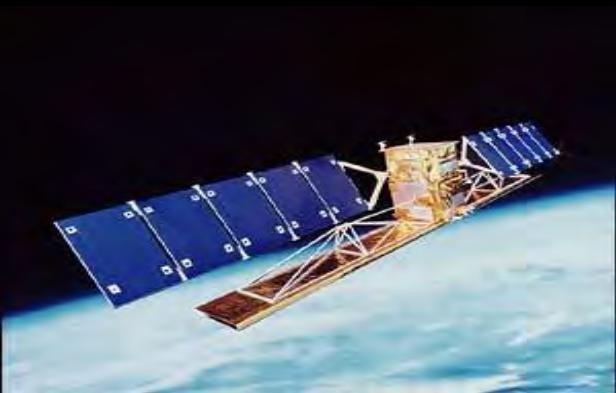
**SEASAT**  
NASA/JPL (USA)  
L-Band, 1978



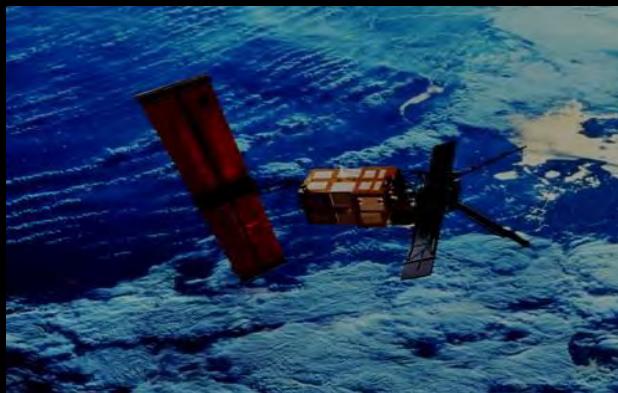
**ERS-1**  
European Space Agency (ESA)  
C-Band, 1991-2000



**J-ERS-1**  
Japanese Space Agency (NASDA)  
L-Band, 1992-1998



**RadarSAT-1**  
Canadian Space Agency (CSA)  
C-Band, 1995

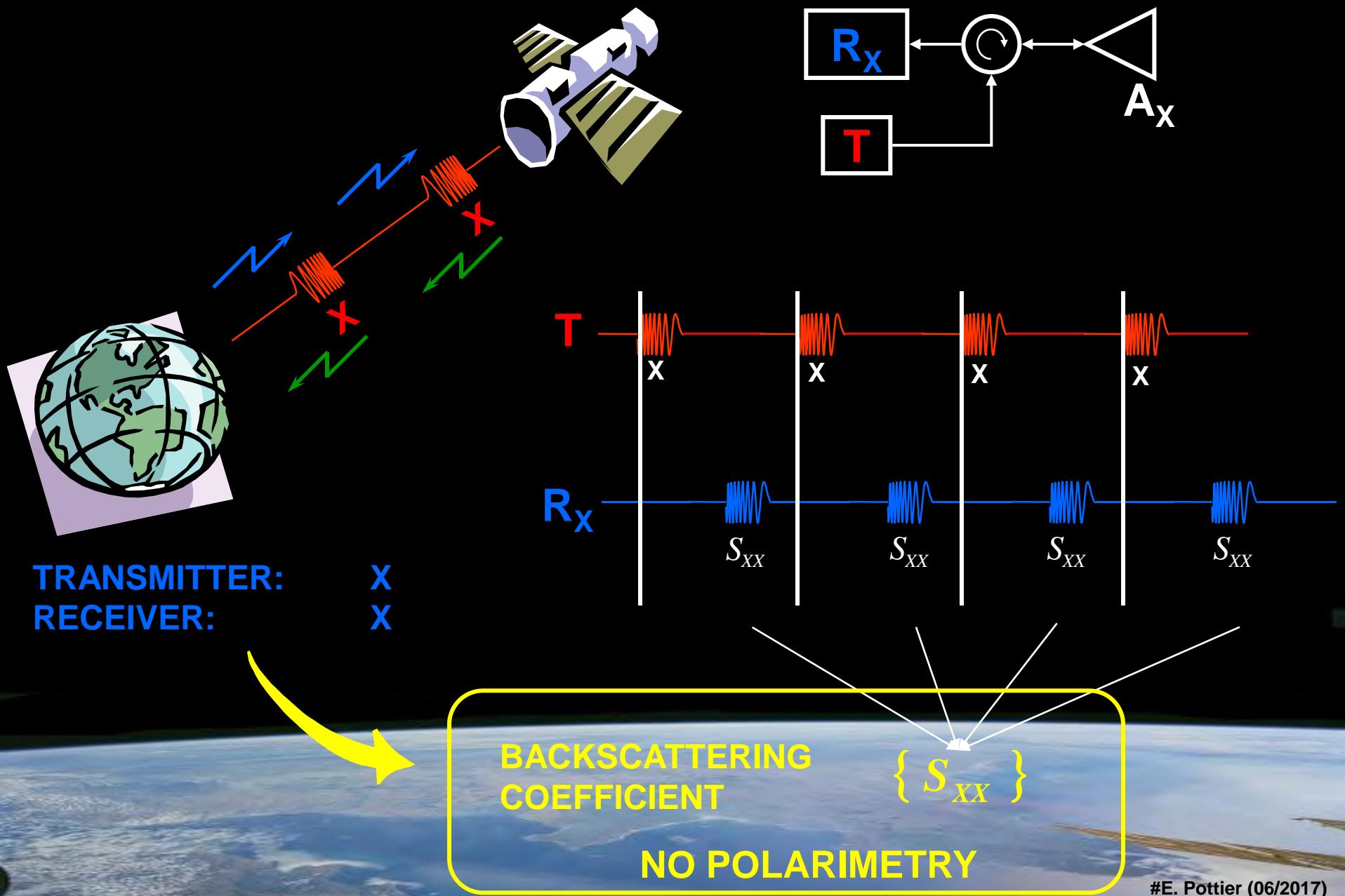


**ERS-2**  
European Space Agency (ESA)  
C-Band, 1995

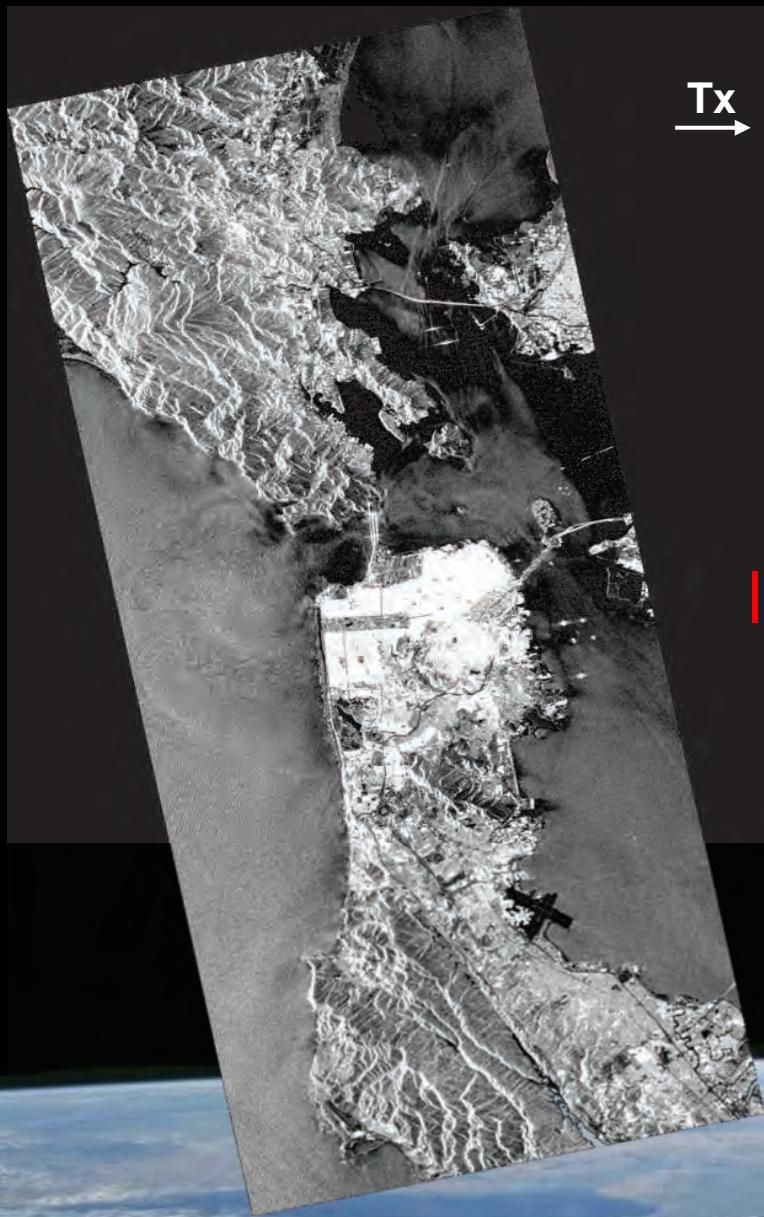


**Shuttle Radar Topography Mission**  
NASA/JPL (C-Band), DLR (X-Band)  
February 2000

# Scattering Coefficient

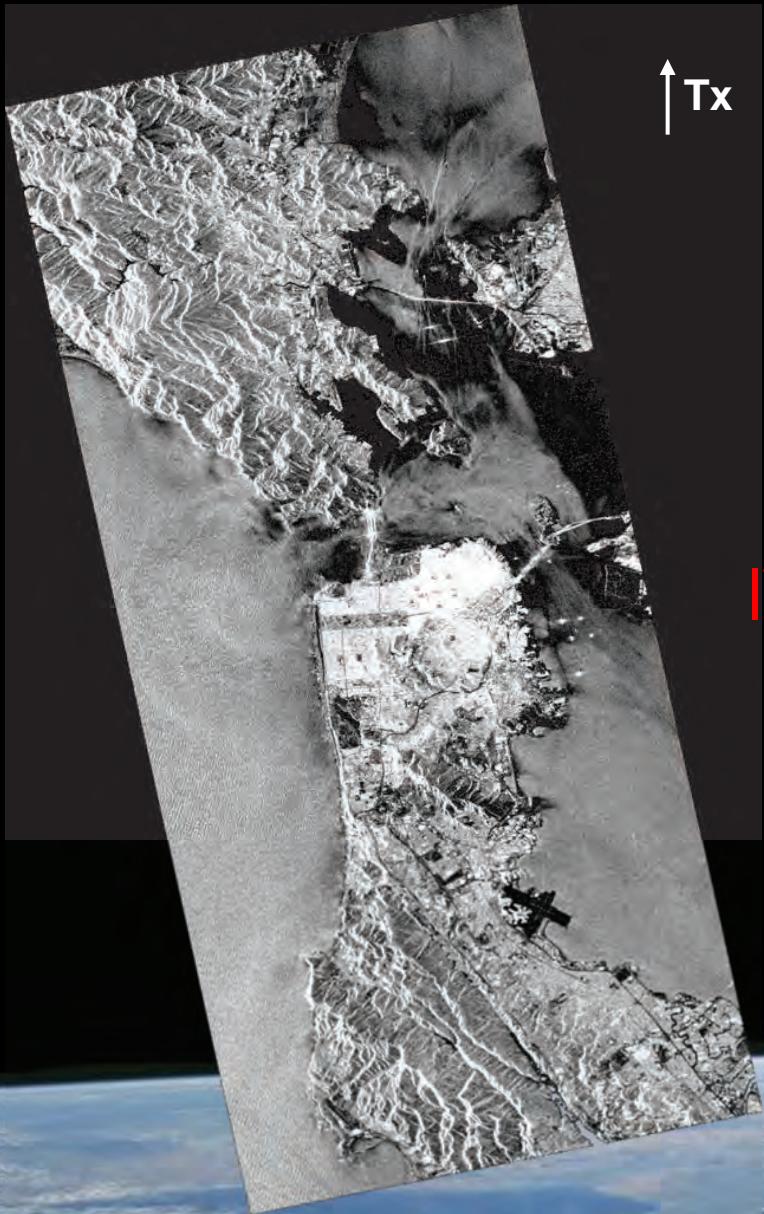


# Space-borne Sensors



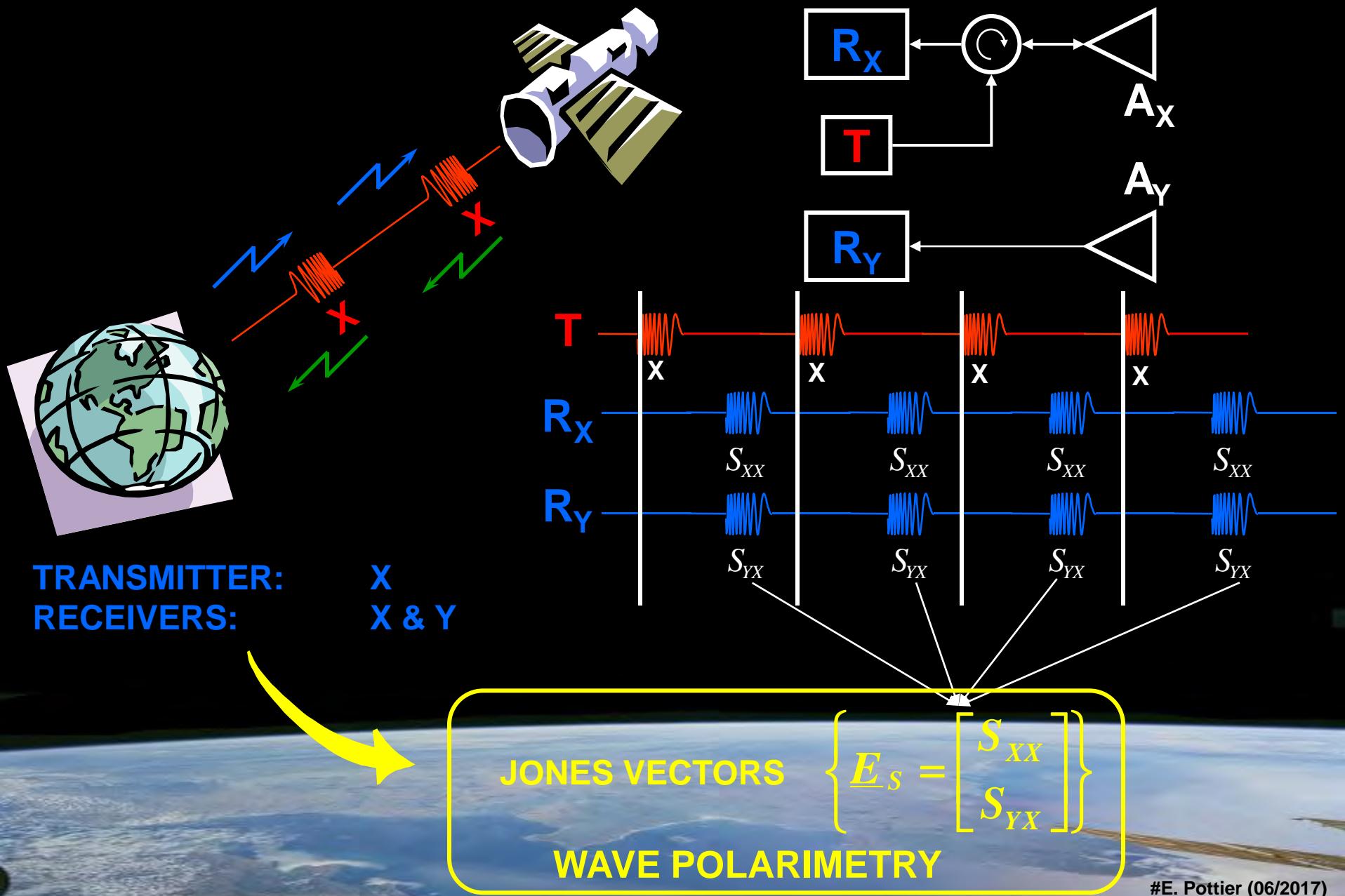
San Francisco Bay – (L-Band)

# Space-borne Sensors

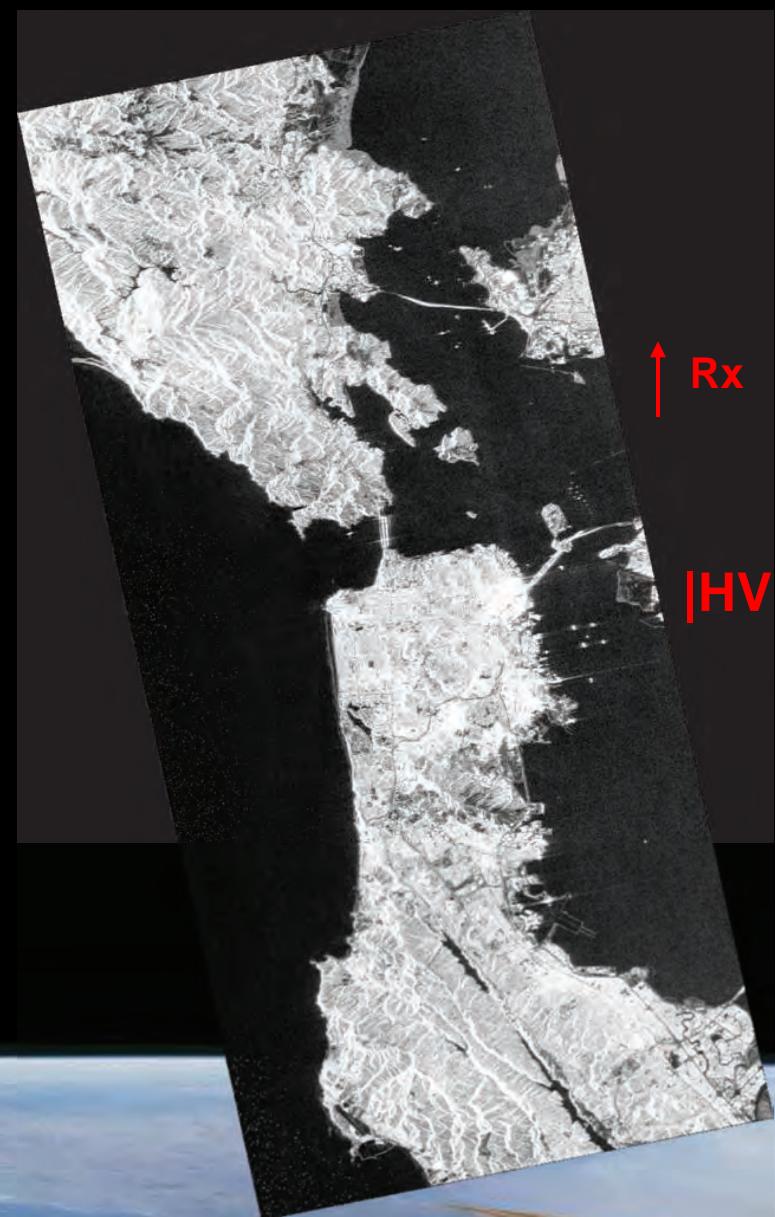
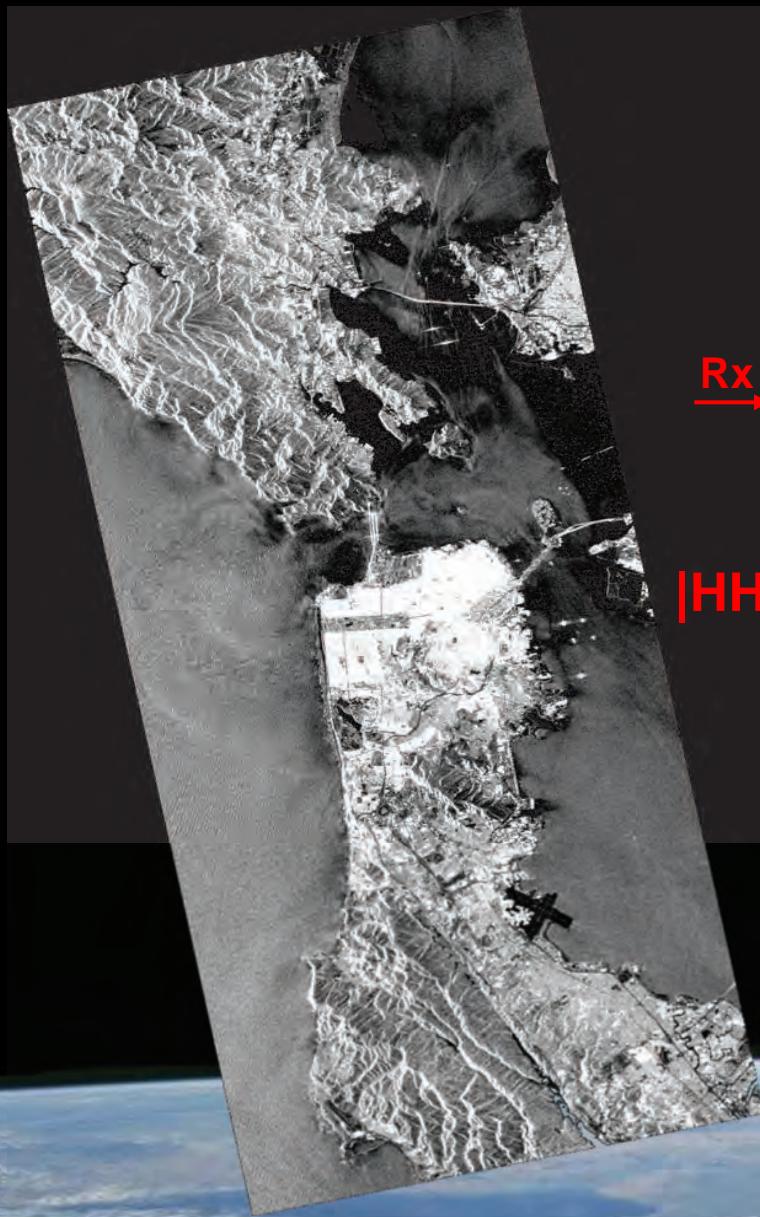


San Francisco Bay – (L-Band)

# Wave Polarimetry



# Space-borne Sensors



San Francisco Bay – (L-Band)

# Space-borne PolSAR Sensors

## ENVISAT - ASAR

October 2001  
C-Band (Sngl / Dual Inc)

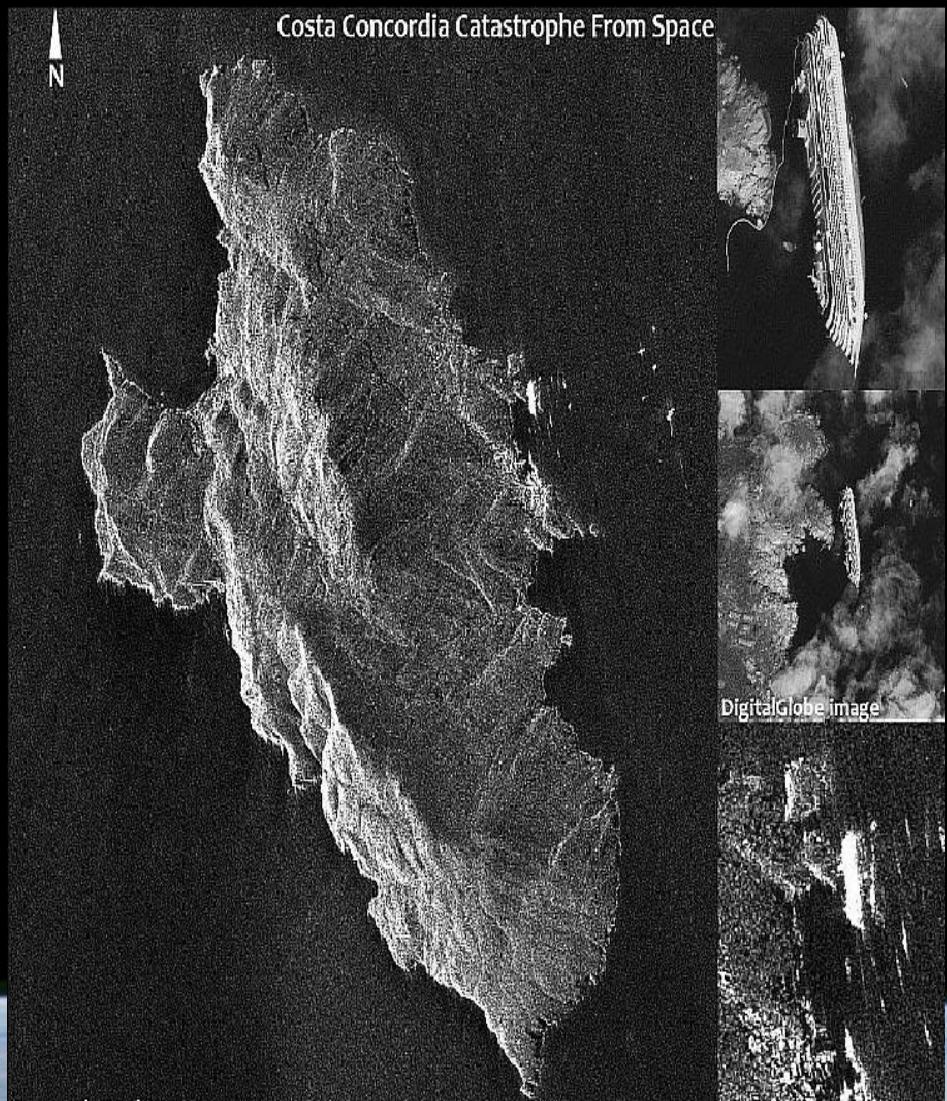


# Space-borne PolSAR Sensors

## COSMO - SkyMed

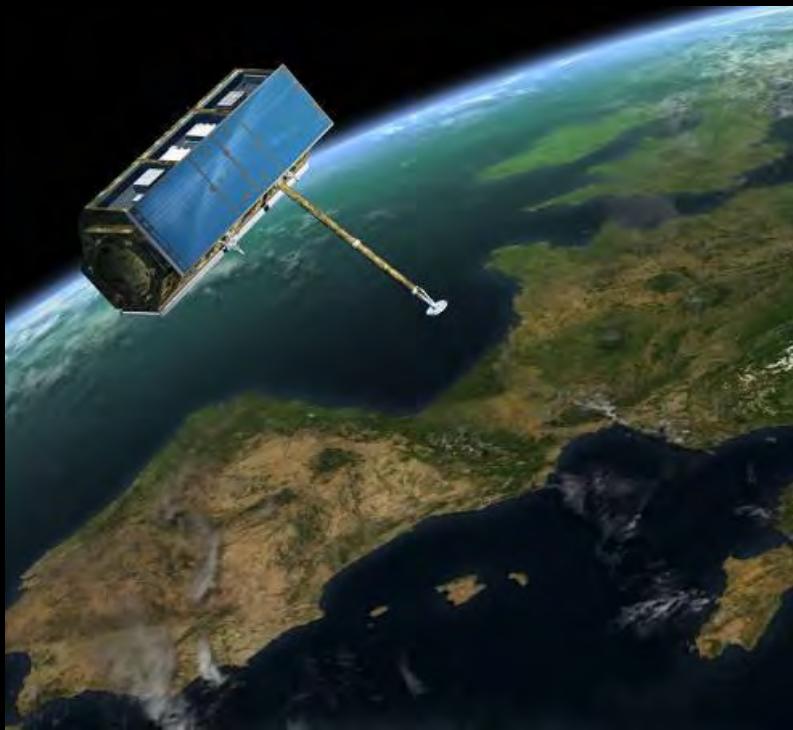


June 2007, Dec. 2007  
Oct. 2008, Nov. 2010  
X-Band (Singl / Dual)  
Revisit : 1 day



# Space-borne PolSAR Sensors

TerraSAR - X



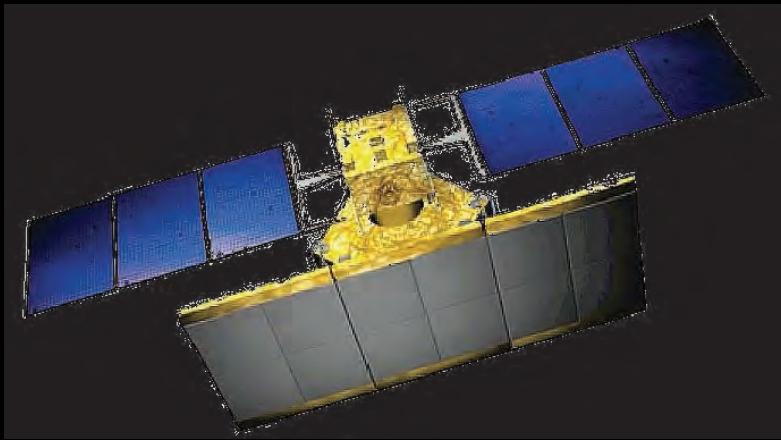
June 2007  
X-Band (Sngl / Twin HH-VV / Quad Exp.)

Rostok (Twin)



# Space-borne PolSAR Sensors

## RISAT-1A

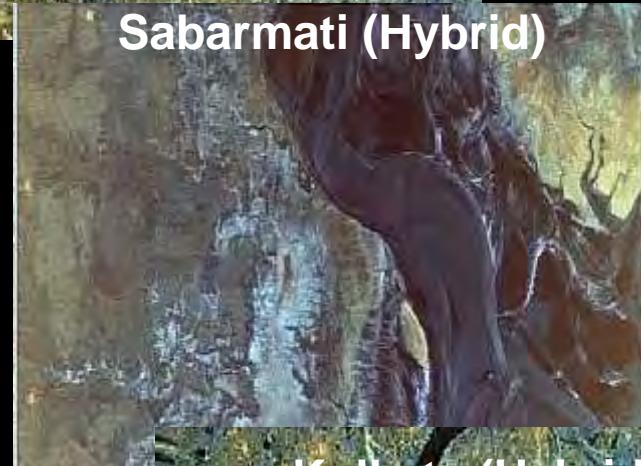


26 April 2012  
C-Band (Sngl, Dual, Hybrid)  
*Operational since 2015*

Rajasthan (Dual)



Sabarmati (Hybrid)



Kolkata (Hybrid)



# Space-borne PolSAR Sensors

## SENTINEL – 1A



S1A : April 2014      S1B : April 2016  
C-Band (Sngl, Dual)  
Revisit : 6 days

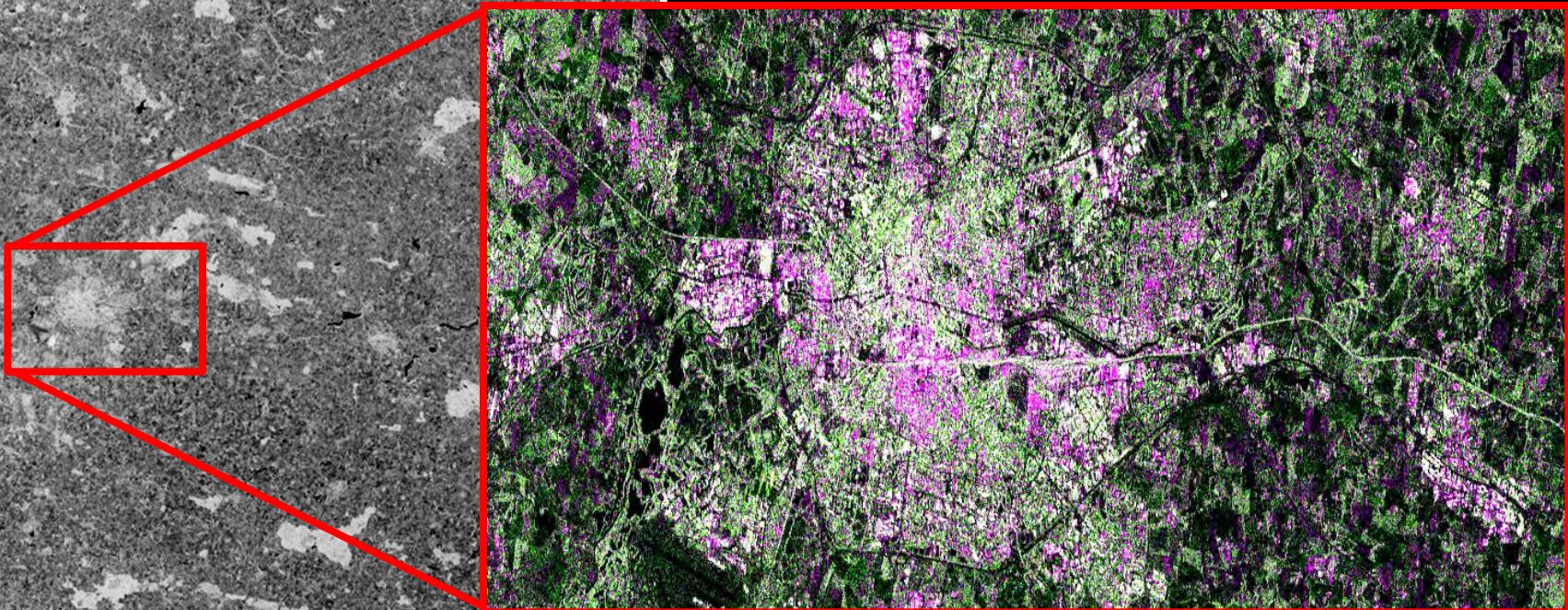


Brussels – 12 April 2014

# Space-borne PolSAR Sensors

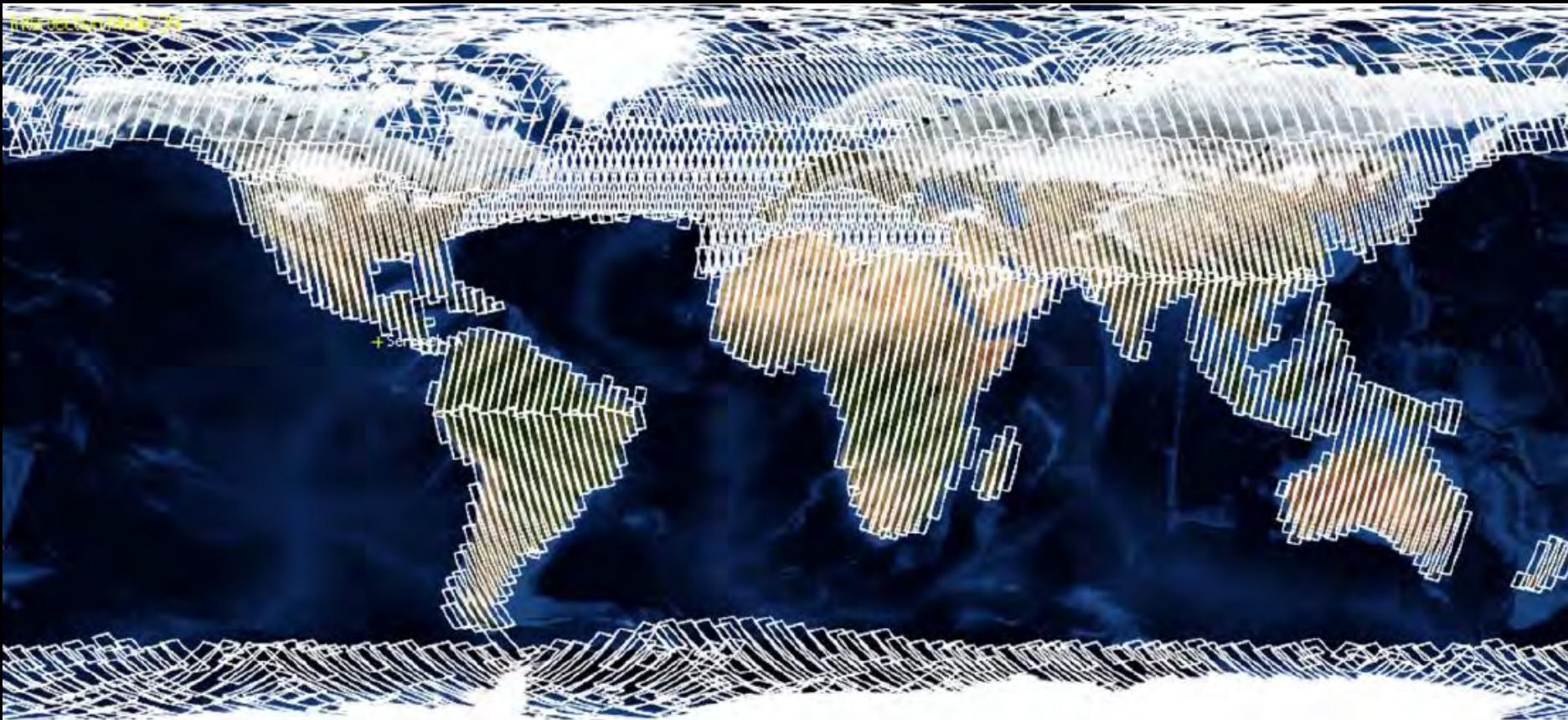


Rennes  
Brittany  
France



17/08/2016 @ 17h56

# Space-borne PolSAR Sensors

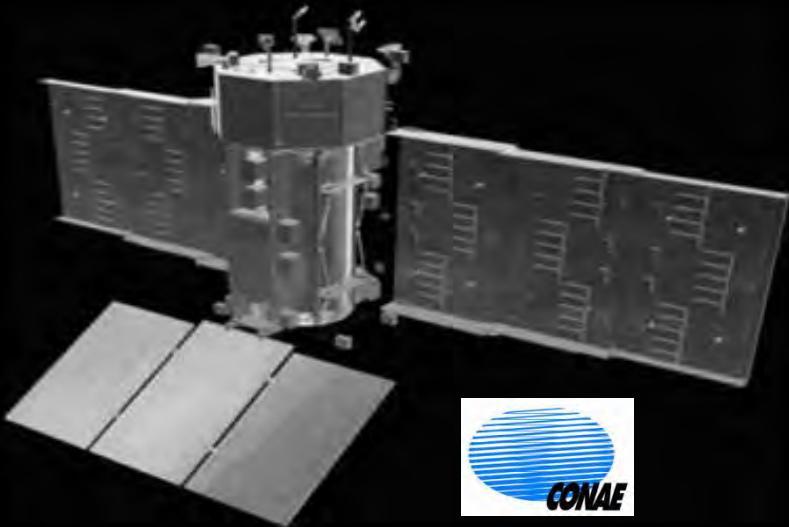


The screenshot shows the homepage of the Sentinel's Scientific Data Hub. At the top, there are links for "Scientific Hub", "API Hub", "User Guide", and "Roadmap". Below this is a section titled "Access Points" with a note about using the Access Point for API users. At the bottom, there are statistics: 5042 products published in the last 24h, 11568 products downloaded in the last 24h (Orbit - 495 MB), and 333927 queries received in the last 24h (Orbit - 495 MB).

<https://scihub.copernicus.eu/>

# Space-borne PolSAR Sensors

## SAOCOM – SAR-L



1A : 2017      1B : 2018  
2A : 2019      2B : 2020

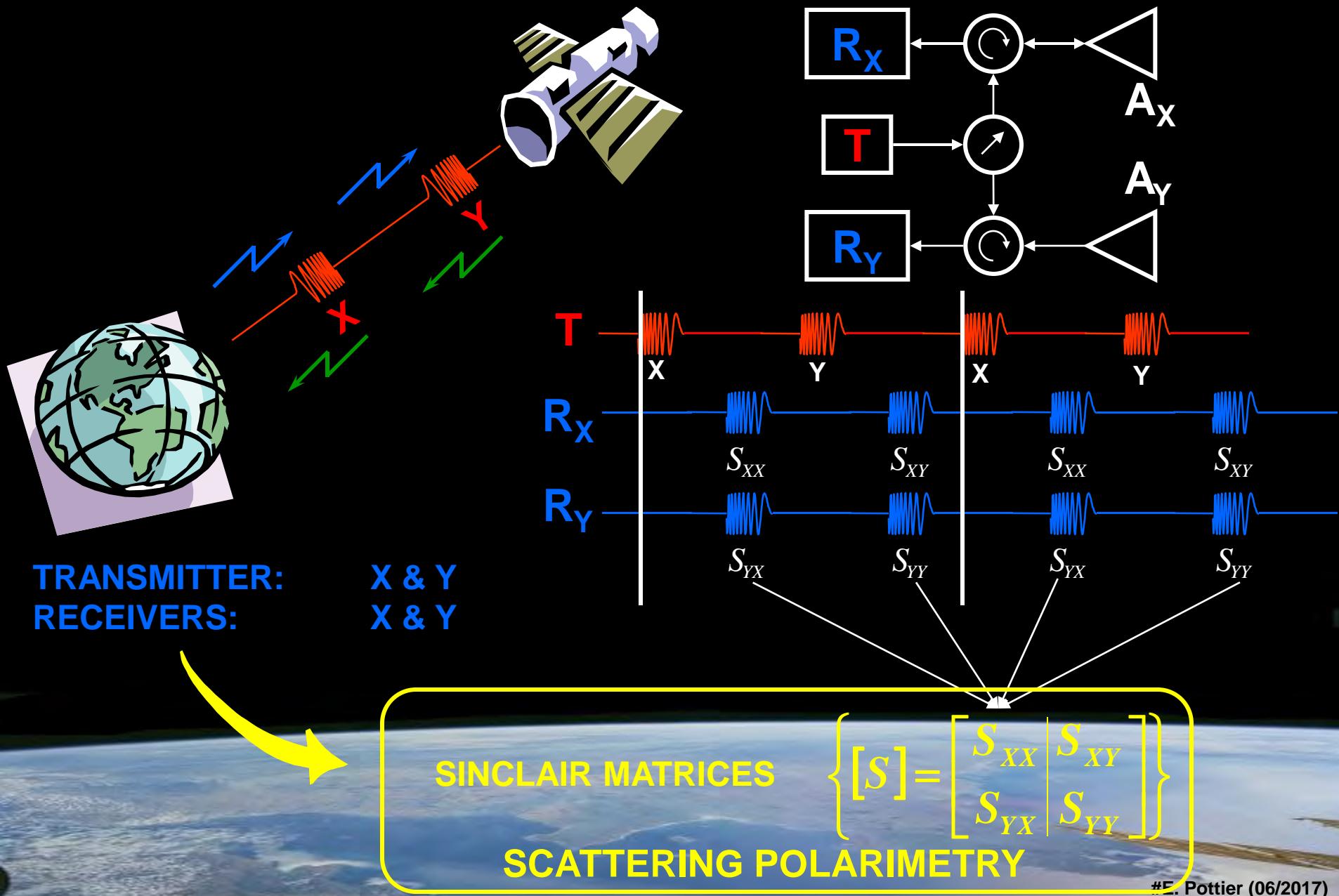
L-Band (Sngl, Dual, Twin HH-VV)  
Revisit : 4 days

## RADARSAT Constellation Mission (RCM)

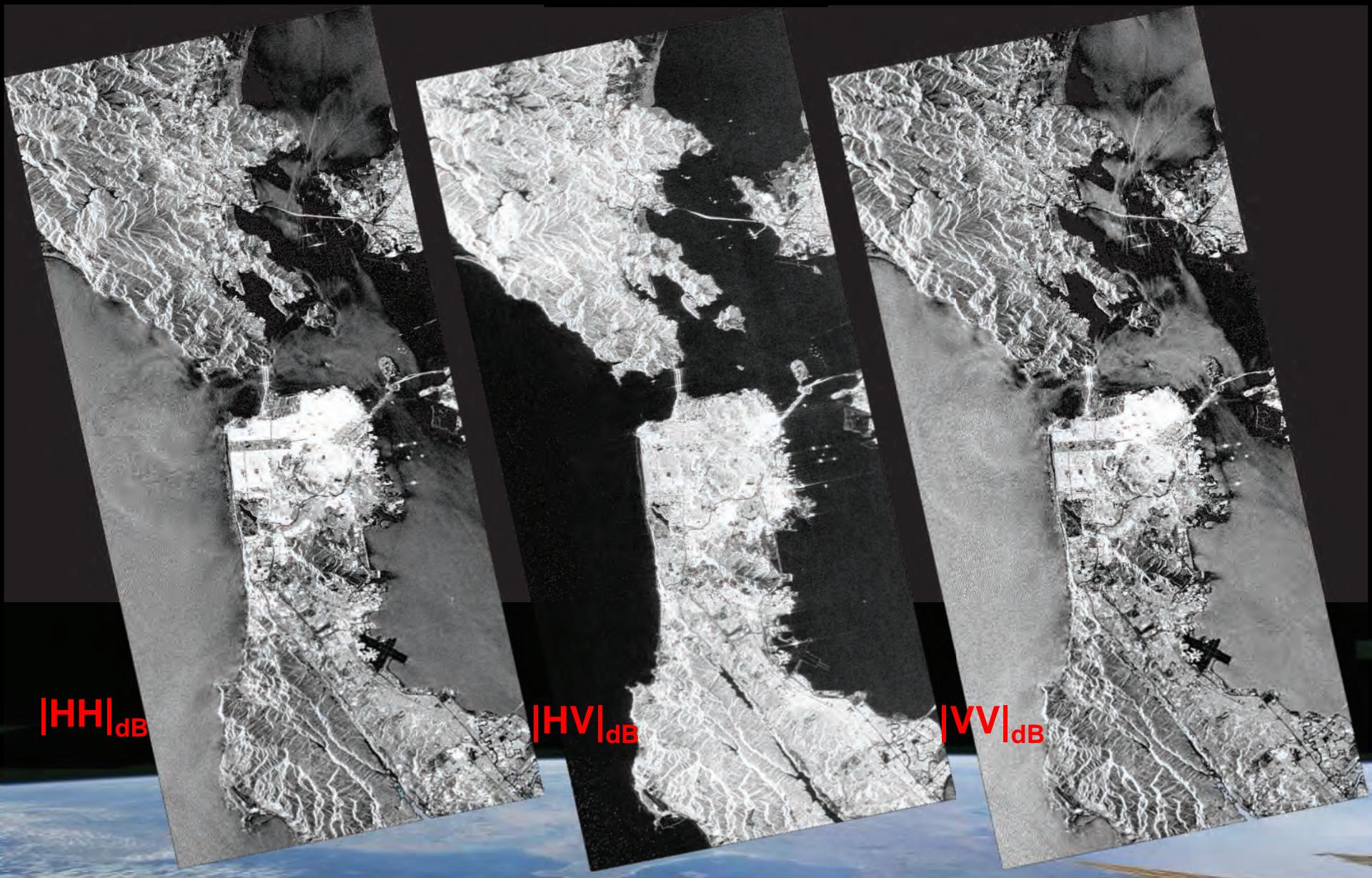


1A : 2017      1B / 1C : 2018  
C-Band (Sngl, Dual, Hybrid)  
Revisit : 4 days

# Scattering Polarimetry



# Space-borne Sensors



San Francisco Bay – (L-Band)

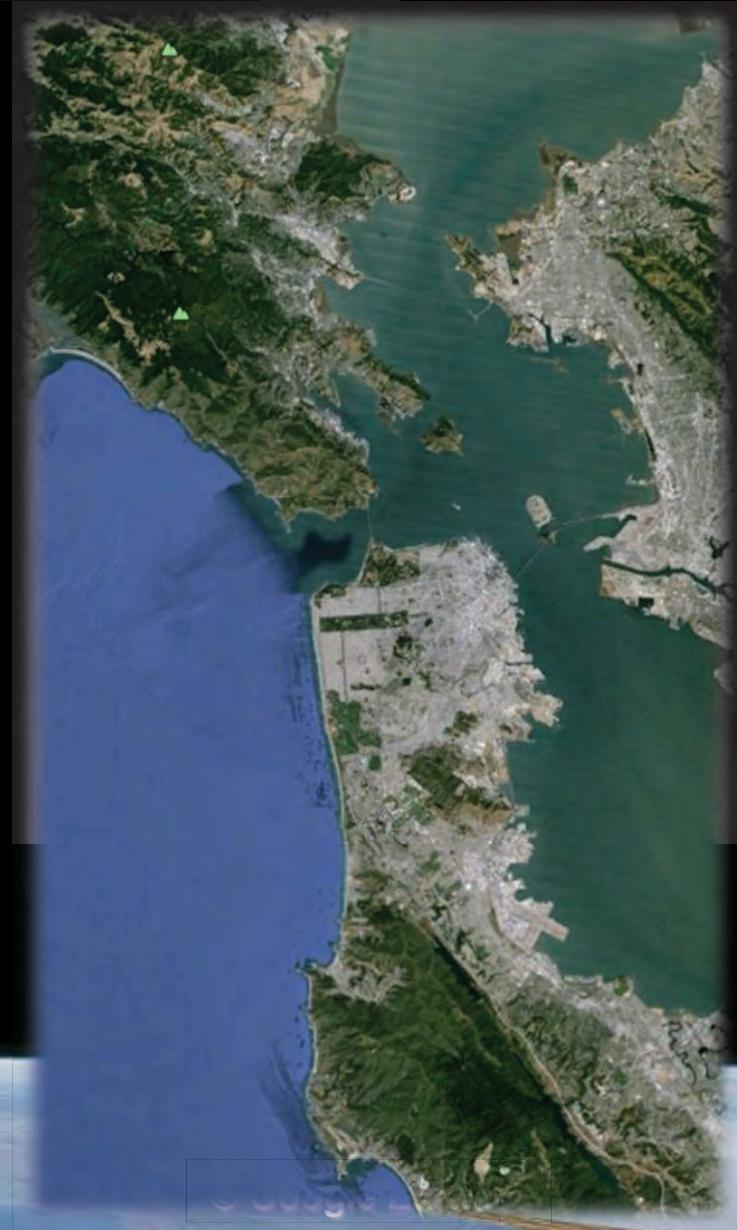
# Space-borne Sensors



$|HH|_{dB}$

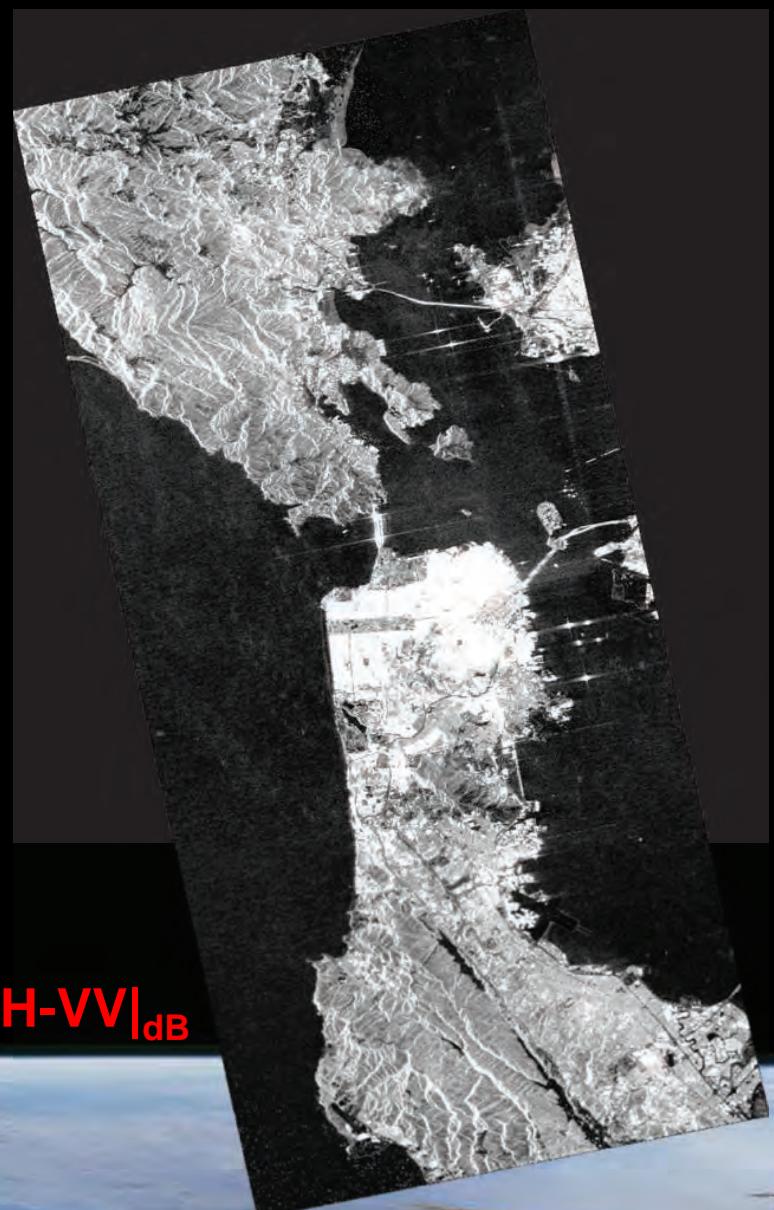
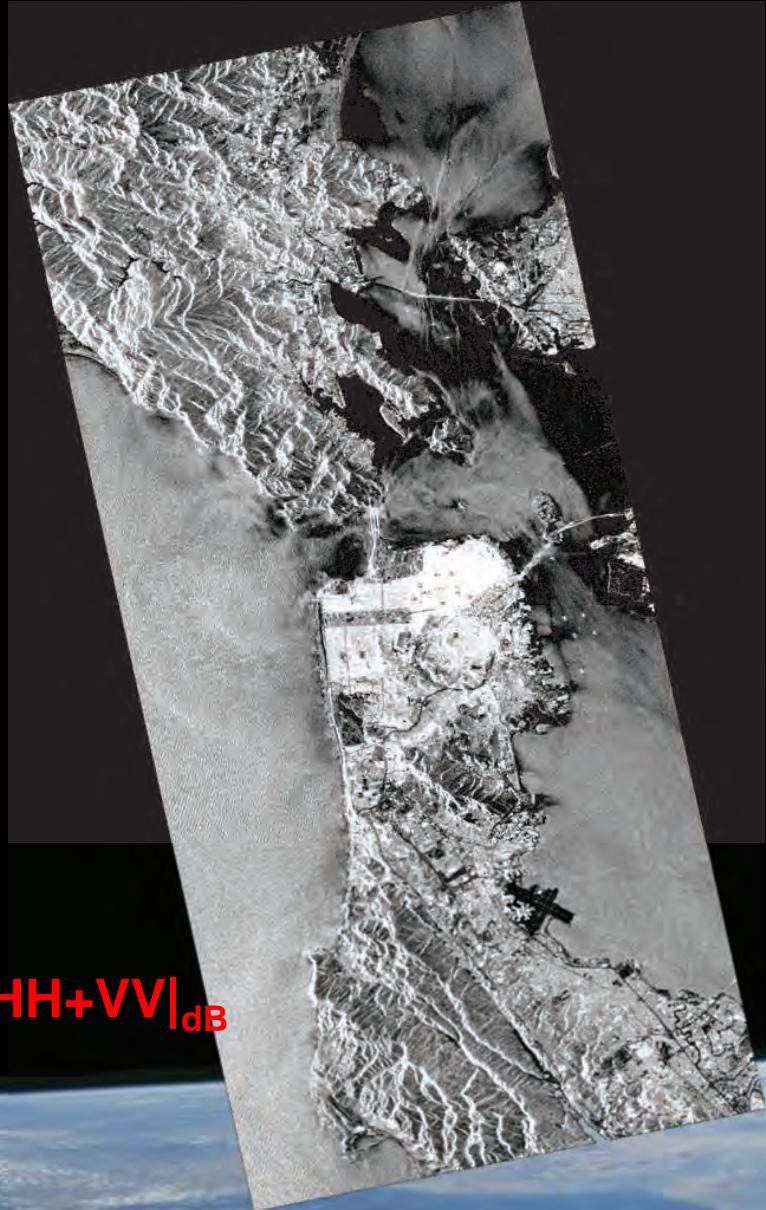
$|HV|_{dB}$

$|VV|_{dB}$



San Francisco Bay – (L-Band)

# Space-borne Sensors



San Francisco Bay – (L-Band)

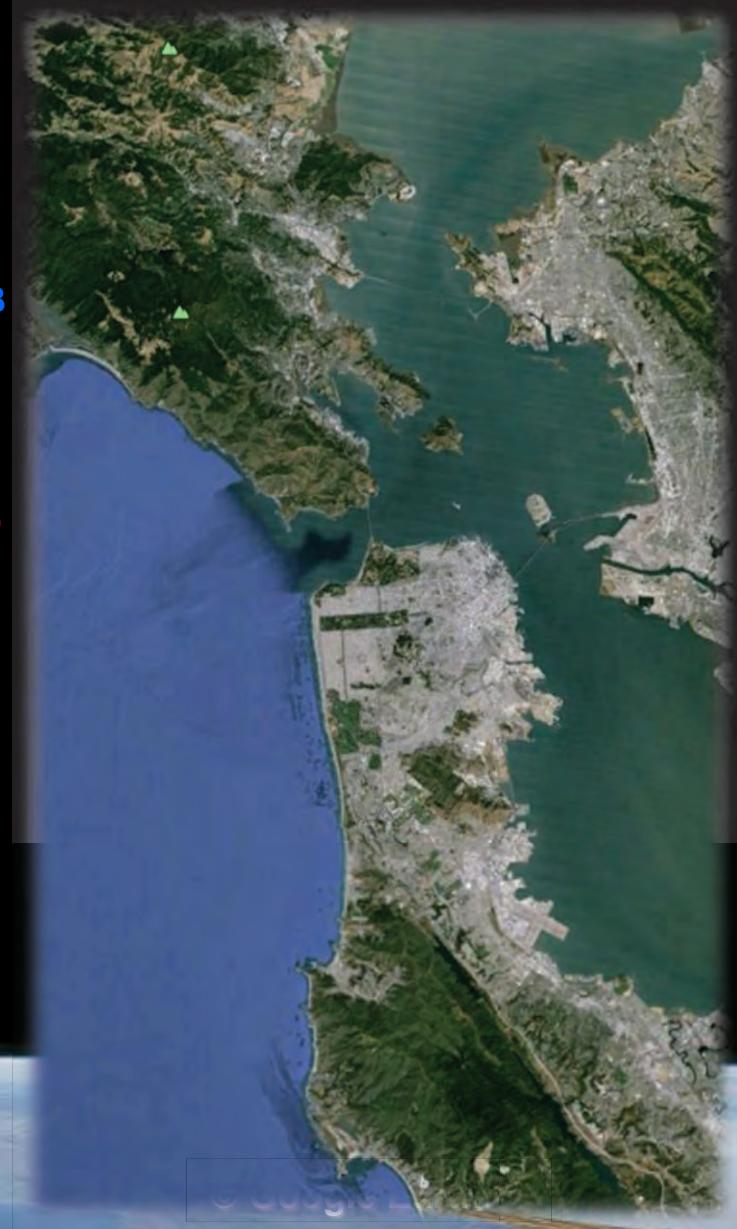
# Space-borne Sensors



$|HH+VV|_{dB}$

$|HV|_{dB}$

$|HH-VV|_{dB}$



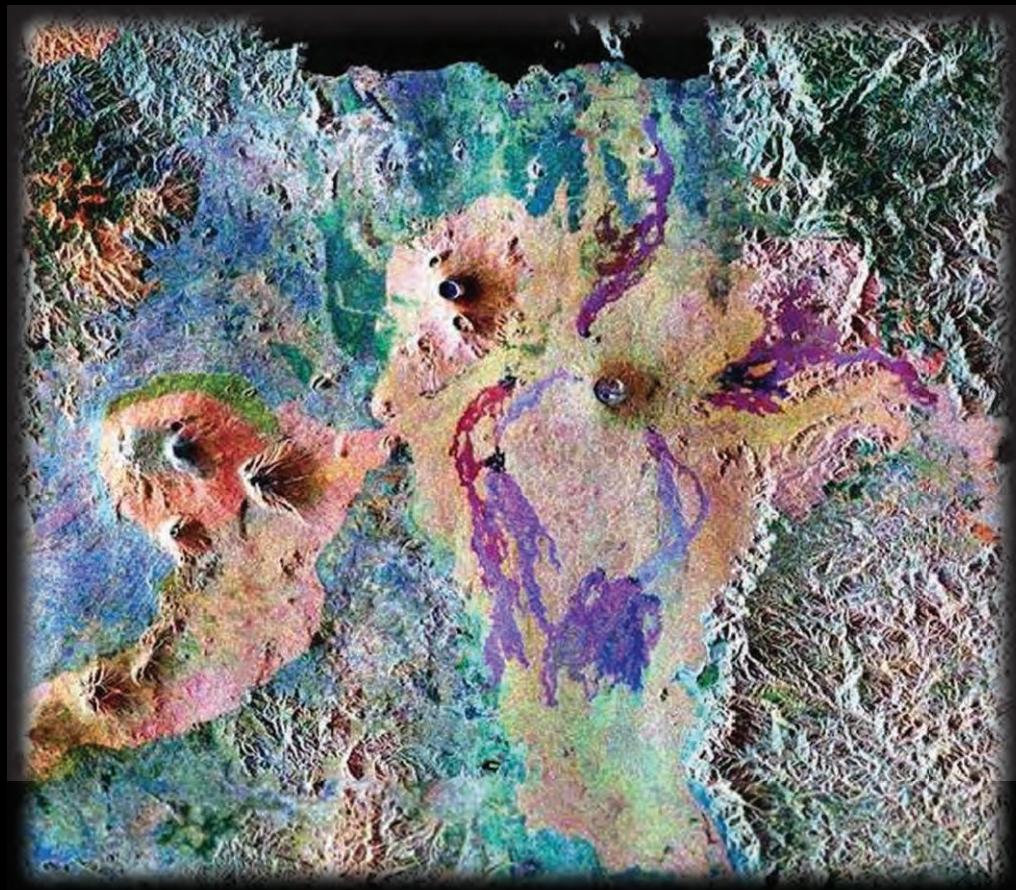
San Francisco Bay – (L-Band)

# Space-borne PolSAR Sensors

## SIR-C / X-SAR



April 1994  
L- and C-Band (Quad)  
X-Band (Sngl)



Rwanda, Zaire, Uganda

# Space-borne PolSAR Sensors

## ALOS - PALSAR



January 2006  
L-Band (Sngl / Twin / Quad)



ALOS : Advanced Land Observing Satellite  
PALSAR : Phase Array L-Band SAR

# Space-borne PolSAR Sensors

## RADARSAT - 2



December 2007  
C-Band (Quad)



# Space-borne Sensors



$|HH+VV|_{dB}$

$|HV|_{dB}$

$|HH-VV|_{dB}$



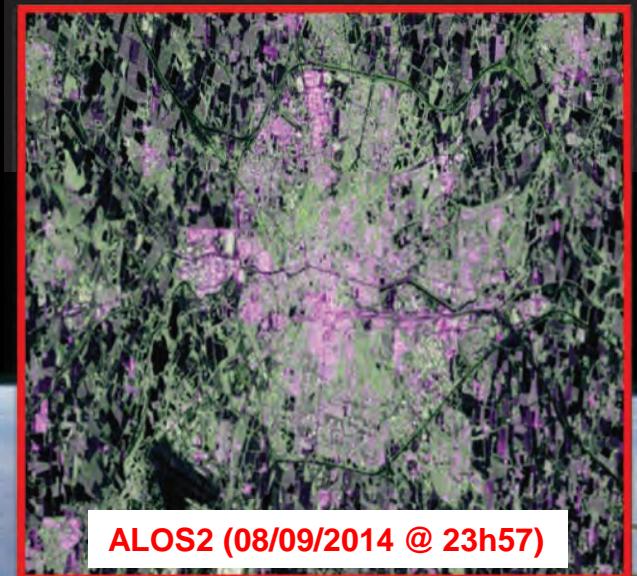
San Francisco Bay – (L-Band and C-Band)

# Space-borne PolSAR Sensors

## ALOS - 2



May 2014  
L-Band (Quad)



# Space-borne PolSAR Sensors

Chang Zheng-4C - GaoFen-3 (GF-3)

*Long March-4C - High Resolution-3*



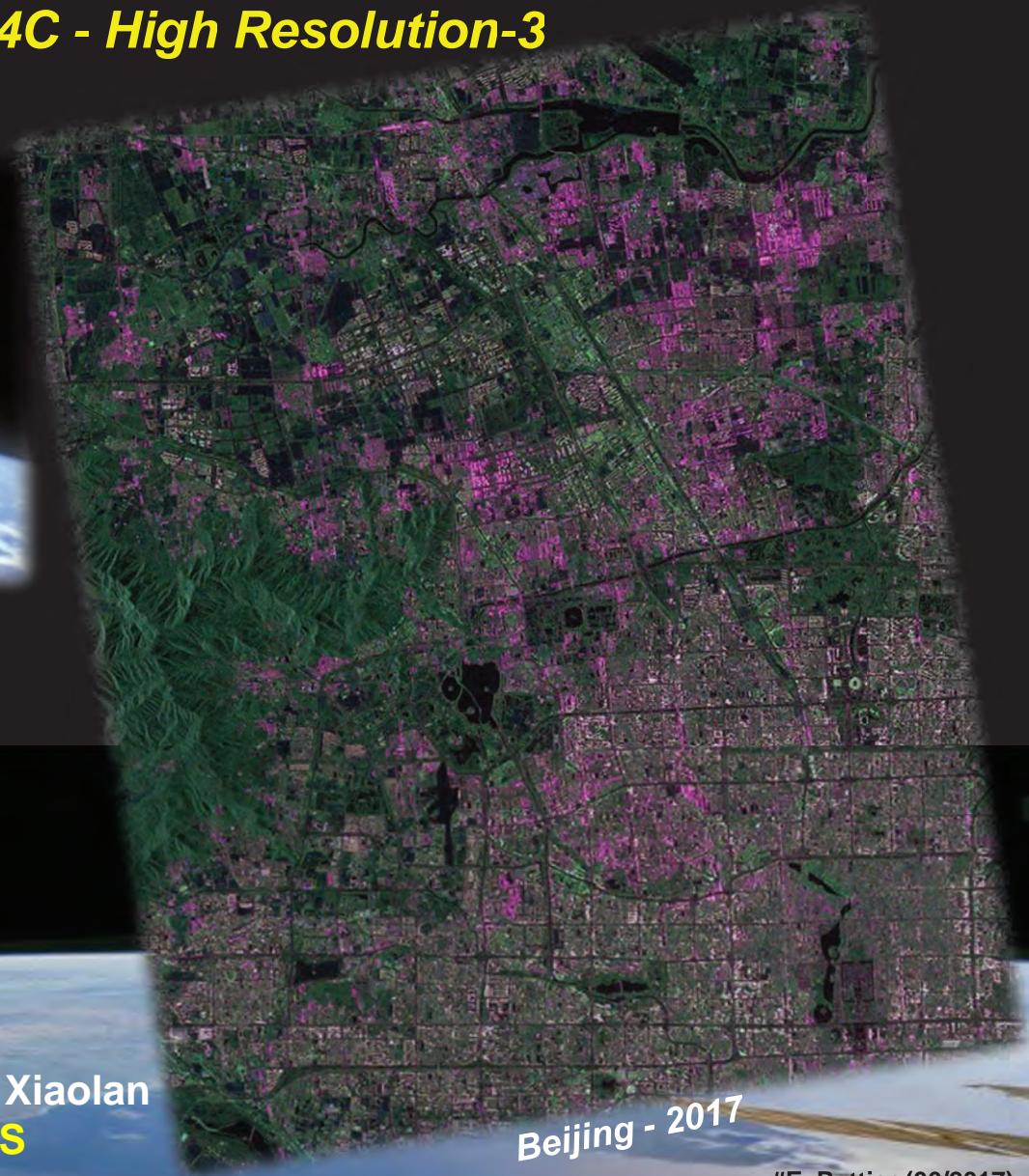
August 2016  
C-Band (Quad)



中国空间技术研究院  
China Academy of Space Technology

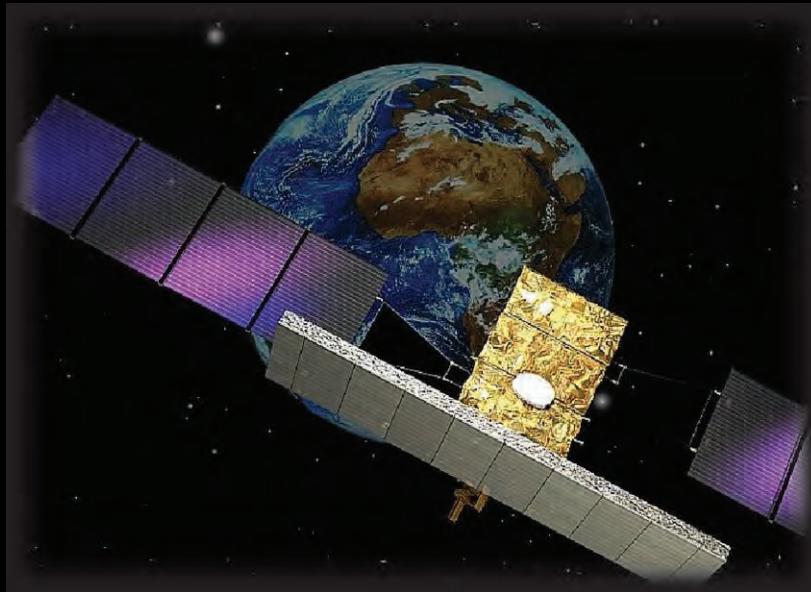


Courtesy of Dr. Qiu Xiaolan  
IECAS / GIPAS

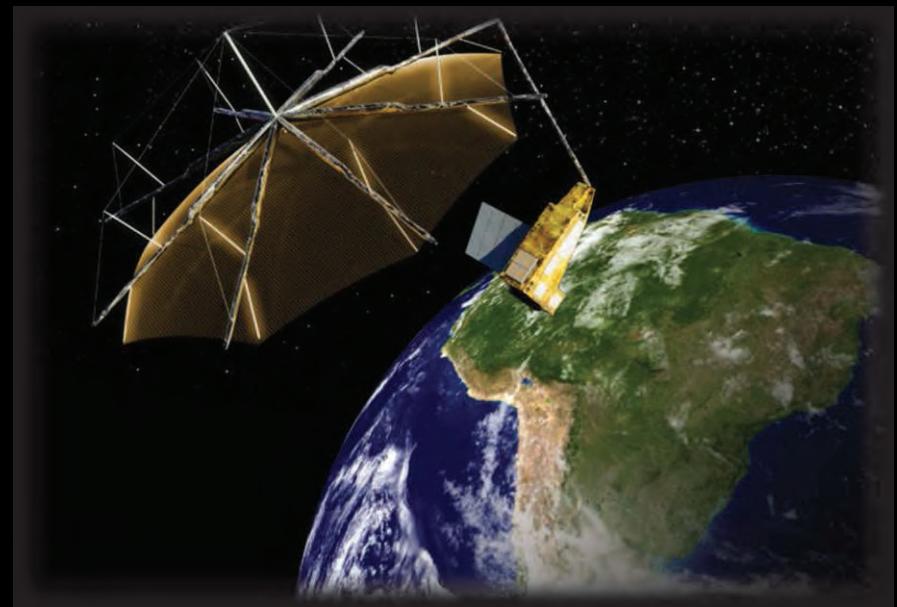


# Space-borne PolSAR Sensors

COSMO - SkyMed - CSG



Earth Explorer - BIOMASS

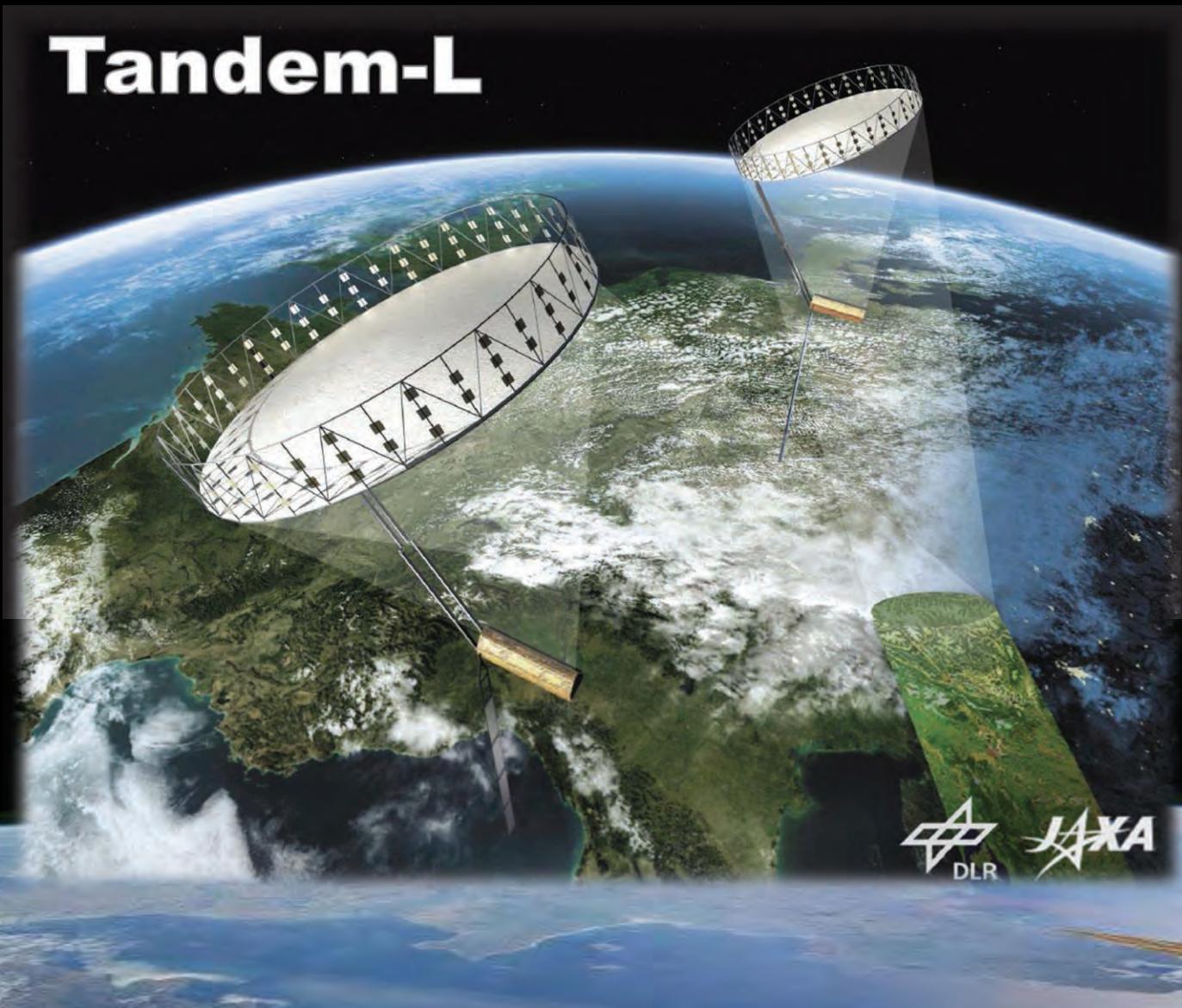


2A : 2018      2B : 2019  
X-Band (Sngl / Dual / Quad Exp.)

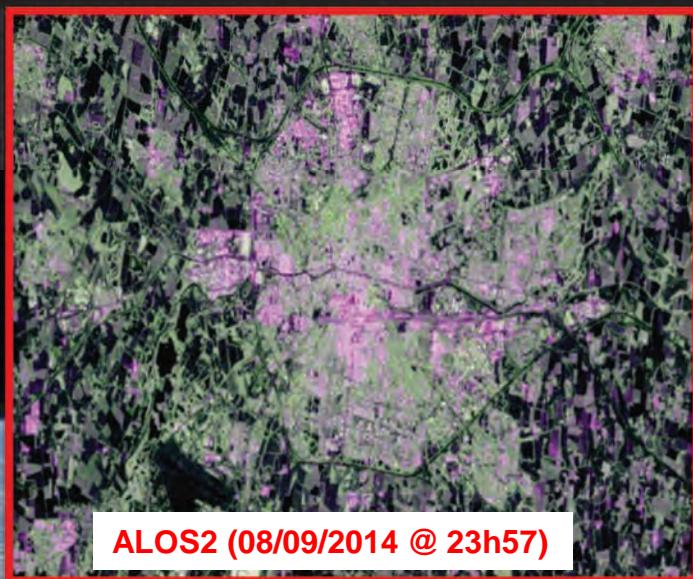
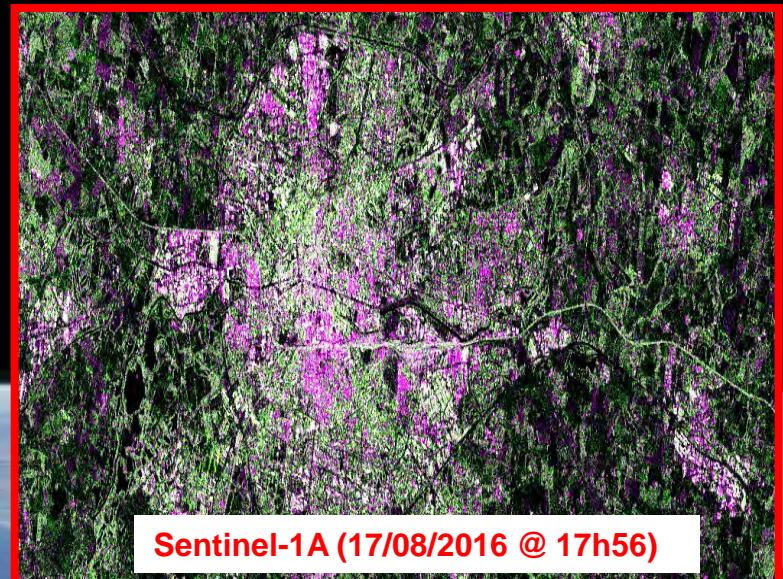
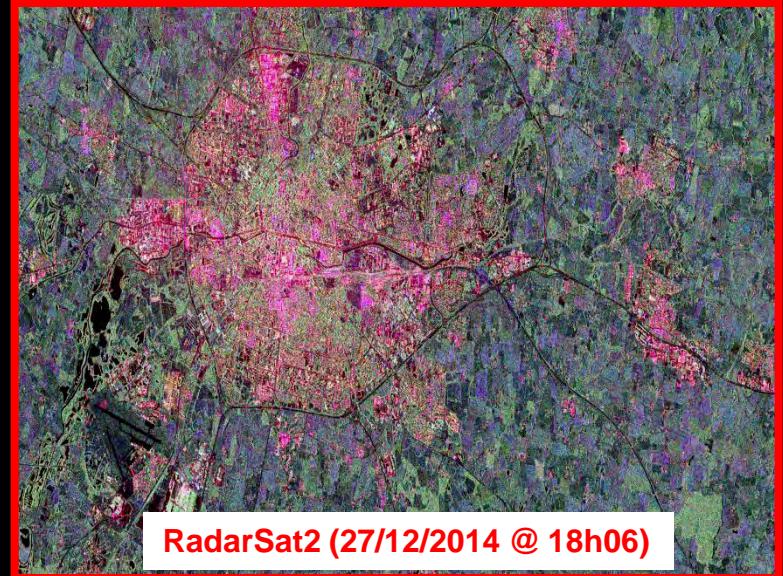
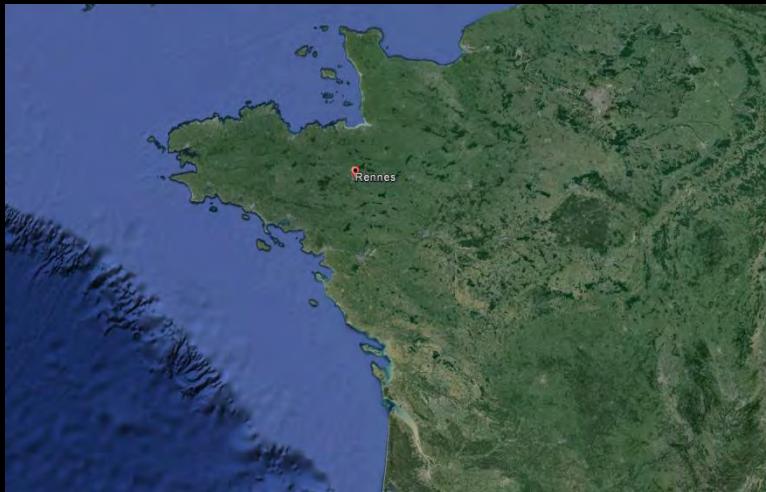
2019  
P-Band (Quad)

# Space-borne PolSAR Sensors

## Tandem-L



# Space-borne PolSAR Sensors



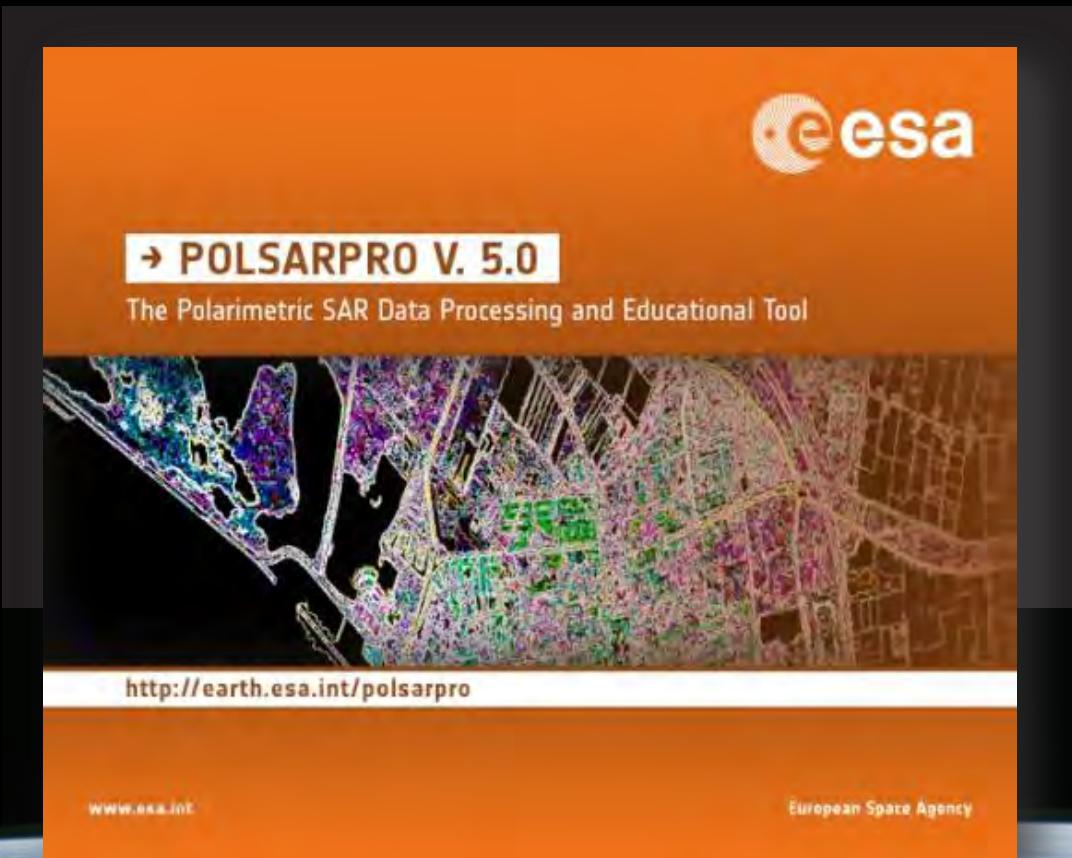
# **What About**



# **Software / Toolbox ?**

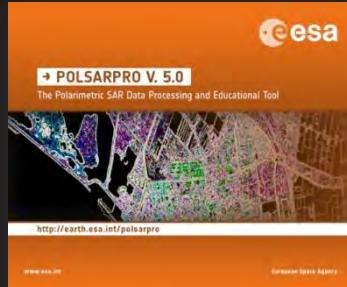
# ESA PolSARpro Toolbox

## The Polarimetric SAR Data Processing and Educational Toolbox



# ESA PolSARpro Toolbox

Polarimetric SAR data processing and educational toolbox



ESA funded project since 2003

+ 3000 registered users / + 70 foreign countries

Toolbox specifically designed to handle : Pol-SAR, Pol-InSAR and Pol-TimeSAR data

Educational Software offering a tool for self-education in the field of Polarimetric SAR data processing and analysis

International collaborative project : space agencies (4), research centres (14) and universities (19).

Airborne sensors : AIRSAR, CONVAIR, ESAR, EMISAR, FSAR, PISAR, SATHI, UAVSAR.

Spaceborne sensors : ALOS1, ALOS2, COSMO-Skymed, RADARSAT-2, RISAT, Sentinel 1A/B, TerraSAR-X, Tandem-X,

More than 550 different Pol-SAR, Pol-InSAR, Pol-TomSAR, Pol-TimeSAR functionalities.

# ESA PoISARpro Toolbox

**<http://earth.esa.int/web/polsarpro>**

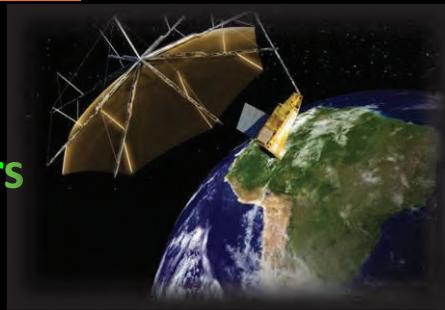
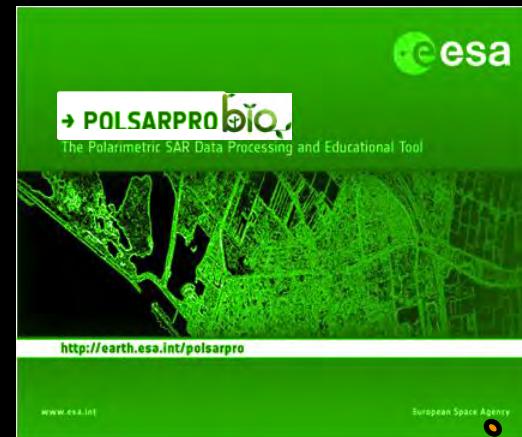
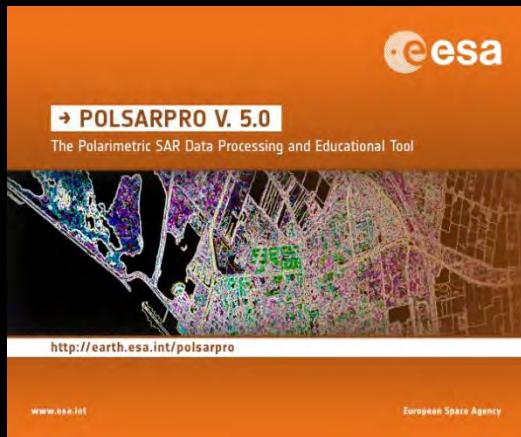
**The Web Site provides**

The screenshot shows the homepage of the PoISARpro website. At the top, there's a navigation bar with links for 'Data Sources', 'Overview', 'Download and Installation', 'Documentation', and 'Results & News'. Below the navigation is a main content area. On the left, a sidebar lists 'PolSARpro Version 4.2' and 'Latest News'. The 'Latest News' section contains a list of five items: 'New PoISARpro version 4.2 released', 'New PoISARpro version 4.1.5 released', 'New PoISARpro version 4.0 Beta 1.3 released', 'PoISARpro v. 4.0 beta 1 training course -', and 'PoISARpro version 4.0 beta 1 released for'. On the right, another sidebar titled 'Useful Links' lists various project resources. At the bottom of the page, there's a footer with the text '© ESA 2000 - 2014'.

- **Details of the project**
- **Access to the tutorial and software**
- **Information about status of the development**
- **Demonstration Sample Datasets**

# ESA PolSARpro Toolbox

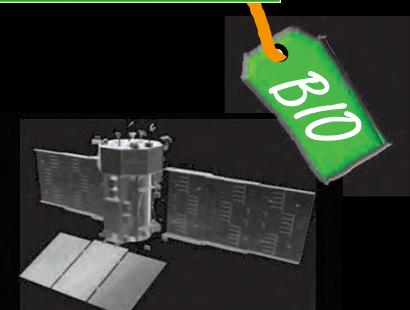
ESA & third party fully polarimetric SAR missions (**PolSARpro-Bio**)



BIOMASS



R.C.M



SAOCOM-CS

Future spaceborne sensors

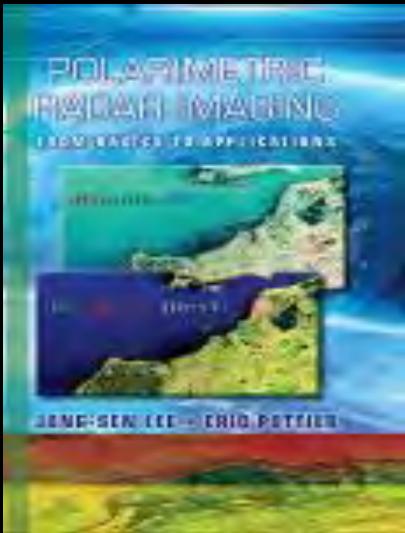
New functionalities : Pol-SAR, Pol-TomSAR and Pol-TimeSAR / Cloud-based infrastructure ...

# Learning / Training

## Next P.I Generations



# Books On Polarimetric Radar SAR, Polarimetric Interferometry



**Polarimetric Radar Imaging: From basics to applications**

***Jong-Sen LEE – Eric POTTIER***

CRC Press; 1st ed., February 2009, pp 422

ISBN: 978-1420054972



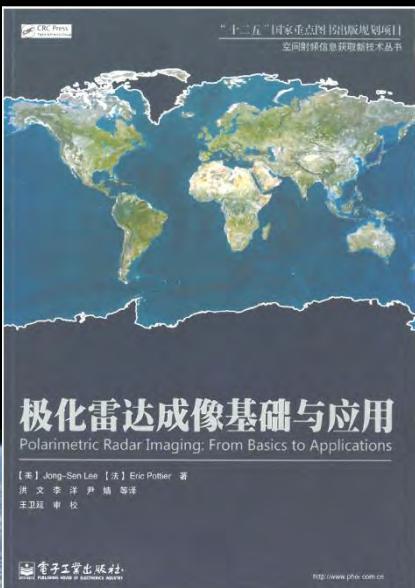
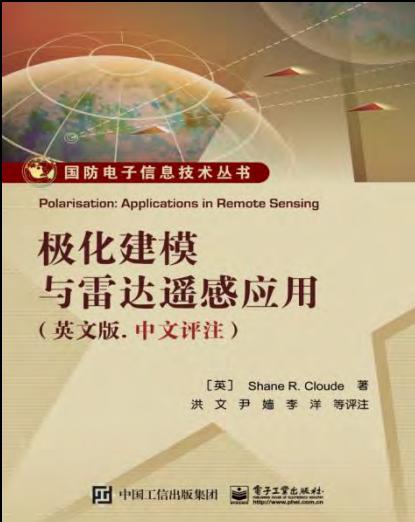
**Polarisation: Applications in Remote Sensing**

***Shane R. CLOUDE***

Oxford University Press, October 2009, pp 352

ISBN: 978-0199569731

# Books On Polarimetric Radar SAR, Polarimetric Interferometry



## Polarisation: Applications in Remote Sensing

**Shane R. CLOUDE**

Oxford University Press, October 2009, pp 352

ISBN: 978-0199569731

**Prof. Wen HONG, Dr. Qiang YIN et al.**



## Polarimetric Radar Imaging: From basics to applications

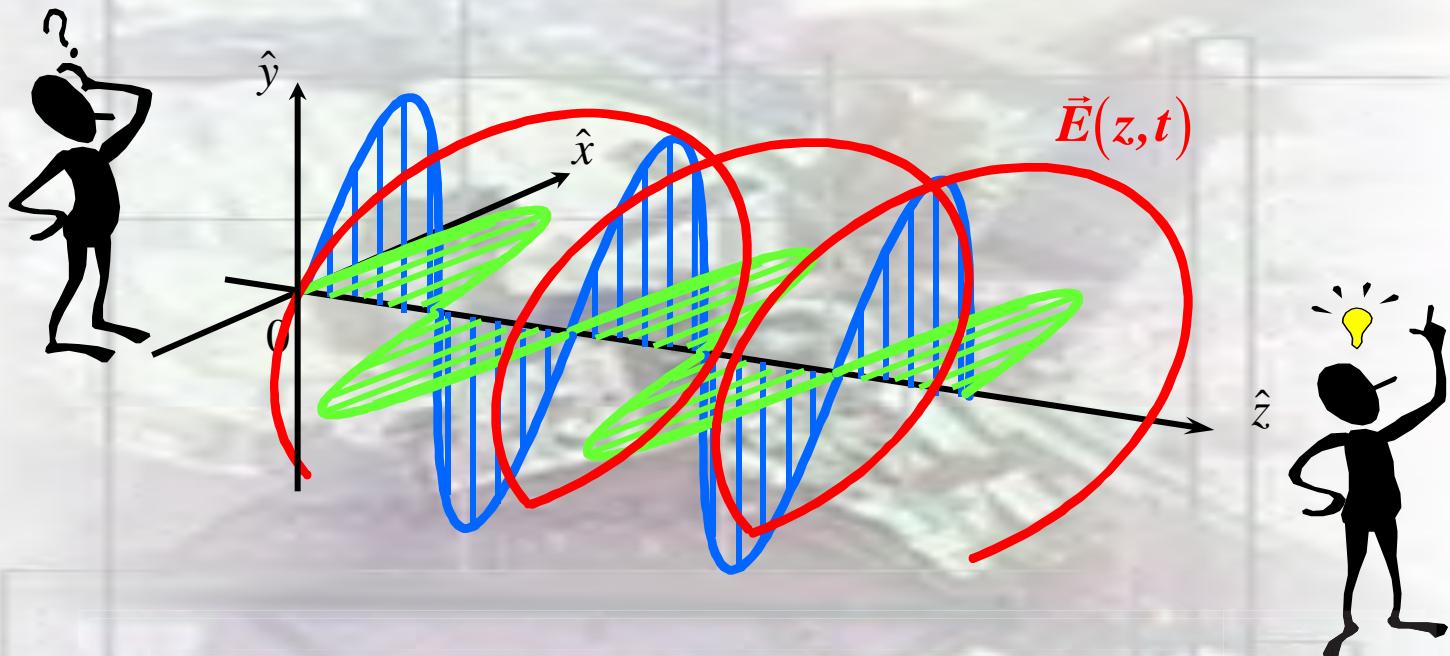
**Jong-Sen LEE – Eric POTTIER**

CRC Press; 1st ed., February 2009, pp 422

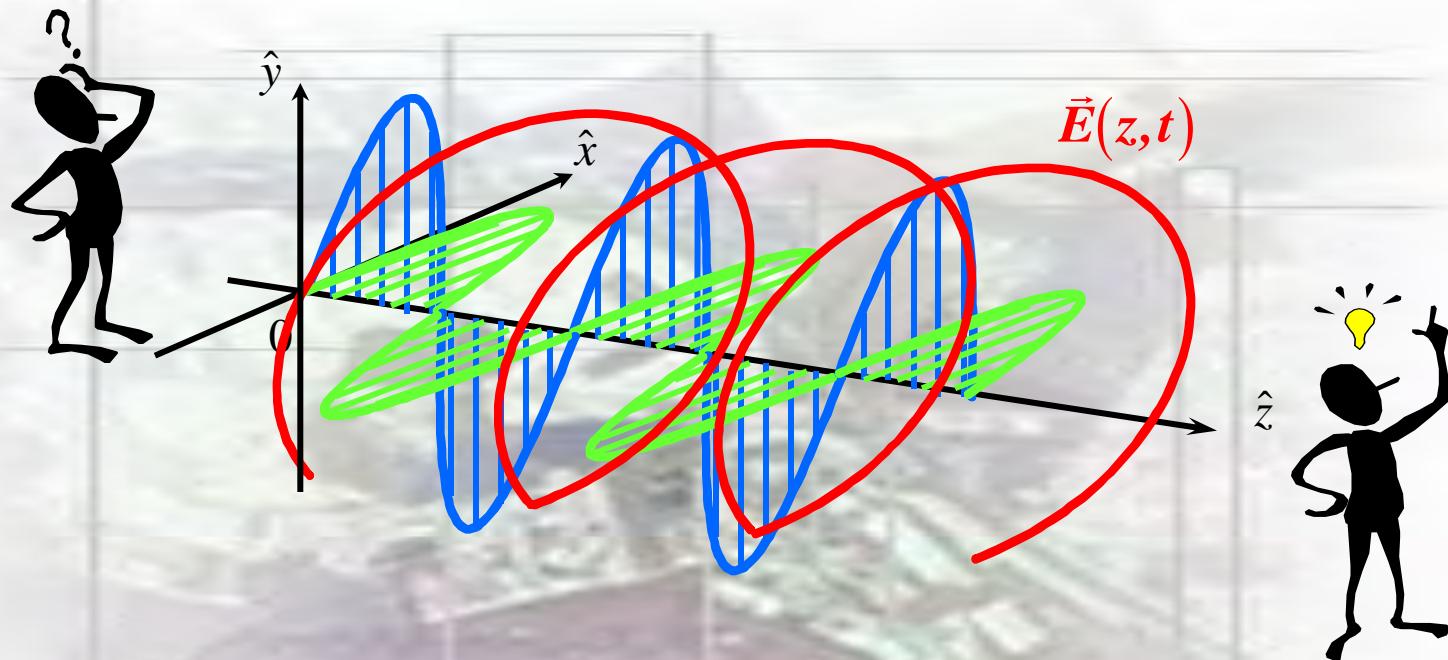
ISBN: 978-1420054972

Questions ?

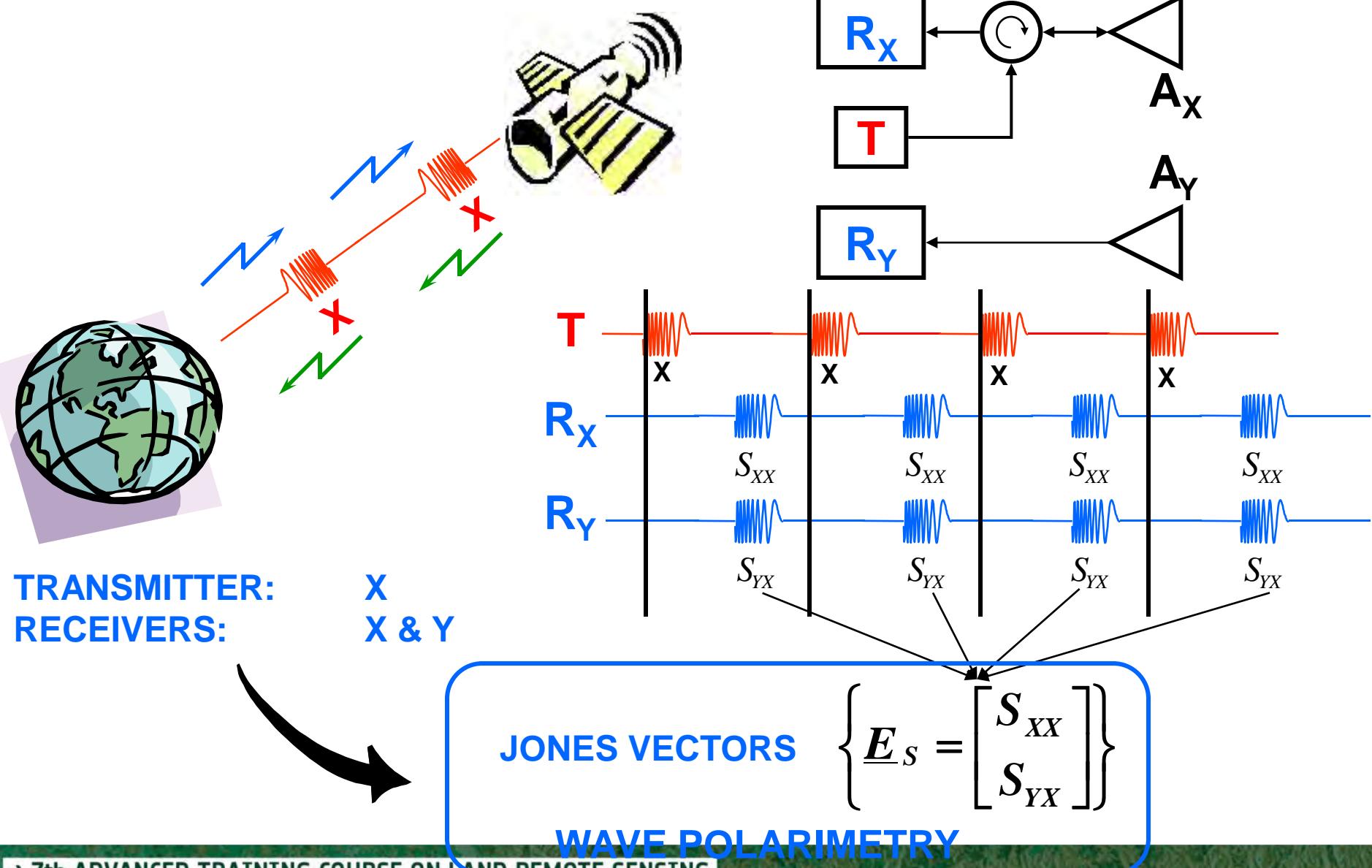


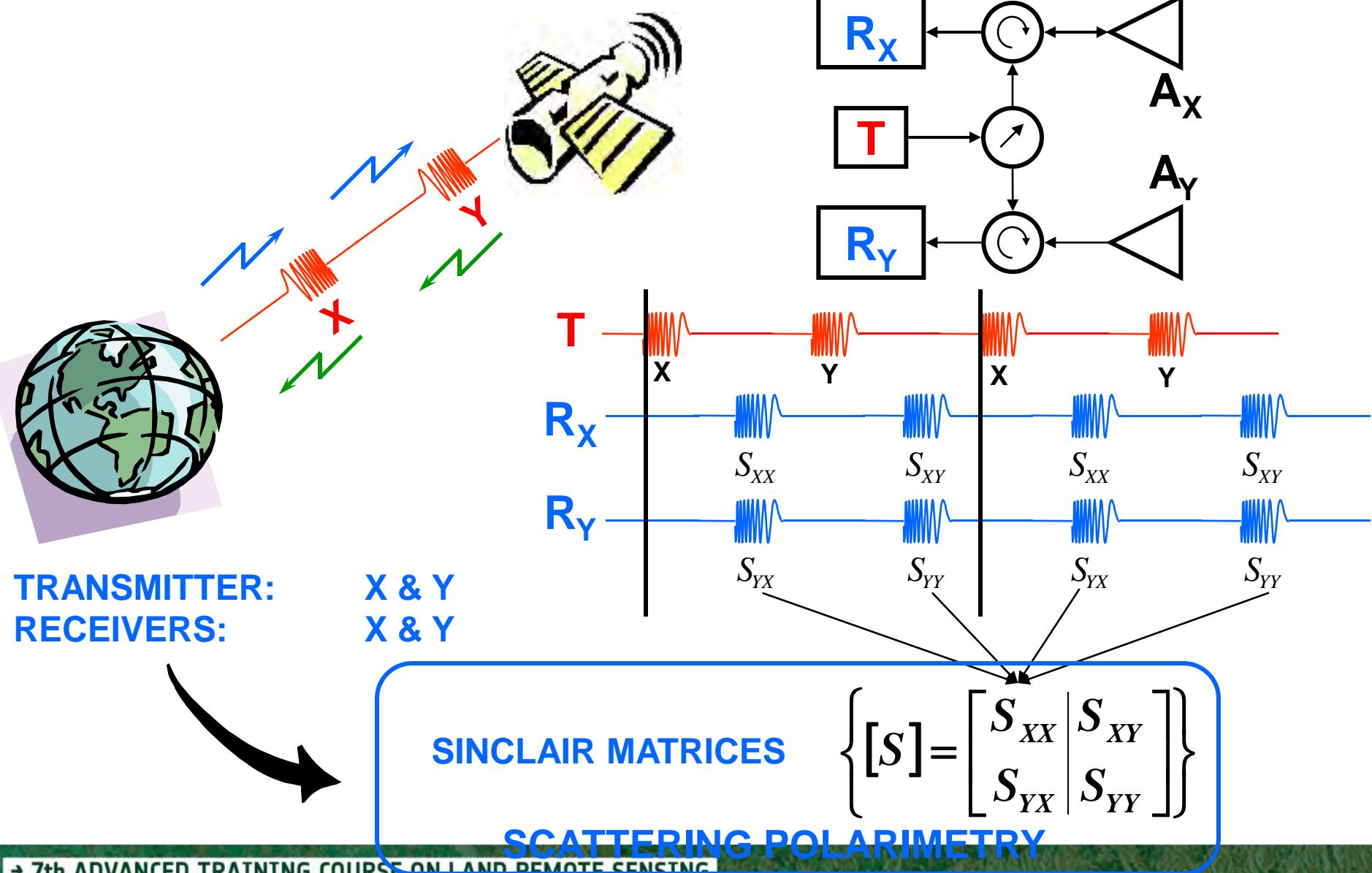


# BASIC CONCEPTS



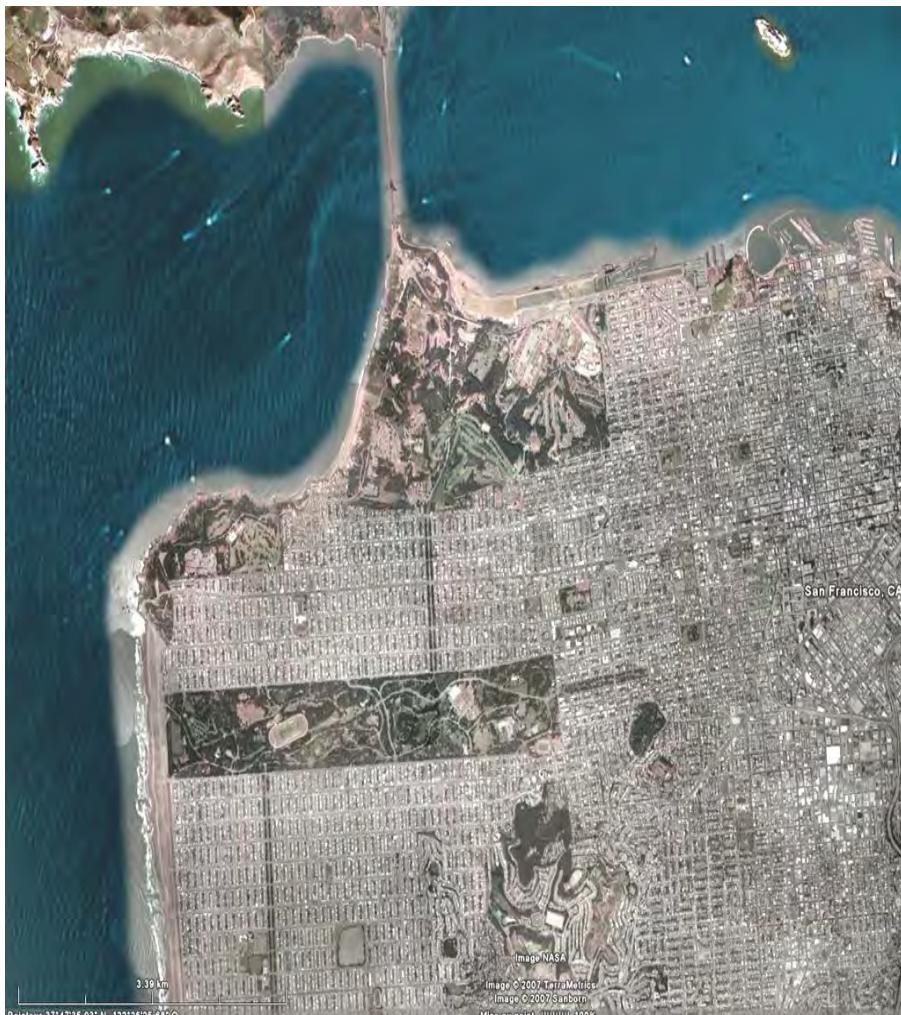
# SCATTERING POLARIMETRY





$\xrightarrow{\text{Tx}}$  $\xrightarrow{\text{Rx}}$  $\xrightarrow{\text{Tx}}$  $\xrightarrow{\text{Rx}}$  $\xrightarrow{\text{Tx}}$  $\xrightarrow{\text{Rx}}$  $|\text{HH}|_{\text{dB}}$  $|\text{HV}|_{\text{dB}}$  $|\text{VV}|_{\text{dB}}$ 

## Sinclair Color Coding



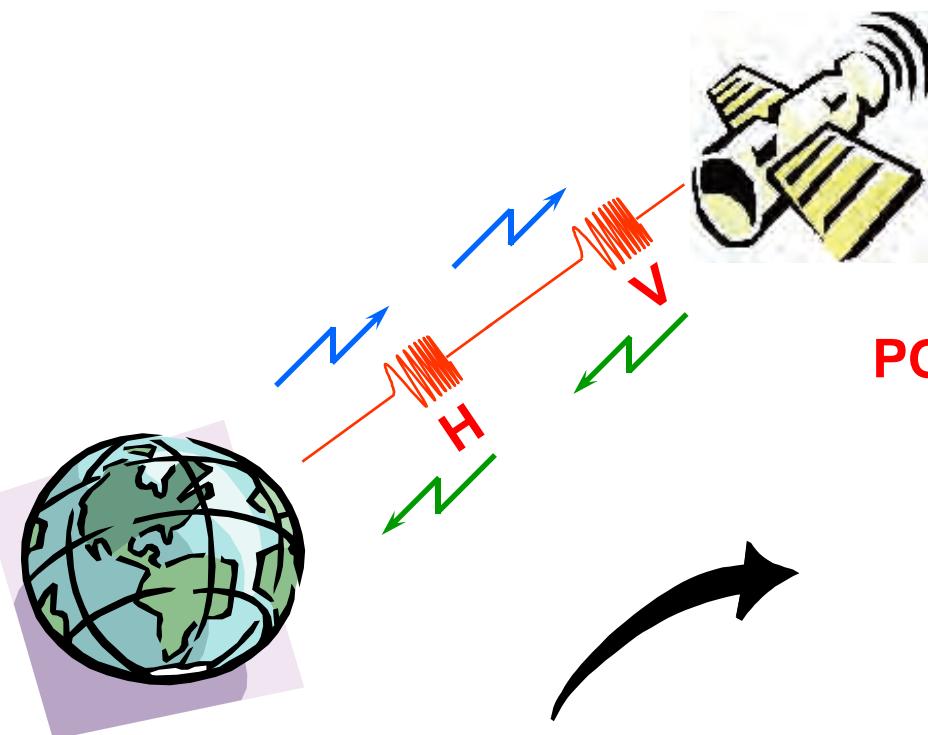
© Google Earth



|HH|

|HV|

|VV|



## POLARIMETRIC DESCRIPTORS

[S] SINCLAIR Matrix

$$[S] = \begin{bmatrix} S_{HH} & | & S_{HV} \\ S_{VH} & | & S_{VV} \end{bmatrix}$$

TRANSMITTER: H & V  
RECEIVERS: H & V

k Target Vector  
[T] 3x3 COHERENCY Matrix

**TARGET VECTOR  $\underline{k}$** 

$$\underline{k} = \frac{1}{\sqrt{2}} [ S_{HH} + S_{VV} \quad S_{HH} - S_{VV} \quad 2S_{HV} ]^T$$

**COHERENCY MATRIX [ $\mathbf{T}$ ]**

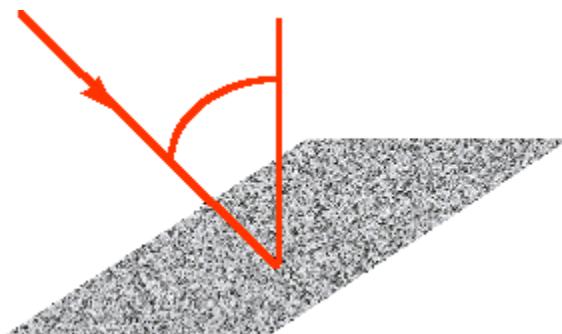
$$[\mathbf{T}] = \underline{k} \cdot \underline{k}^{*T} = \begin{bmatrix} 2A_0 & C - jD & H + jG \\ C + jD & B_0 + B & E + jF \\ H - jG & E - jF & B_0 - B \end{bmatrix}$$

**HERMITIAN MATRIX - RANK 1****A0, B0+B, B0-B : HUYNEN TARGET GENERATORS**

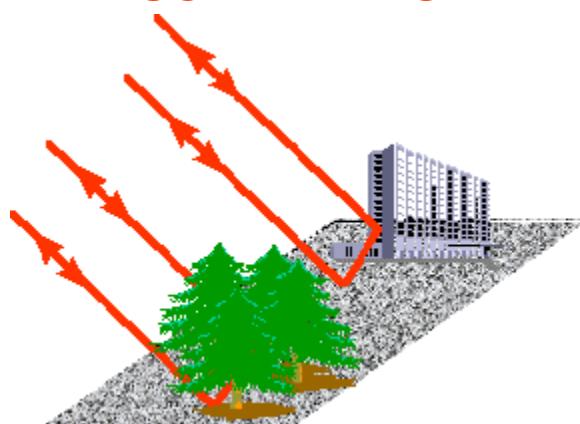
**[ $\mathbf{T}$ ]** is closer related to Physical and Geometrical Properties of the Scattering Process, and thus allows a better and direct physical interpretation

## PHYSICAL INTERPRETATION

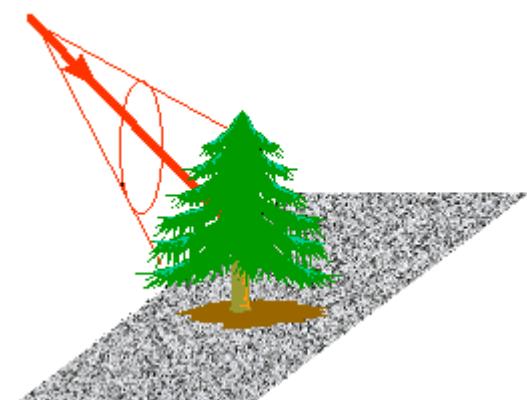
**SINGLE BOUNCE  
SCATTERING  
(ROUGH SURFACE)**



**DOUBLE BOUNCE  
SCATTERING**



**VOLUME  
SCATTERING**



$$T_{11} = 2A_0 = |S_{XX} + S_{YY}|^2$$

$$T_{33} = B_0 - B = 2|S_{XY}|^2$$

$$T_{22} = B_0 + B = |S_{XX} - S_{YY}|^2$$

# TARGET GENERATORS



$|HH+VV|_{dB}$



$|HV|_{dB}$



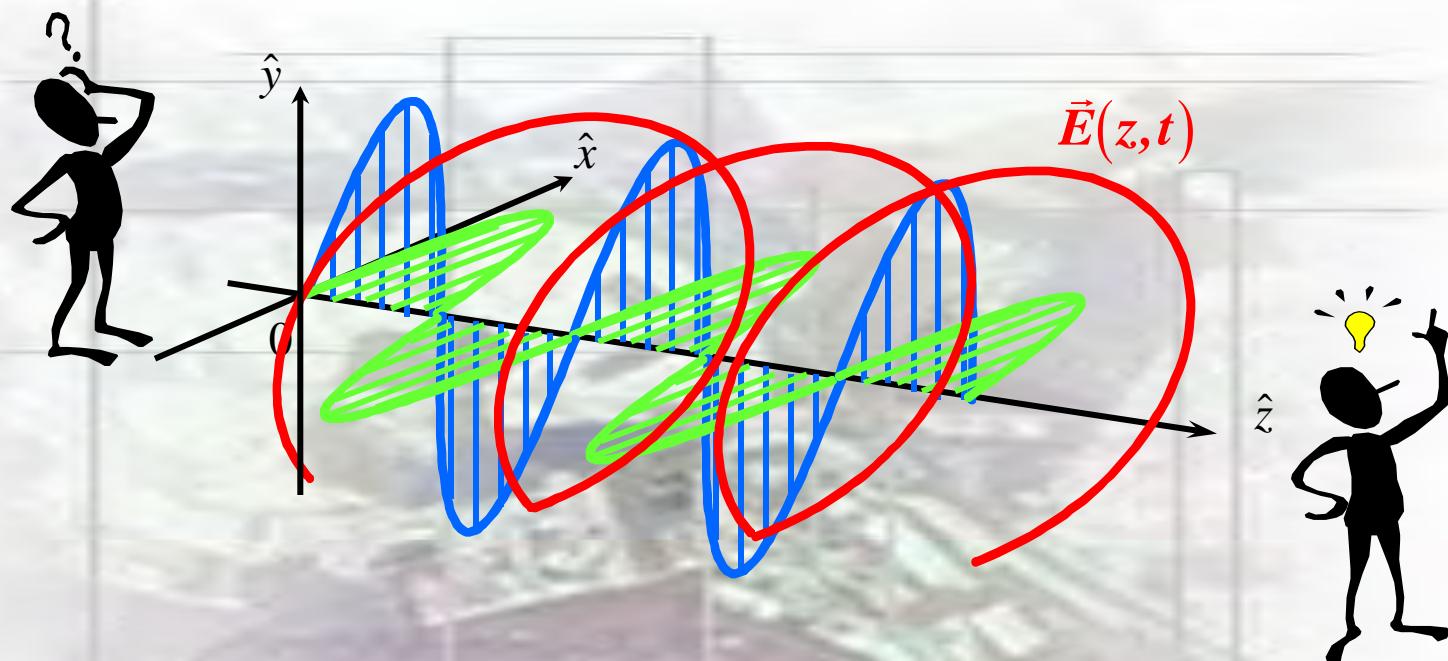
$|HH-VV|_{dB}$

# TARGET GENERATORS

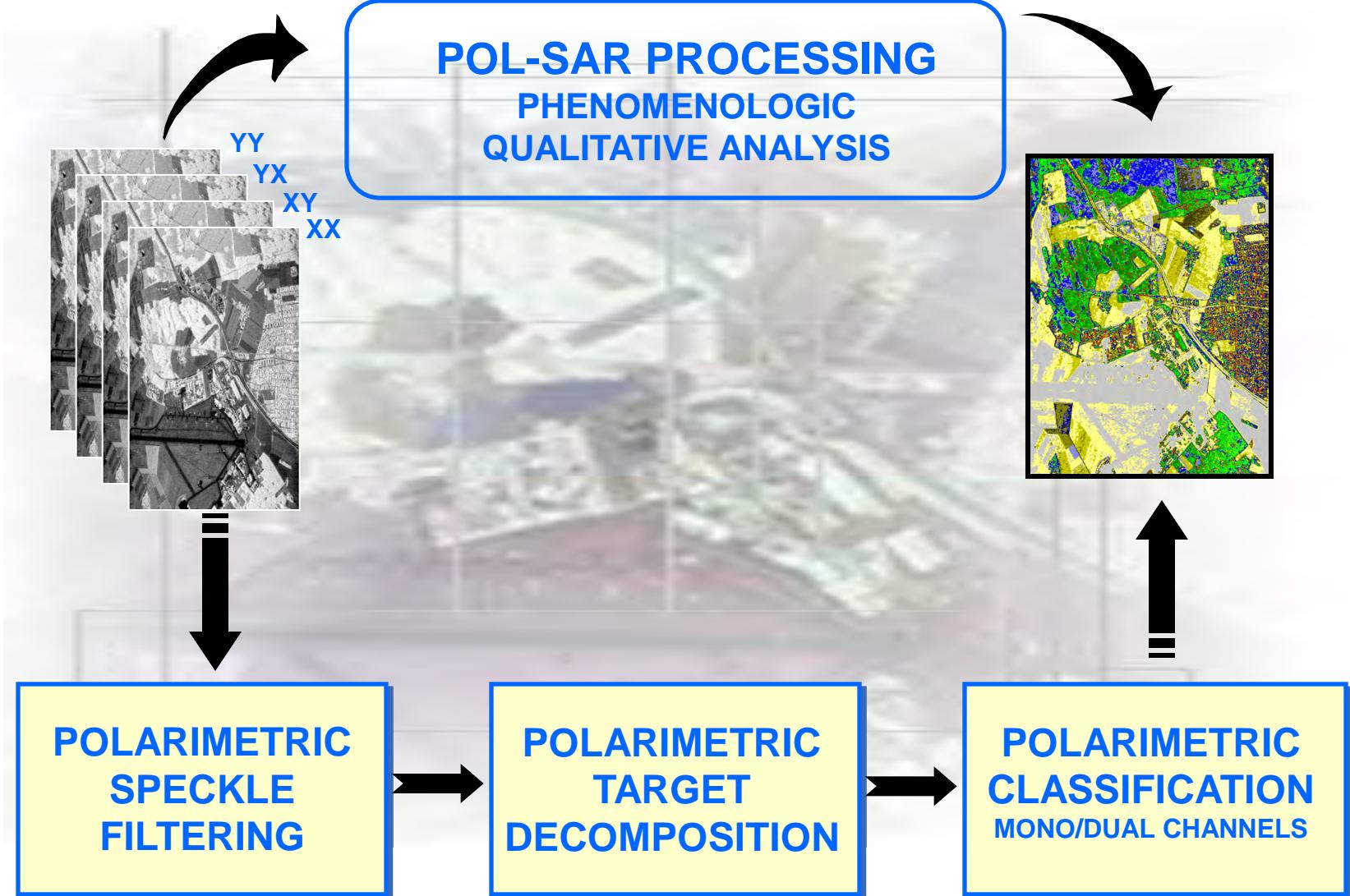


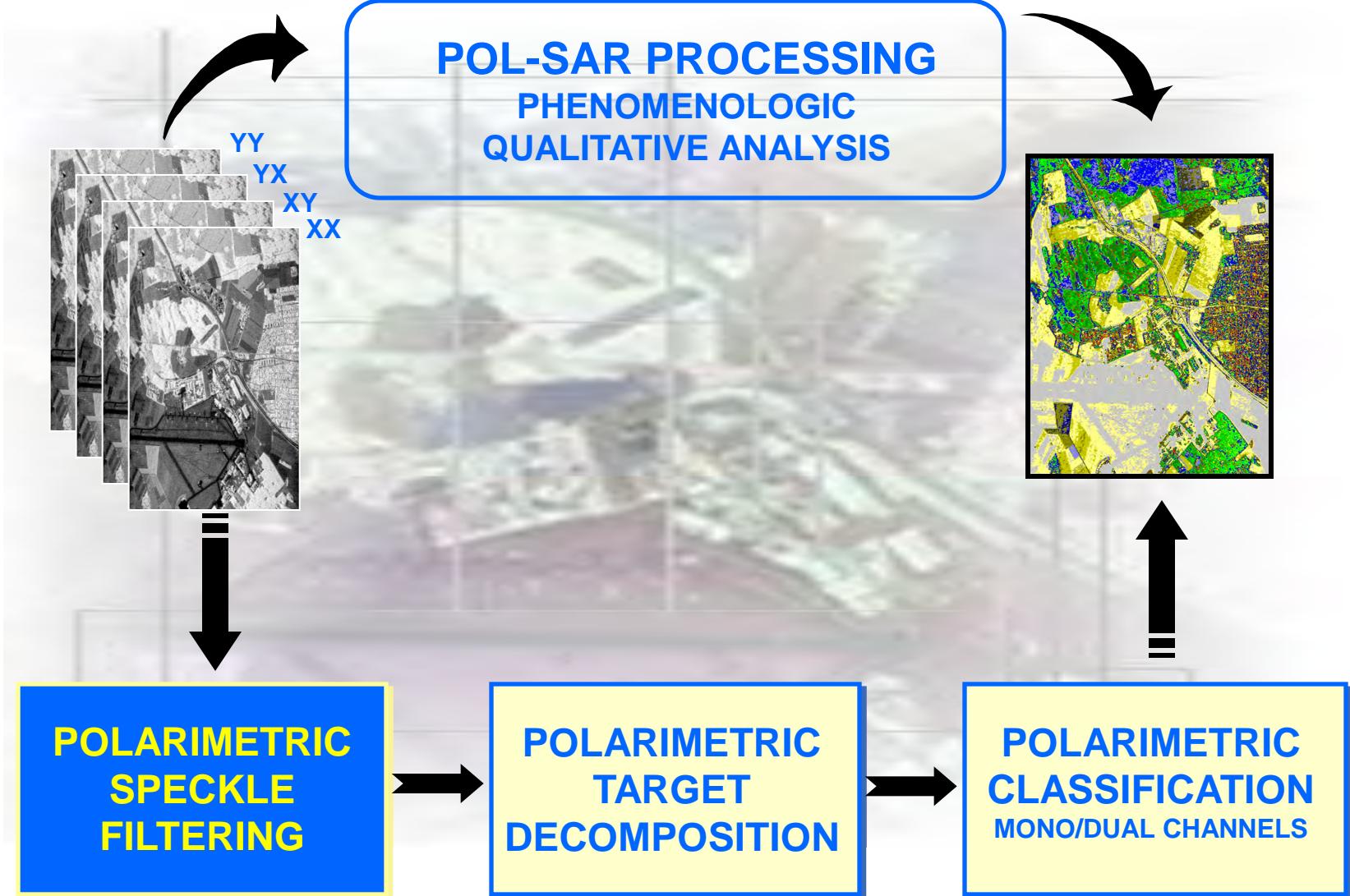
© Google Earth

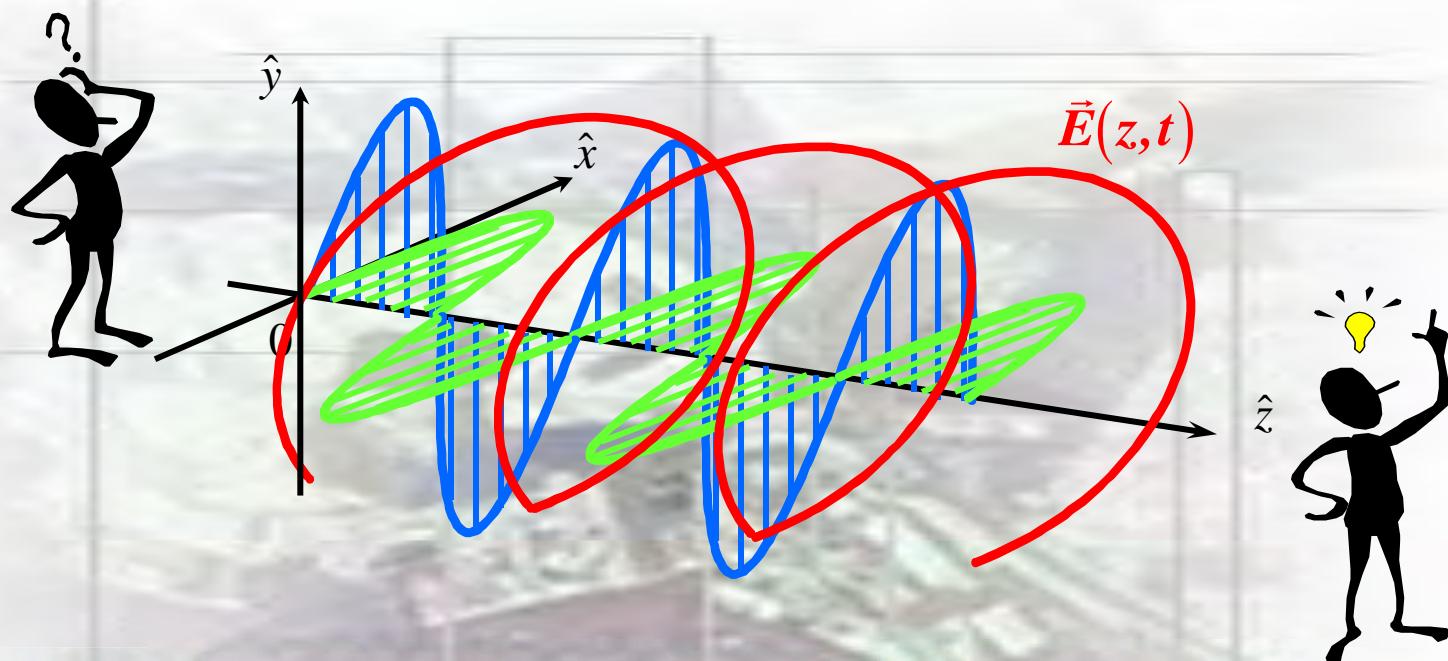




# POLARIMETRIC REMOTE SENSING



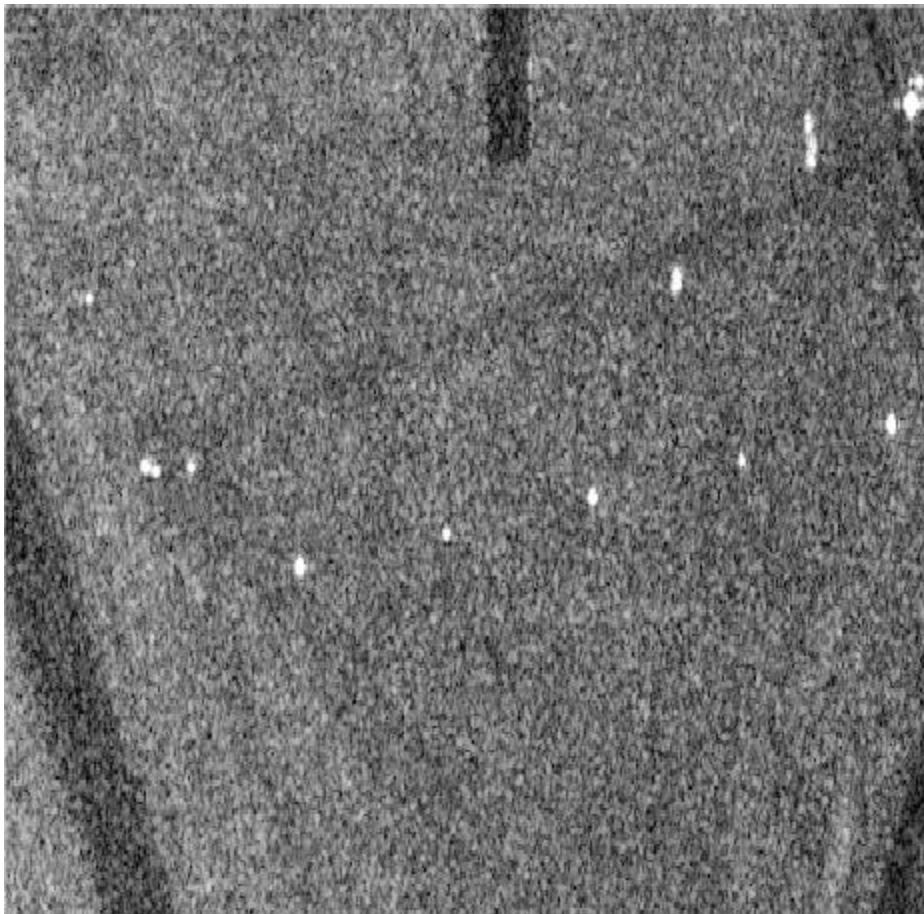




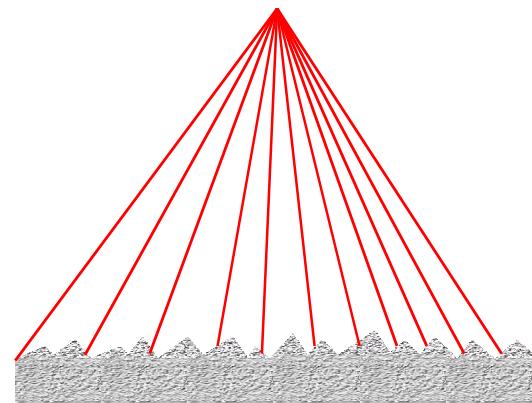
# POLARIMETRIC SPECKLE FILTERING

## An Introduction

# SPECKLE PHENOMENON



OBSERVATION POINT



SURFACE ROUGHNESS  
WAVELENGTH  
SCATTERING FROM DISTRIBUTED  
SCATTERERS

COHERENT INTERFERENCES OF WAVES  
SCATTERED FROM MANY RANDOMLY  
DISTRIBUTED ELEMENTARY SCATTERERS  
INSIDE THE RESOLUTION CELL

GRANULAR NOISE

SPECKLE PHENOMENON

# SPECKLE FILTERING

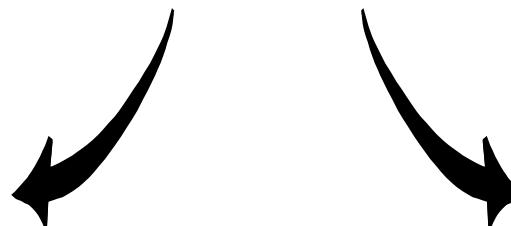
## SPECKLE PHENOMENON



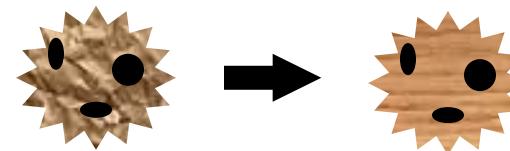
## DISTORTION OF THE INTERPRETATION



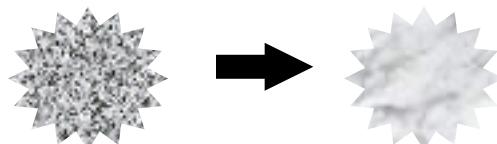
### SPECKLE FILTERING



### HETEROGENEOUS AREA

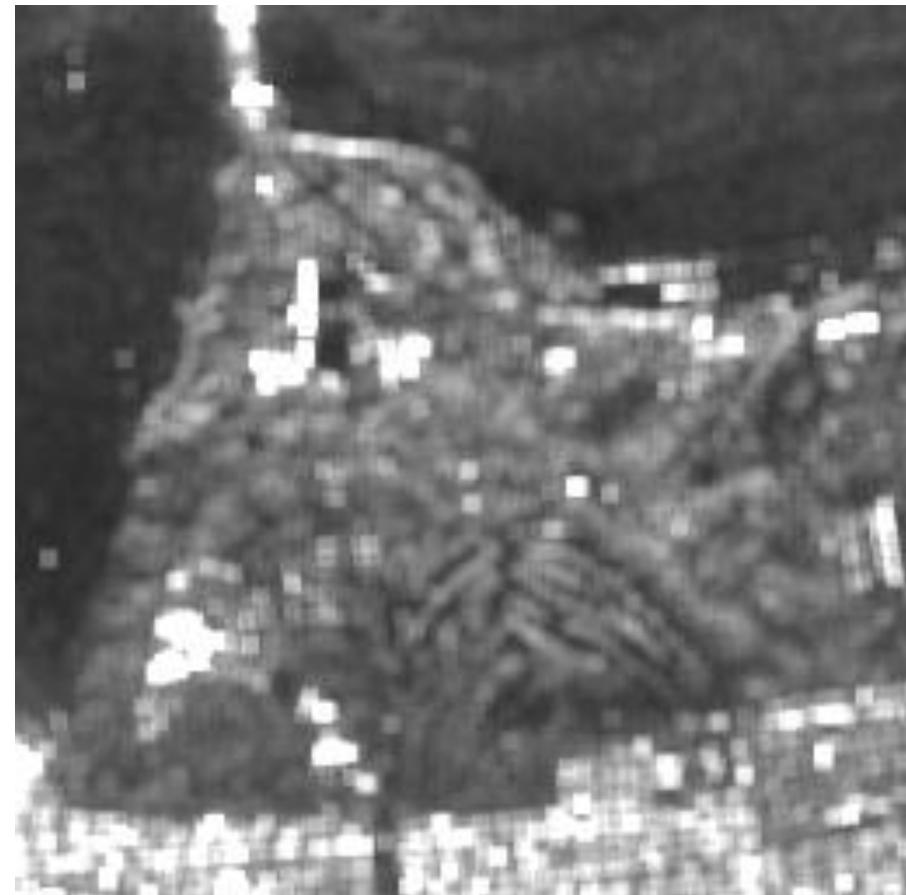


### HOMOGENEOUS AREA



### SPECKLE REDUCTION (RADIOMETRIC RESOLUTION)

### DETAILS PRESERVATION (SPATIAL RESOLUTION)



**SAN FRANCISCO BAY JPL - AIRSAR L-band 1988**

**BoxCar Filter**



## SAN FRANCISCO BAY JPL - AIRSAR L-band 1988

J.S. Lee, M.R. Grunes and G. De Grandi, "Polarimetric SAR Speckle Filtering and Its Impact on Terrain Classification" *IEEE TGRS*, September 1999



## SAN FRANCISCO BAY JPL - AIRSAR L-band 1988

J.S. Lee, D.L. Schuler, T.L. Ainsworth, M.R. Grunes, E Pottier, L. Ferro-Famil, "Scattering Model Based Speckle Filtering of Polarimetric SAR Data" IEEE – TGRS, vol 1, January 2006



## SAN FRANCISCO BAY JPL - AIRSAR L-band 1988

J.S. Lee, J.H. Wen, T.L. Ainsworth, K.S. Chen, A.J. Chen, "Improved Sigma Filter for Speckle Filtering of SAR Imagery"  
IEEE – TGRS, vol 1, January 2009

# SPECKLE FILTERING



AVERAGING DATA



SECOND ORDER  
STATISTICS

COHERENCY MATRICES



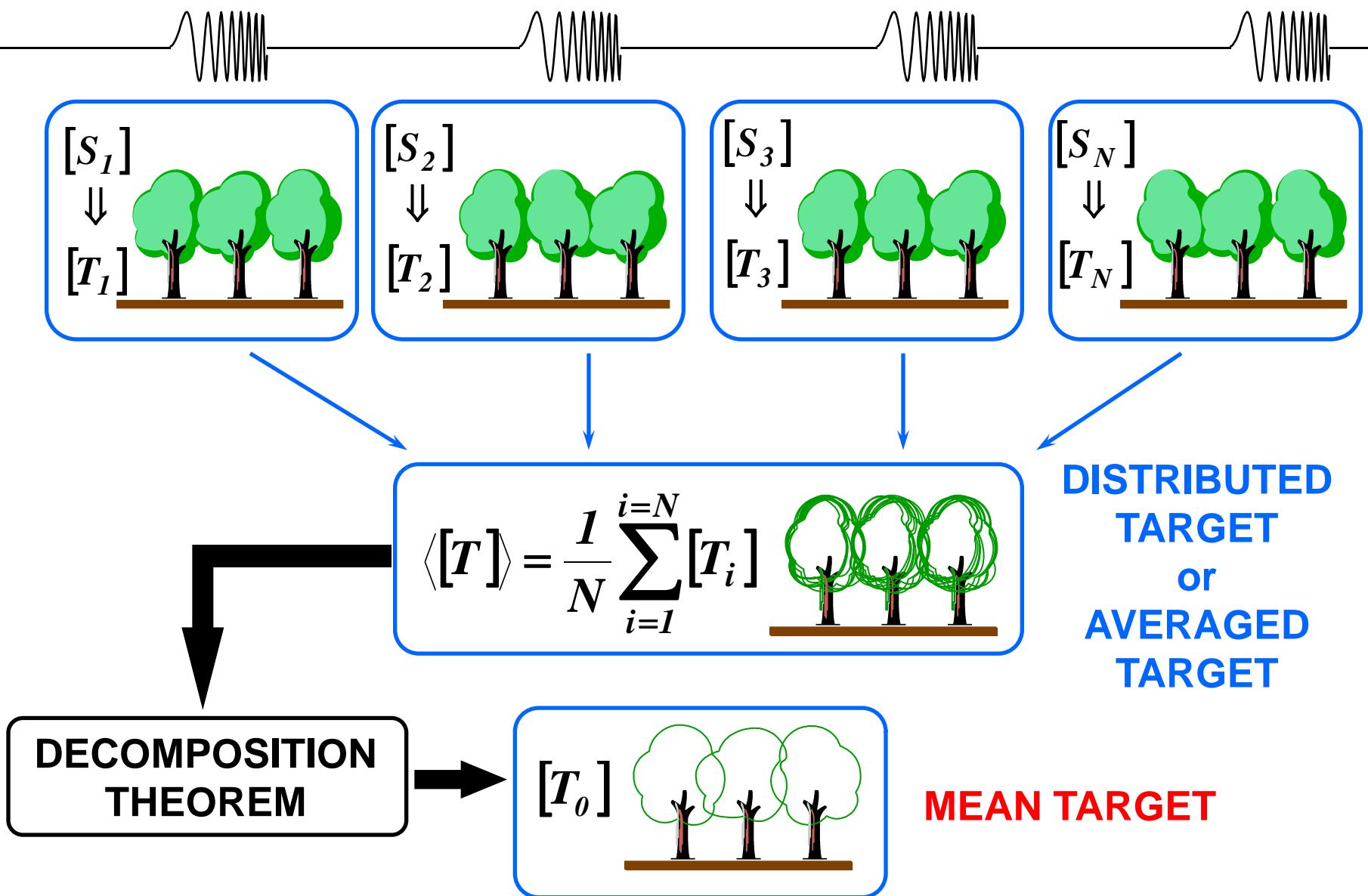
SMOOTHING AVERAGING

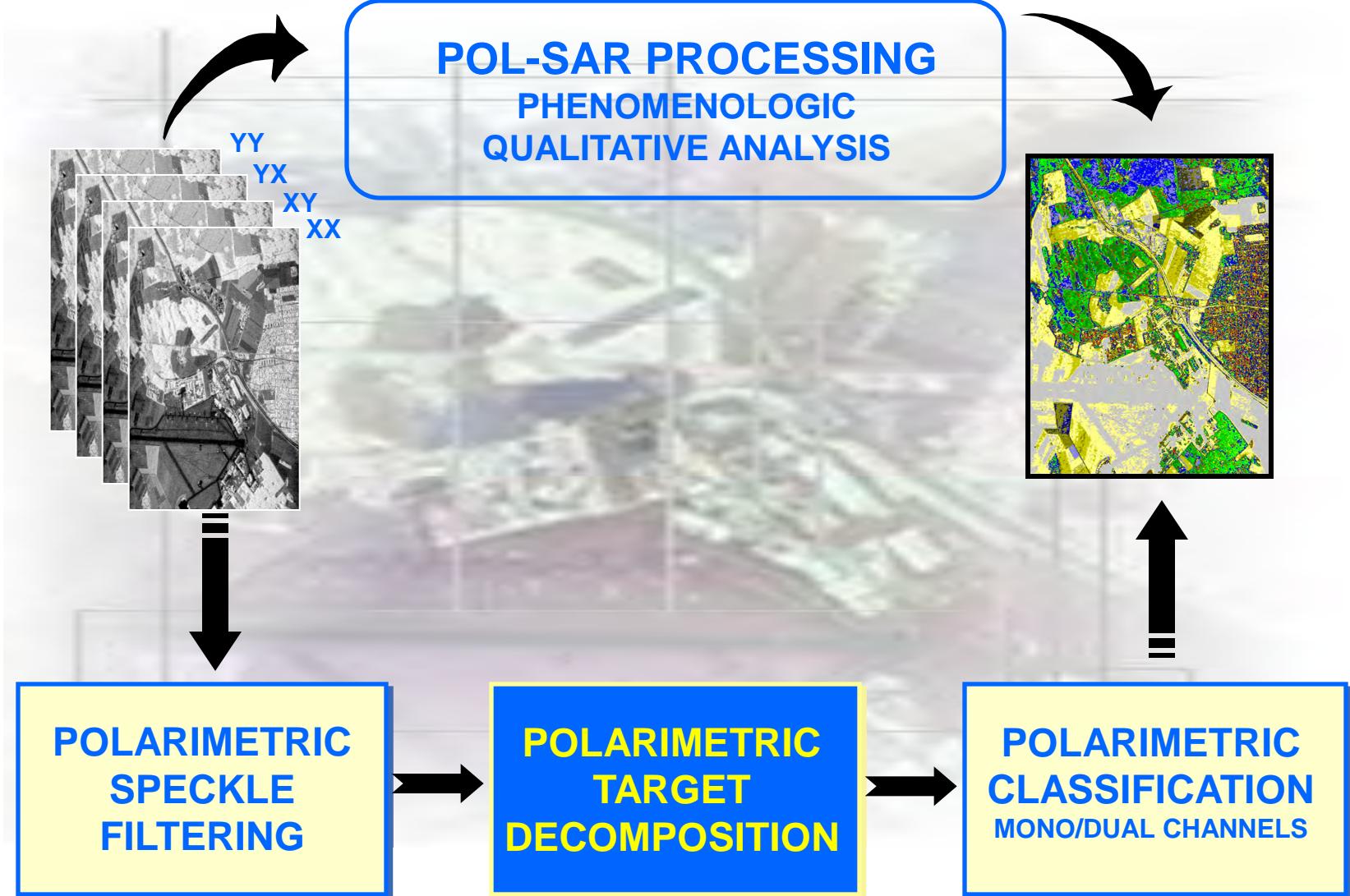


$$[T] = \underline{k} \underline{k}^* {}^T$$

$$\langle [T] \rangle = \frac{1}{N} \sum_{i=1}^N \underline{k}_i \underline{k}_i^* {}^T$$

CONCEPT OF THE DISTRIBUTED TARGET

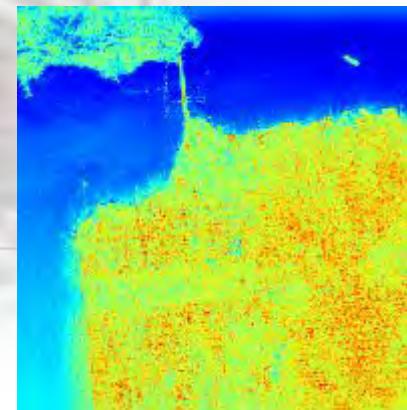
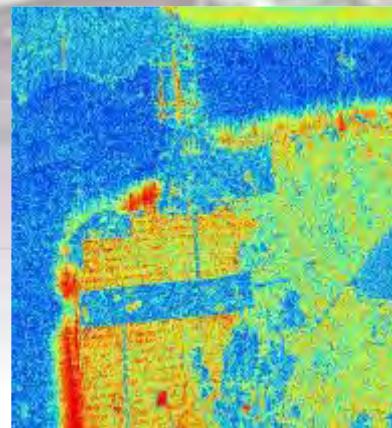
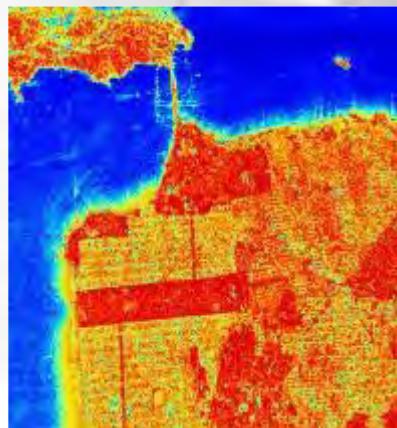




**[S]****COHERENT  
DECOMPOSITION**E. KROGAGER  
(1990)W.L. CAMERON  
(1990)**[K]****TARGET  
DICHOTOMY**J.R. HUYNEN  
(1970)R.M. BARNES  
(1988)**[T]****EIGENVECTORS BASED  
DECOMPOSITION**S.R. CLOUDE  
(1985)W.A. HOLM  
(1988)S.R. CLOUDE - E. POTTIER  
(1996-1997)**[C]****AZIMUTHAL SYMMETRY****MODEL BASED  
DECOMPOSITION**A.J. FREEMAN – S.L. DURDEN (1992)  
Y. YAMAGUSHI (2005 - 2012), AN (2010)**EIGENVECTORS / EIGENVALUES ANALYSIS  
&  
MODEL BASED DECOMPOSITION**J.J. VAN ZYL (1992-2008), M. ARII (2010)  
TSVM (R. TOUZI – 2007)**EIGENVECTORS / EIGENVALUES ANALYSIS  
ENTROPY / ANISOTROPY**

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TSVM (R. TOUZI – 2007)**EIGENVECTORS / EIGENVALUES ANALYSIS  
ENTROPY / ANISOTROPY**

# THE H/A/ $\alpha$ POLARIMETRIC TARGET DECOMPOSITION THEOREM



S.R. CLOUDE - E. POTTIER (1995 - 1996)

→ 7th ADVANCED TRAINING COURSE ON LAND REMOTE SENSING

4–9 September 2017 | Szent István University | Gödöllő, Hungary

**TARGET VECTOR**

$$\underline{k} = \frac{1}{\sqrt{2}} [ S_{XX} + S_{YY} \quad S_{XX} - S_{YY} \quad 2S_{XY} ]^T$$

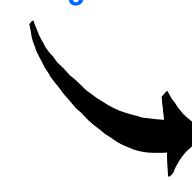
**LOCAL ESTIMATE OF  
THE COHERENCY MATRIX**

$$\langle [T] \rangle = \frac{1}{N} \sum_{i=1}^N \underline{k}_i \cdot \underline{k}_i^{*T} = \frac{1}{N} \sum_{i=1}^N [T_i]$$

**EIGENVECTORS / EIGENVALUES ANALYSIS**

$$\langle [T] \rangle = [\underline{U}_3] [\Sigma] [\underline{U}_3]^{-1} = \begin{bmatrix} & & \\ \underline{u}_1 & \underline{u}_2 & \underline{u}_3 \\ & & \end{bmatrix} \begin{bmatrix} \lambda_1 & 0 & 0 \\ 0 & \lambda_2 & 0 \\ 0 & 0 & \lambda_3 \end{bmatrix} \begin{bmatrix} & & \\ \underline{u}_1 & \underline{u}_2 & \underline{u}_3 \\ & & \end{bmatrix}^{*T}$$

ORTHOGONAL EIGENVECTORS      REAL EIGENVALUES  
 $\lambda_1 > \lambda_2 > \lambda_3$



$$P_i = \frac{\lambda_i}{\sum_{k=1}^3 \lambda_k}$$

$$\langle [T] \rangle = [\mathbf{U}_3] [\Sigma] [\mathbf{U}_3]^{-1} = \begin{bmatrix} & & \\ \underline{u}_1 & \underline{u}_2 & \underline{u}_3 \end{bmatrix} \begin{bmatrix} \lambda_1 & 0 & 0 \\ 0 & \lambda_2 & 0 \\ 0 & 0 & \lambda_3 \end{bmatrix} \begin{bmatrix} & & \\ \underline{u}_1 & \underline{u}_2 & \underline{u}_3 \end{bmatrix}^{*T}$$

ORTHOGONAL  
EIGENVECTORS

REAL EIGENVALUES  
 $\lambda_1 > \lambda_2 > \lambda_3$



### PARAMETERISATION OF THE SU(3) UNITARY MATRIX

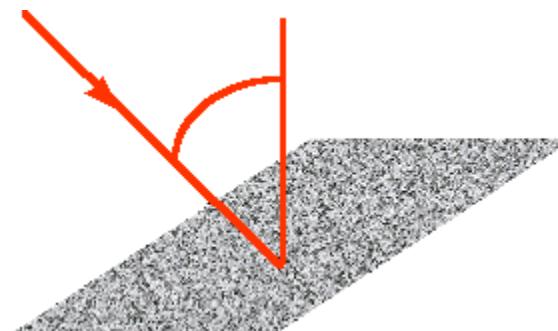
$$[\mathbf{U}_3] = \begin{bmatrix} \cos \alpha_1 e^{j\phi_1} & \cos \alpha_2 e^{j\phi_2} & \cos \alpha_3 e^{j\phi_3} \\ \sin \alpha_1 \cos \beta_1 e^{j\phi_1} e^{j\delta_1} & \sin \alpha_2 \cos \beta_2 e^{j\phi_2} e^{j\delta_2} & \sin \alpha_3 \cos \beta_3 e^{j\phi_3} e^{j\delta_3} \\ \sin \alpha_1 \sin \beta_1 e^{j\phi_1} e^{j\gamma_1} & \sin \alpha_2 \sin \beta_2 e^{j\phi_2} e^{j\gamma_2} & \sin \alpha_3 \sin \beta_3 e^{j\phi_3} e^{j\gamma_3} \end{bmatrix}$$

↓ TARGET 1      ↓ TARGET 2      ↓ TARGET 3

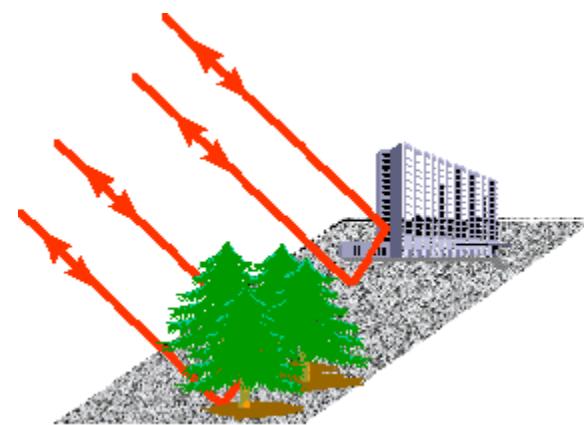
$$\underline{\alpha} = P_1 \alpha_1 + P_2 \alpha_2 + P_3 \alpha_3$$

## PHYSICAL INTERPRETATION

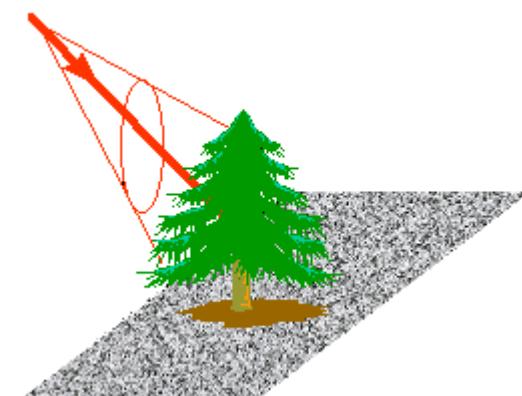
### SINGLE BOUNCE SCATTERING (ROUGH SURFACE)



### DOUBLE BOUNCE SCATTERING



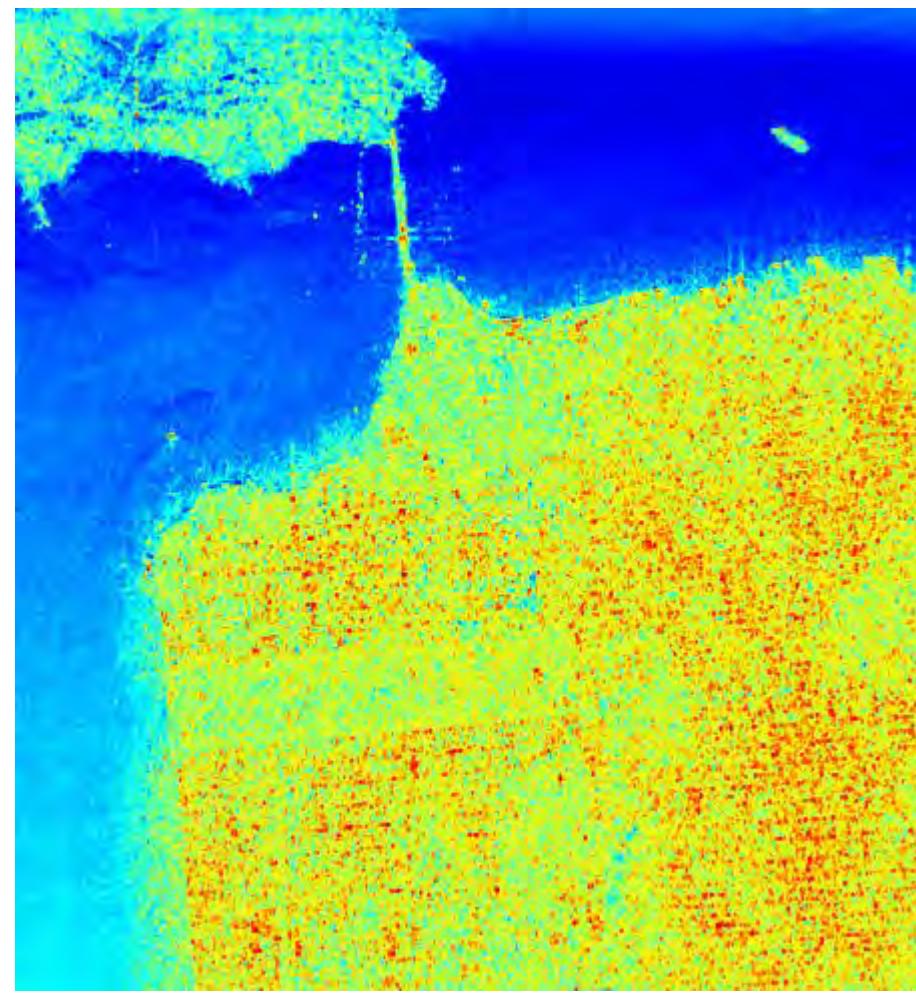
### VOLUME SCATTERING



$$\begin{aligned} a &\mapsto b \Rightarrow v \mapsto 0 \\ &\Downarrow \\ \underline{\alpha} &\mapsto 0 \end{aligned}$$

$$\begin{aligned} a &\mapsto -b \Rightarrow \varepsilon \mapsto 0 \\ &\Downarrow \\ \underline{\alpha} &\mapsto \frac{\pi}{2} \end{aligned}$$

$$\begin{aligned} a &\gg b \Rightarrow \varepsilon \approx v \\ &\Downarrow \\ \underline{\alpha} &\mapsto \frac{\pi}{4} \end{aligned}$$

 $2A_0$  $B_0 + B$  $B_0 - B$ 

0

45°

90°

 $\underline{\alpha}$  PARAMETER

EIGENVALUES  $\lambda_1 \ \lambda_2 \ \lambda_3$  : ROLL INVARIANT

PROBABILITIES  $P_1 \ P_2 \ P_3$  : ROLL INVARIANT



## ENTROPY

(DEGREE OF RANDOMNESS  
STATISTICAL DISORDER)

$$H = - \sum_{i=1}^3 P_i \log_3(P_i)$$



### PURE TARGET

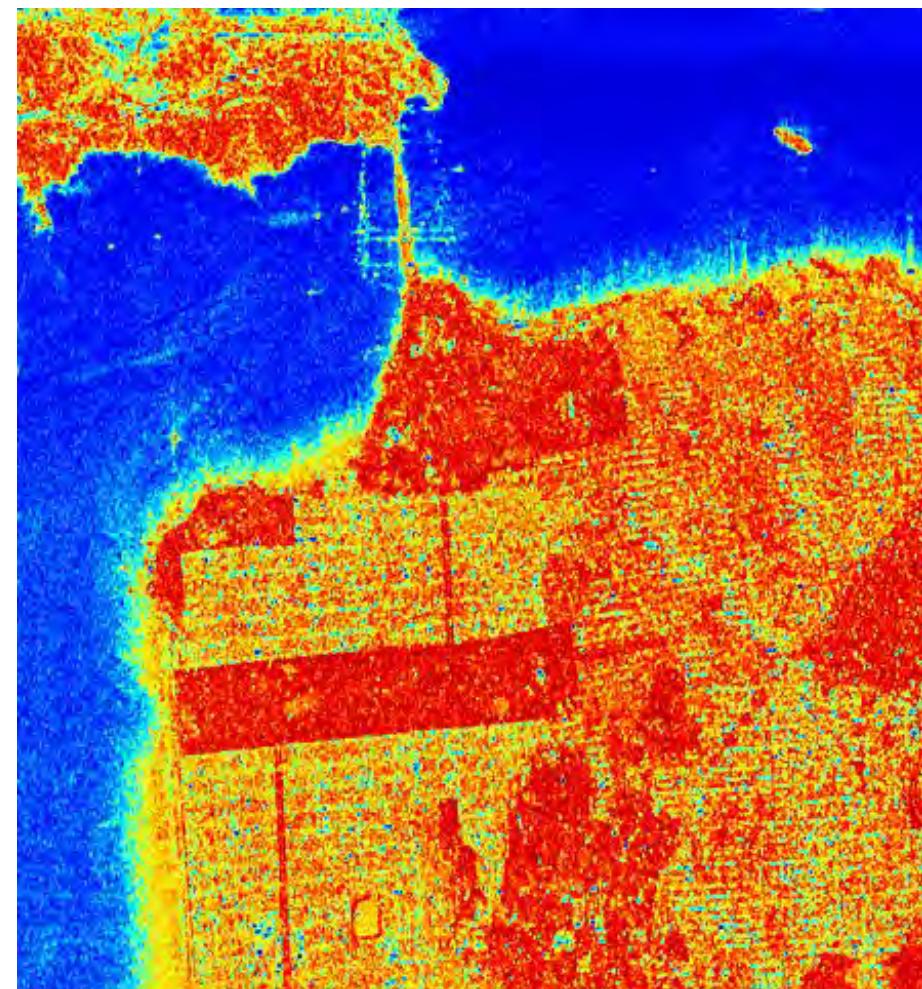
$$\lambda_1 = SPAN \quad \lambda_2 = 0 \quad \lambda_3 = 0$$

$$H = 0$$

### DISTRIBUTED TARGET

$$\lambda_1 = \lambda_2 = \lambda_3 = SPAN / 3$$

$$H = 1$$

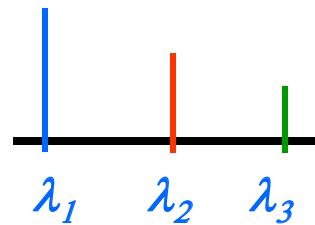
 $2A_0$  $B_0 + B$  $B_0 - B$ 

DIFFICULT MECHANISM DISCRIMINATION WHEN :  $H > 0.7$

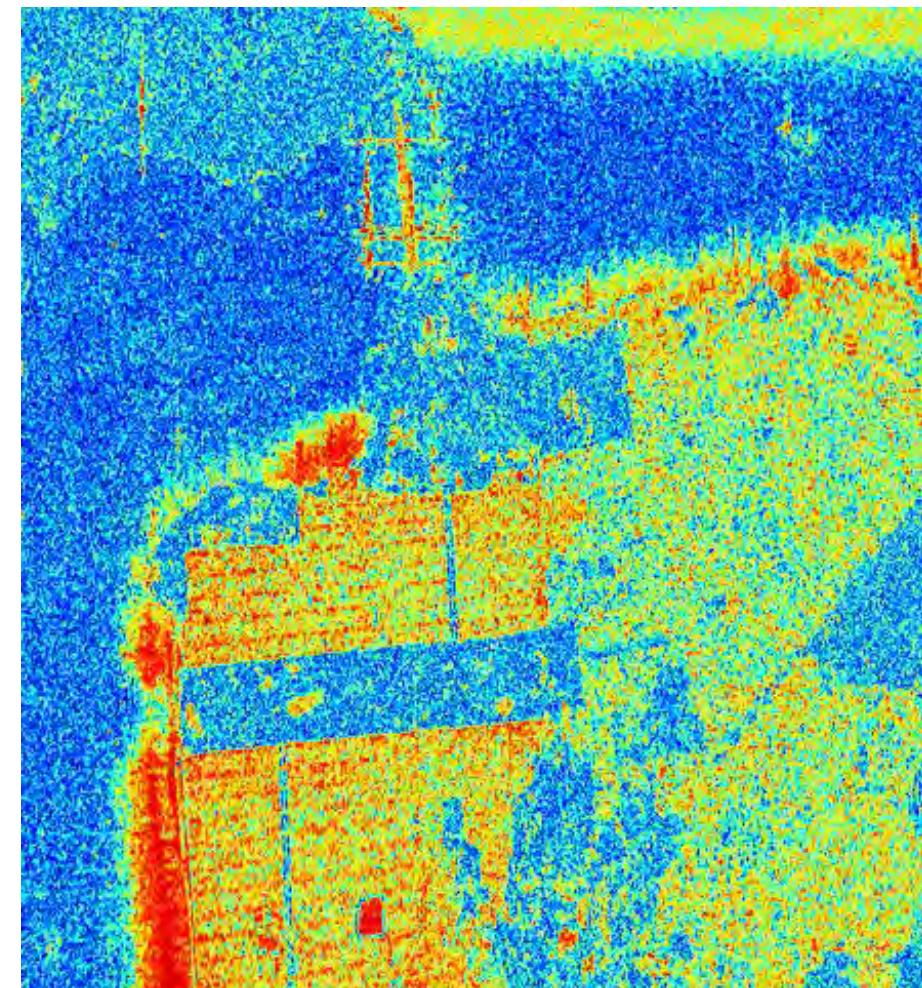


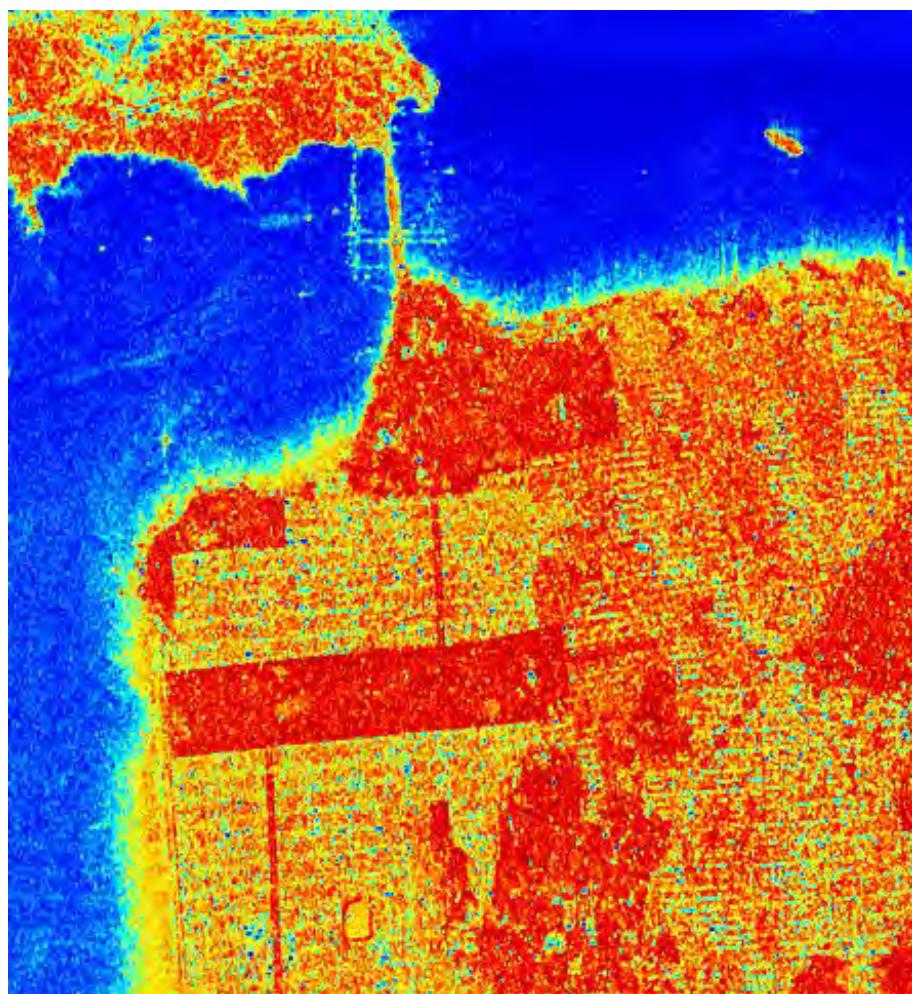
**ANISOTROPY**  
(EIGENVALUES SPECTRUM)

$$A = \frac{\lambda_2 - \lambda_3}{\lambda_2 + \lambda_3}$$



- **COMPLEMENTARY TO ENTROPY**
- **DISCRIMINATION WHEN  $H > 0.7$**
- **ROLL INVARIANT**

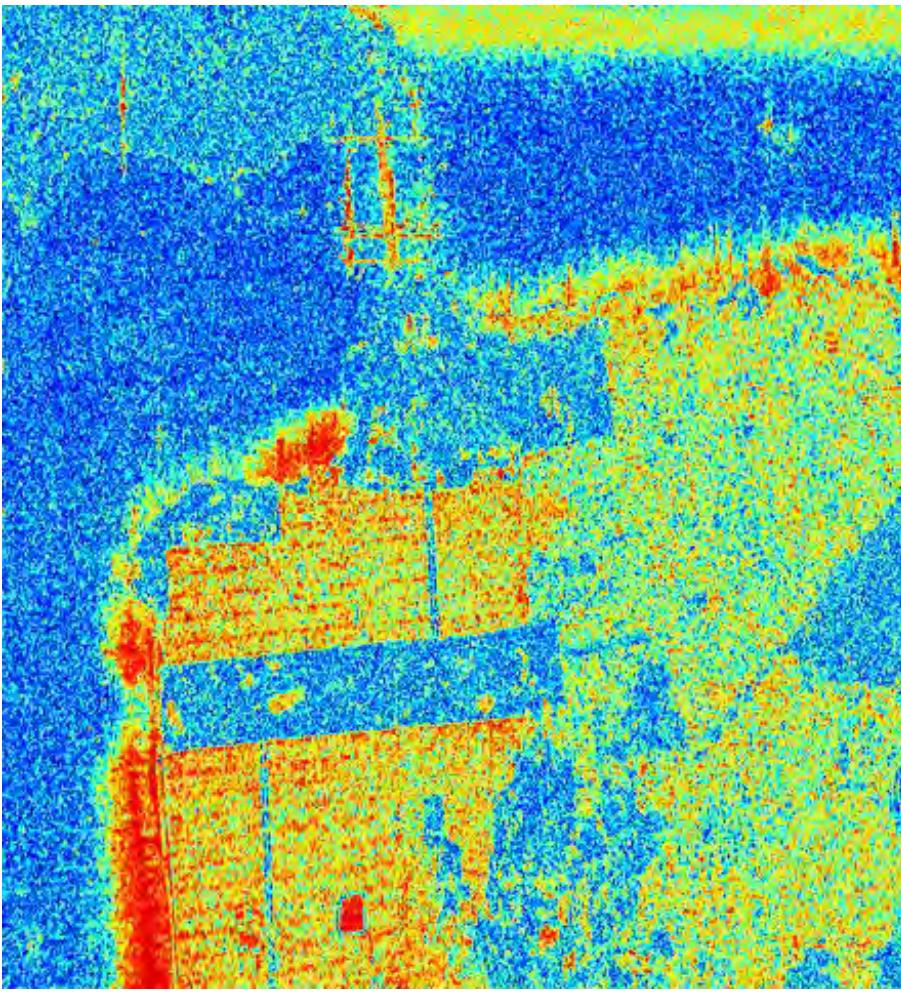
 $2A_0$  $B_0 + B$  $B_0 - B$ 



0

0.5

1.0

**ENTROPY (H)**

0

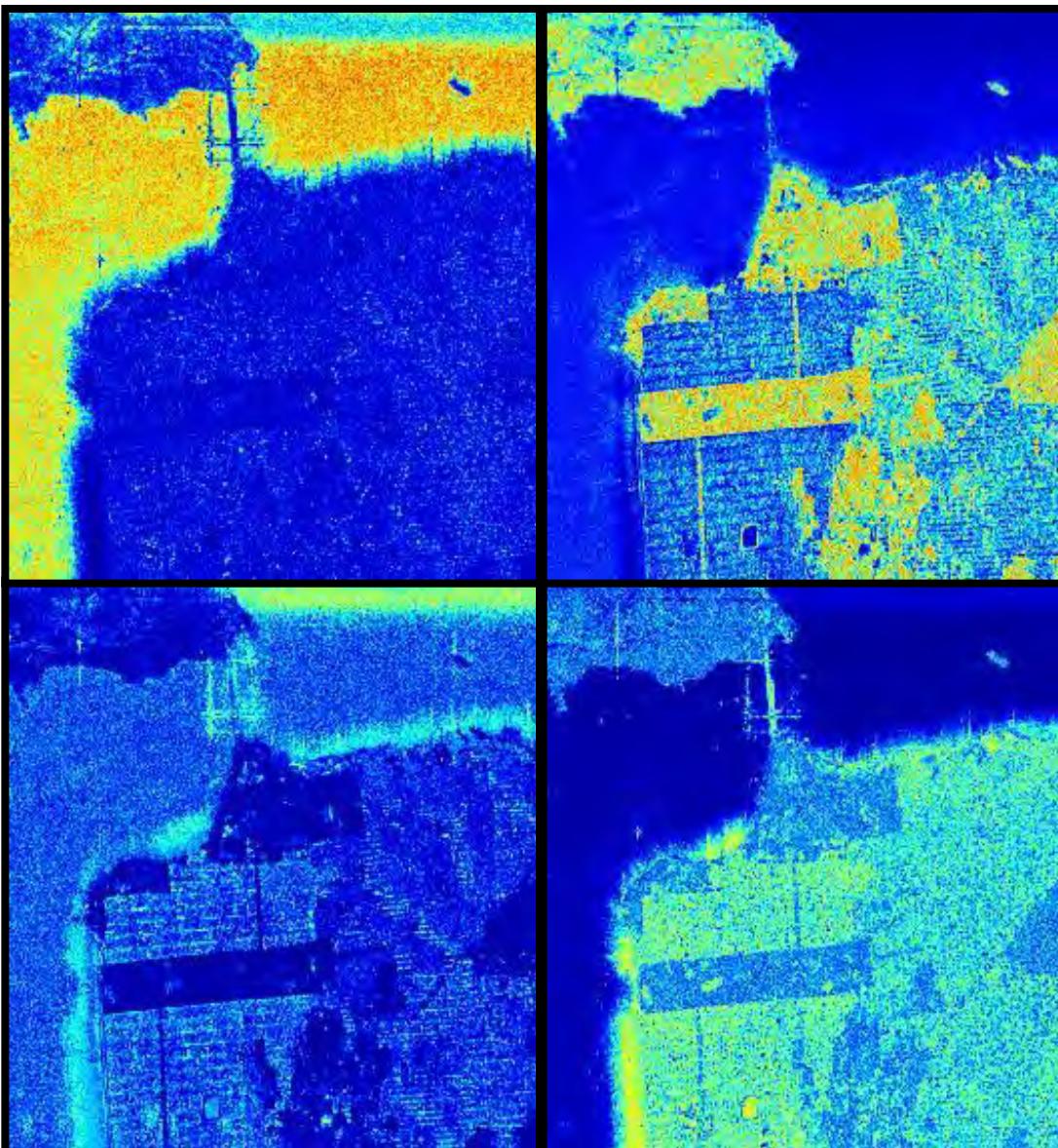
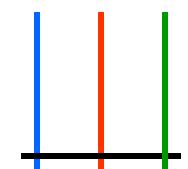
0.5

1.0

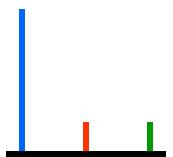
**ANISOTROPY (A)**

**(1-H)(1-A)**

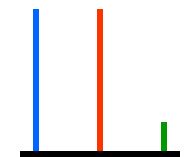
1 MECHANISM

**H(1-A)**

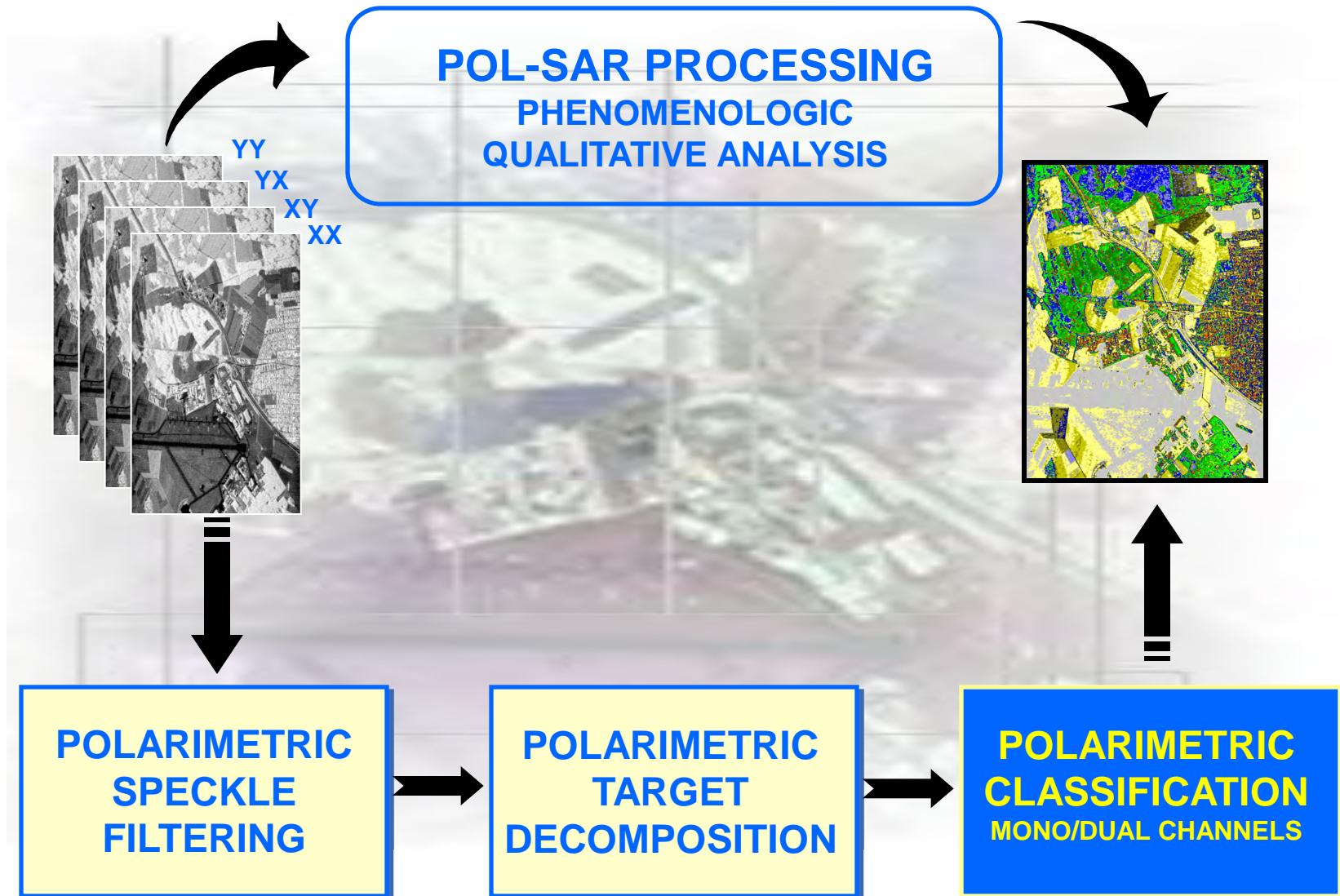
3 MECHANISMS

**A(1-H)**

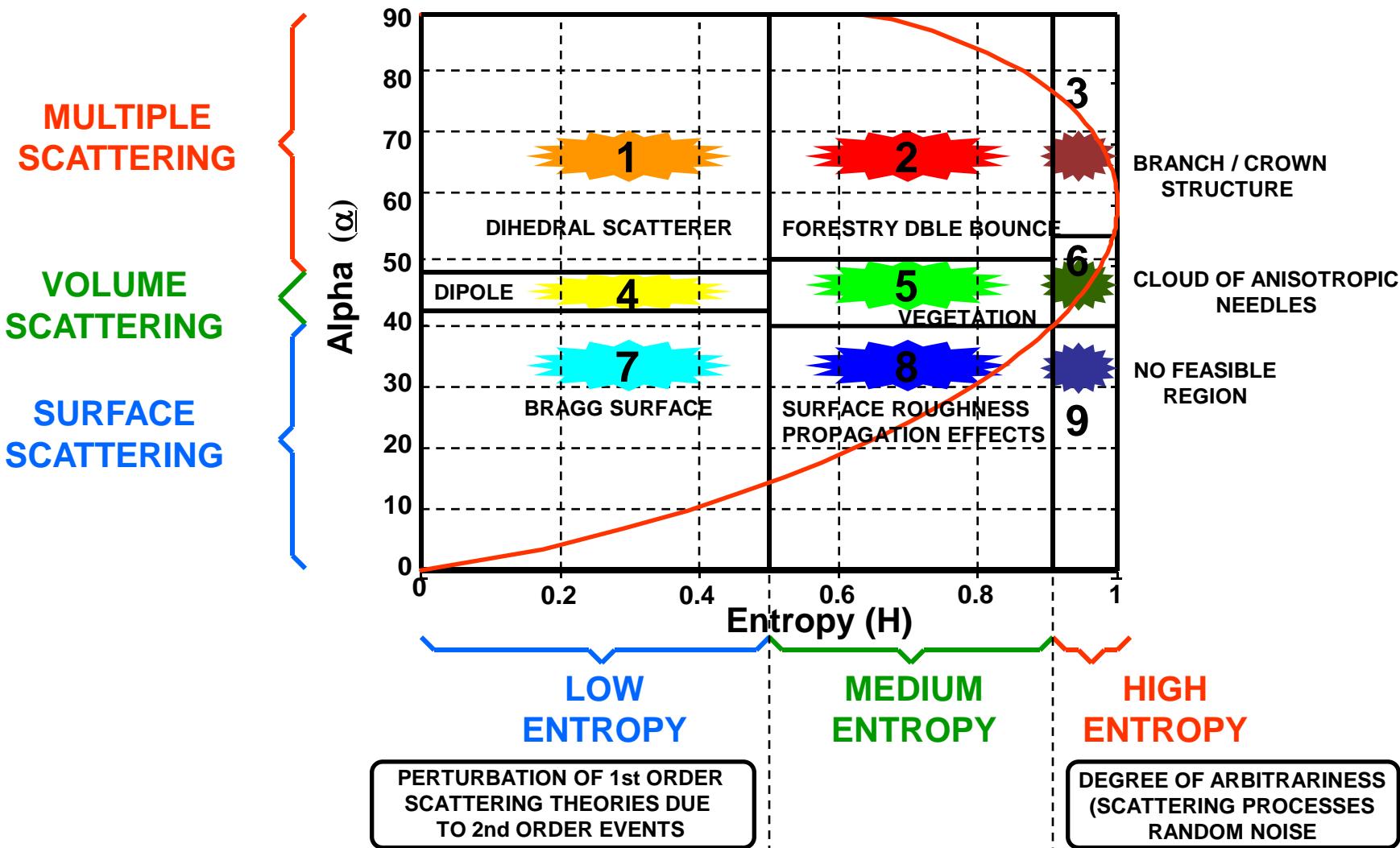
2 MECHANISMS

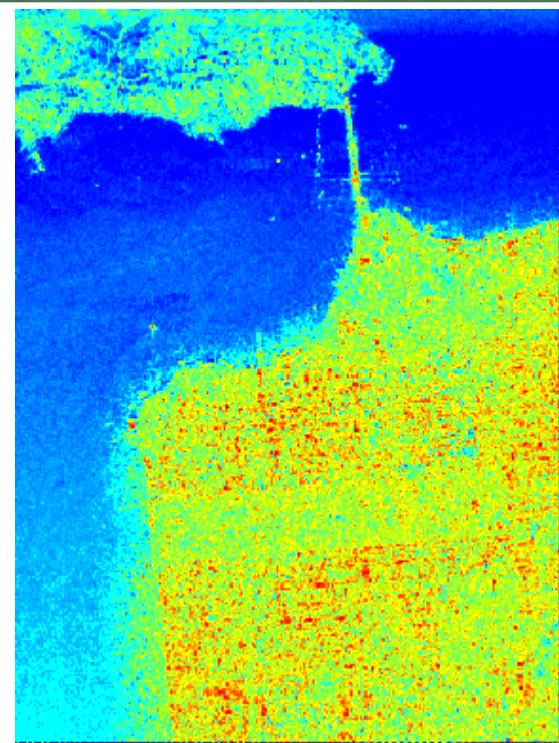
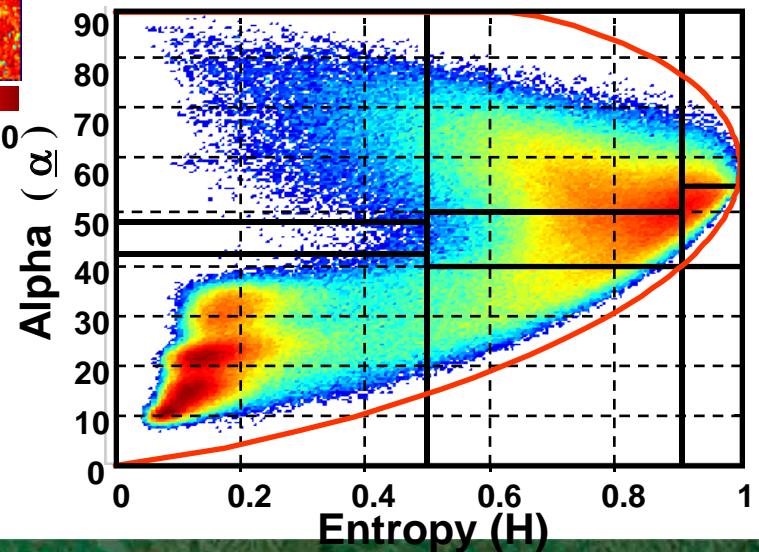
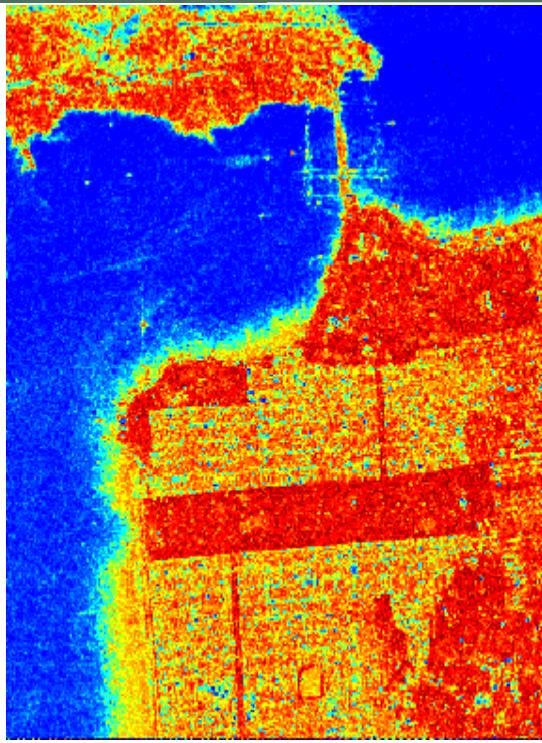
**HA**

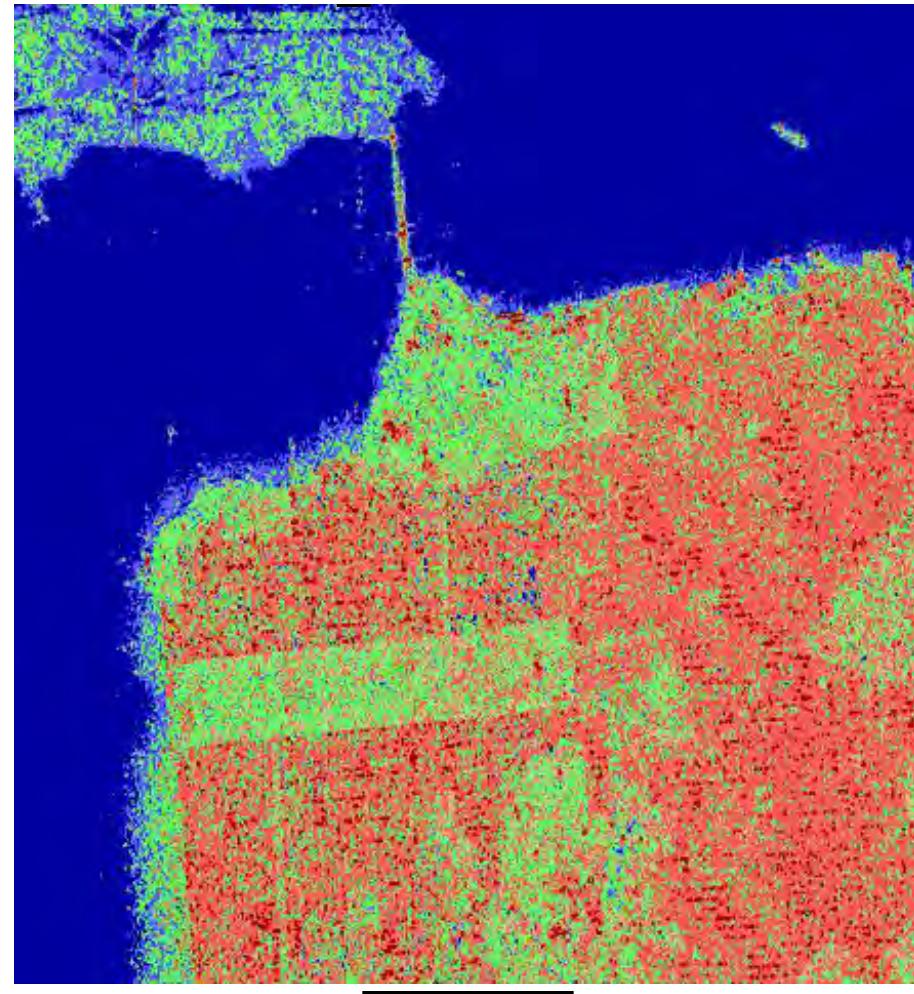
2 MECHANISMS



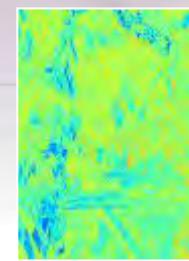
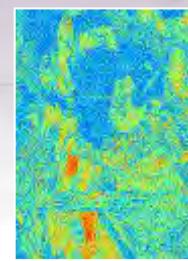
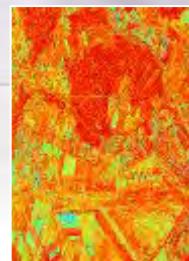
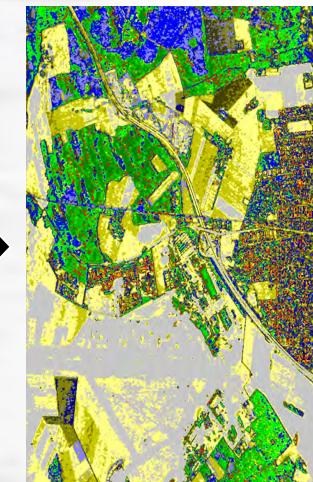
## SEGMENTATION OF THE $H/\alpha$ SPACE



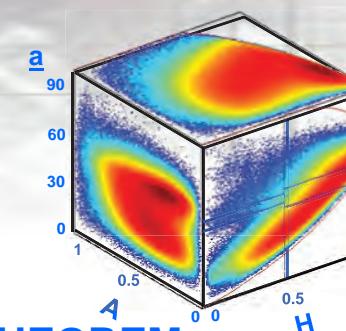


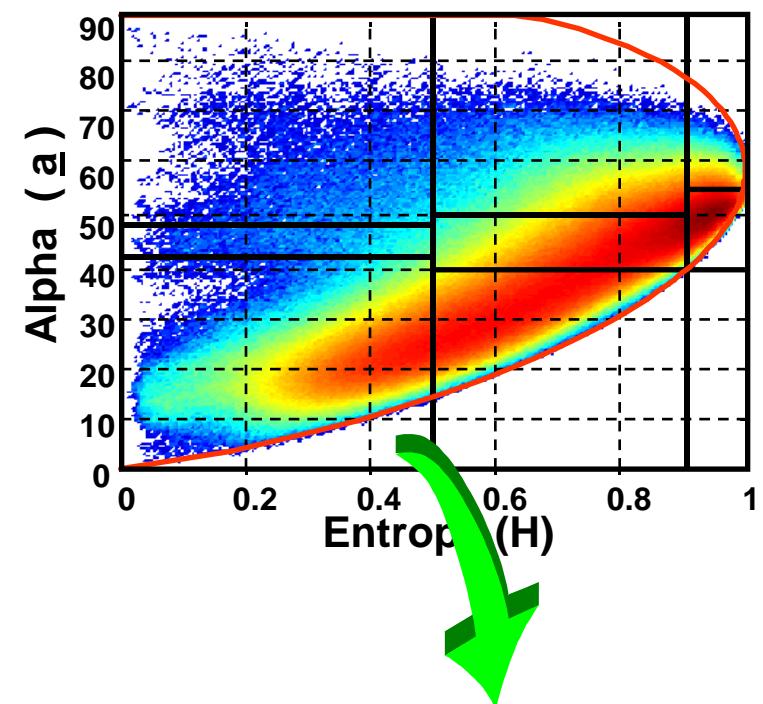
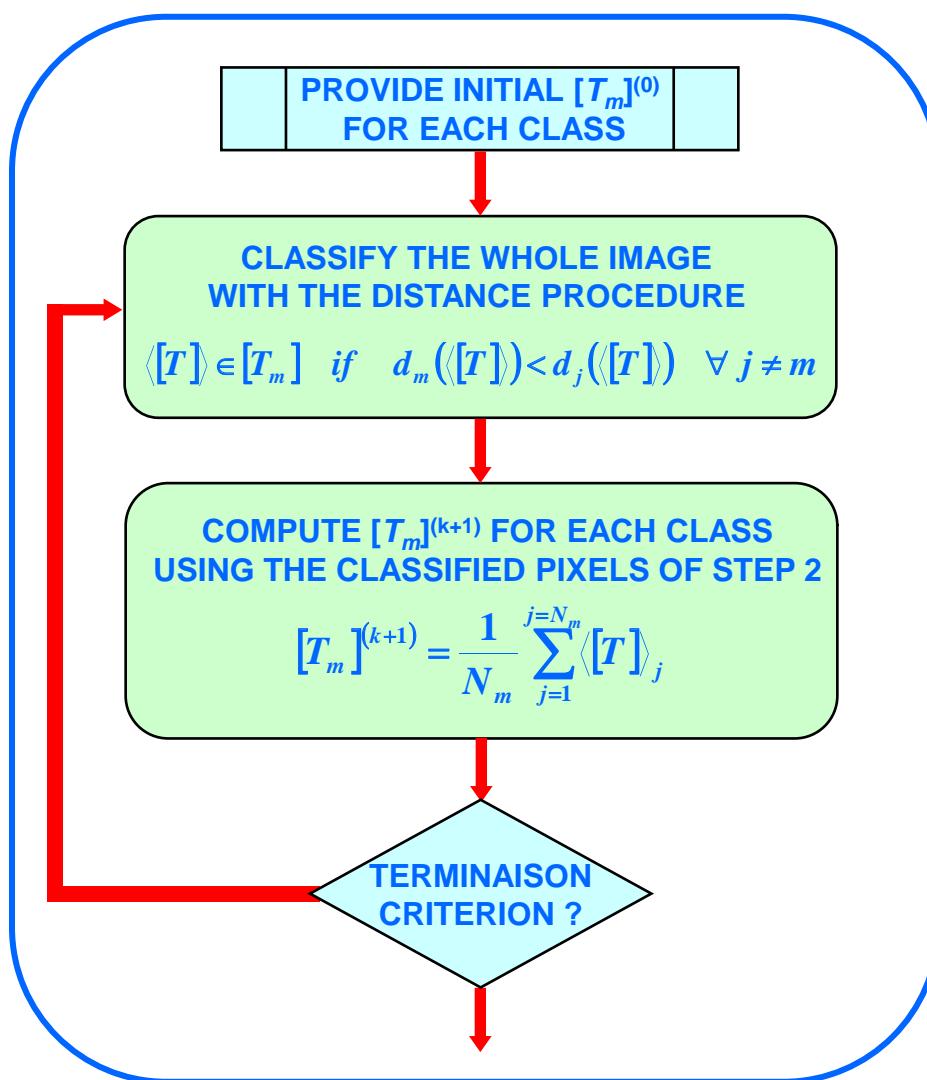
 $2A_0$  $B_0 + B$  $B_0 - B$ 

**WISHART PDF** 
$$P([\mathbf{T}]/[\mathbf{T}_m]) = \frac{L^{Lp} |[\mathbf{T}]|^{L-p} e^{-LTr([\mathbf{T}_m]^{-1}[\mathbf{T}])}}{\pi^{\frac{p(p-1)}{2}} \Gamma(L) \dots \Gamma(L-p+1) [\mathbf{T}_m]^L}$$



**H / A /  $\alpha$  DECOMPOSITION THEOREM**



**k - mean CLASSIFICATION PROCEDURE**

$$[T_m]^{(0)} = \frac{1}{N_m} \sum_{k=1}^{k=N_m} \langle [T] \rangle_k$$

**Cluster Center of the class  $m$  (Lee 1998)**

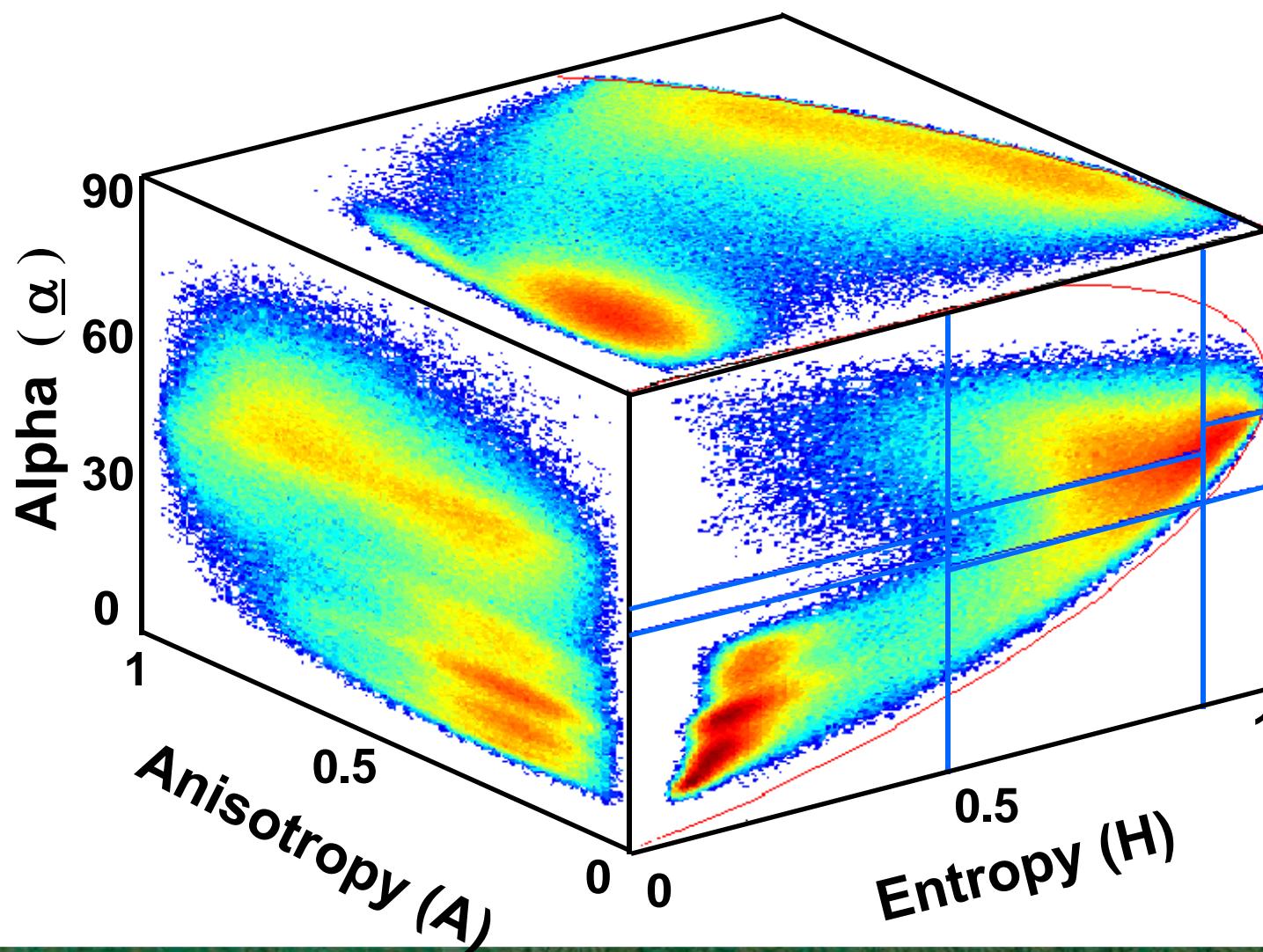
SAN FRANCISCO BAY JPL - AIRSAR L-band 1988



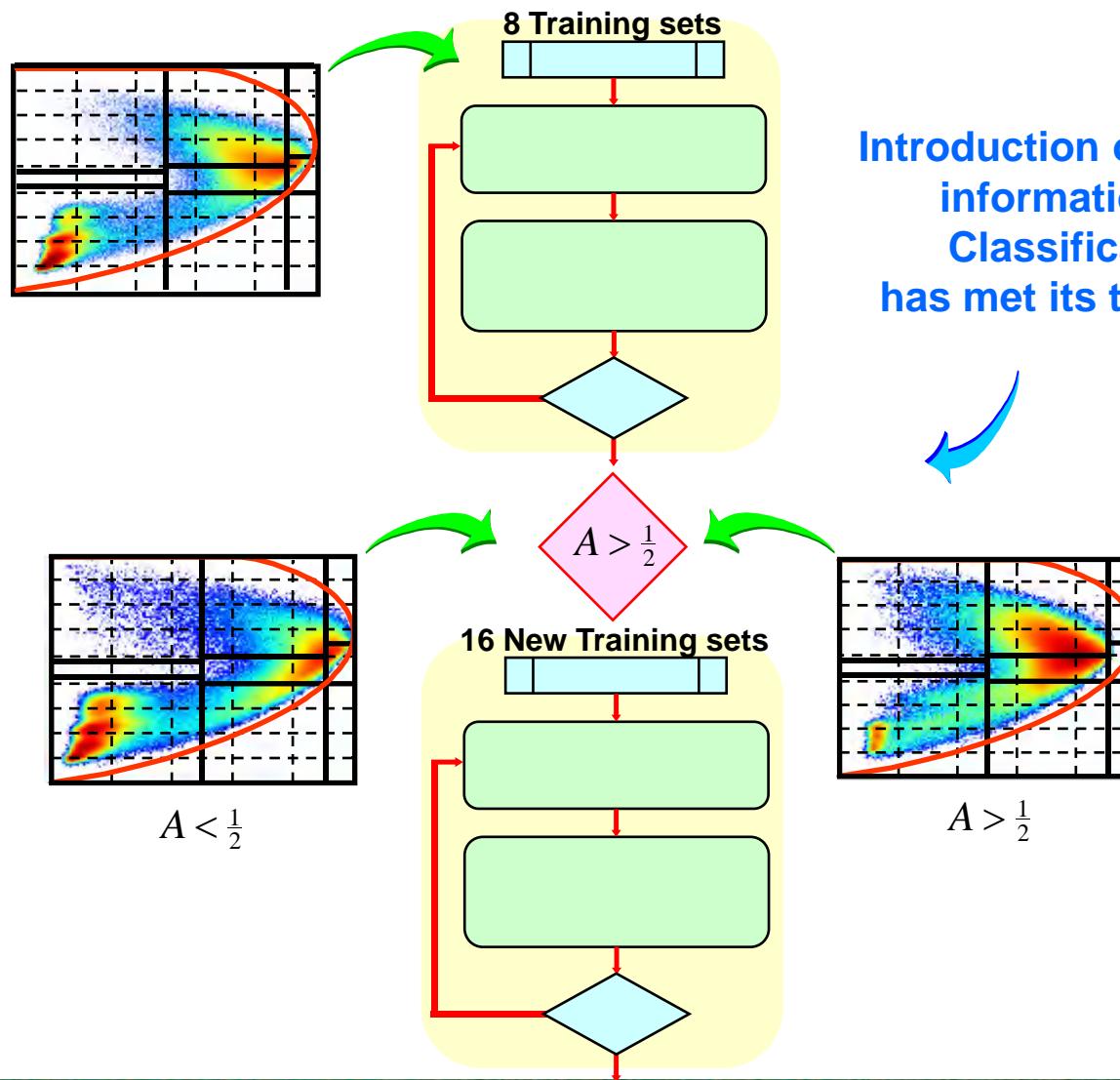
4th ITERATION

 $2A_0$  $B_0 + B$  $B_0 - B$ 

C1 C2 C3 C4 C5 C6 C7 C8

POLsar DATA DISTRIBUTION IN THE H / A /  $\underline{\alpha}$  SPACE

## 2 Successive k - mean Classification procedures

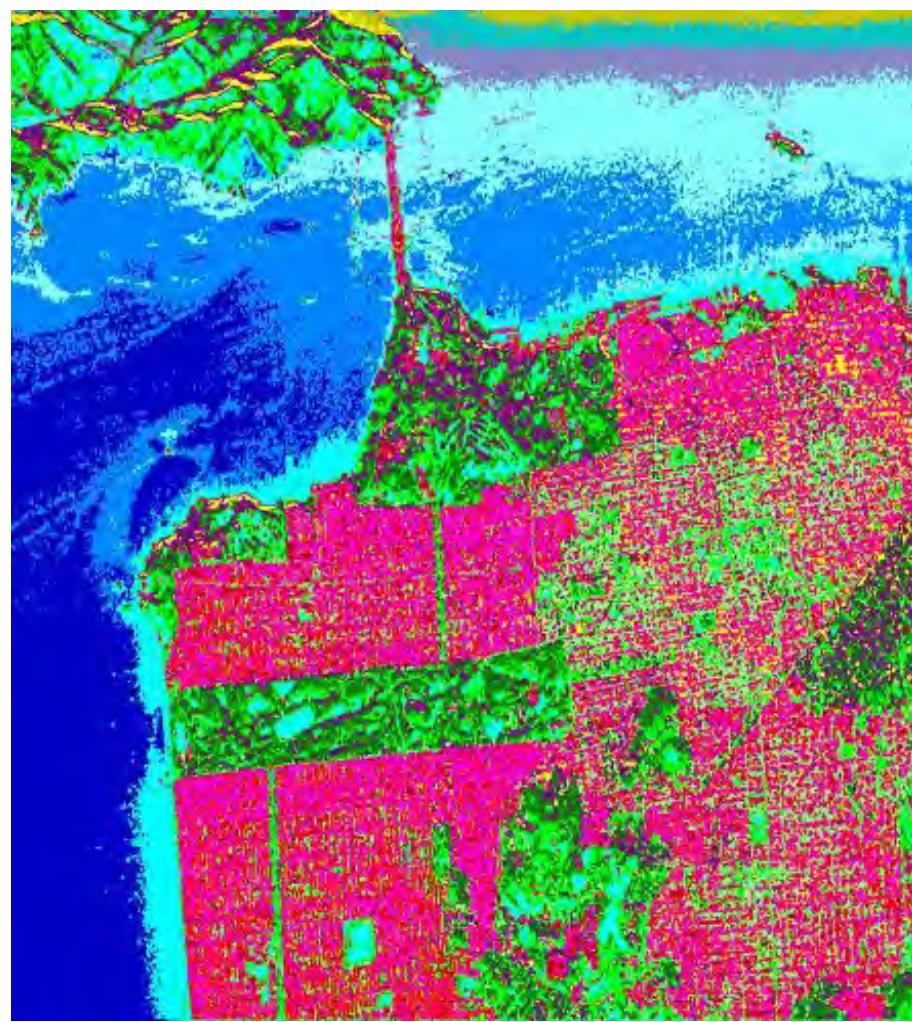


Introduction of the Anisotropy (A)  
information once the first  
Classification procedure  
has met its termination criterion

SAN FRANCISCO BAY JPL - AIRSAR L-band 1988



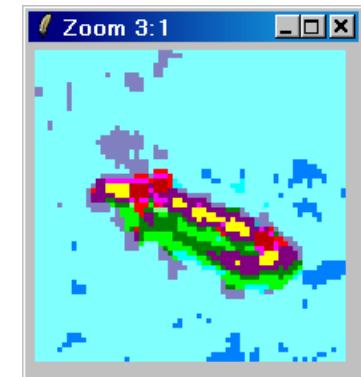
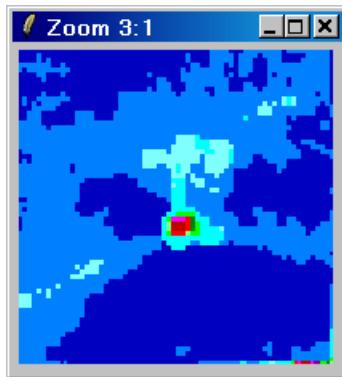
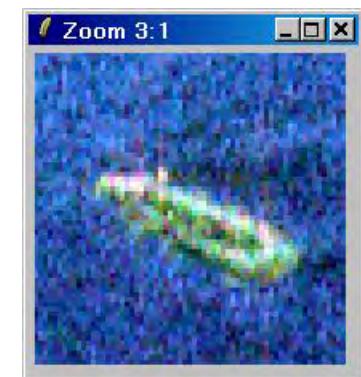
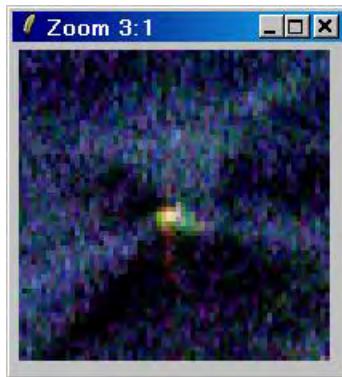
4th ITERATION

 $2A_0$  $B_0 + B$  $B_0 - B$ 

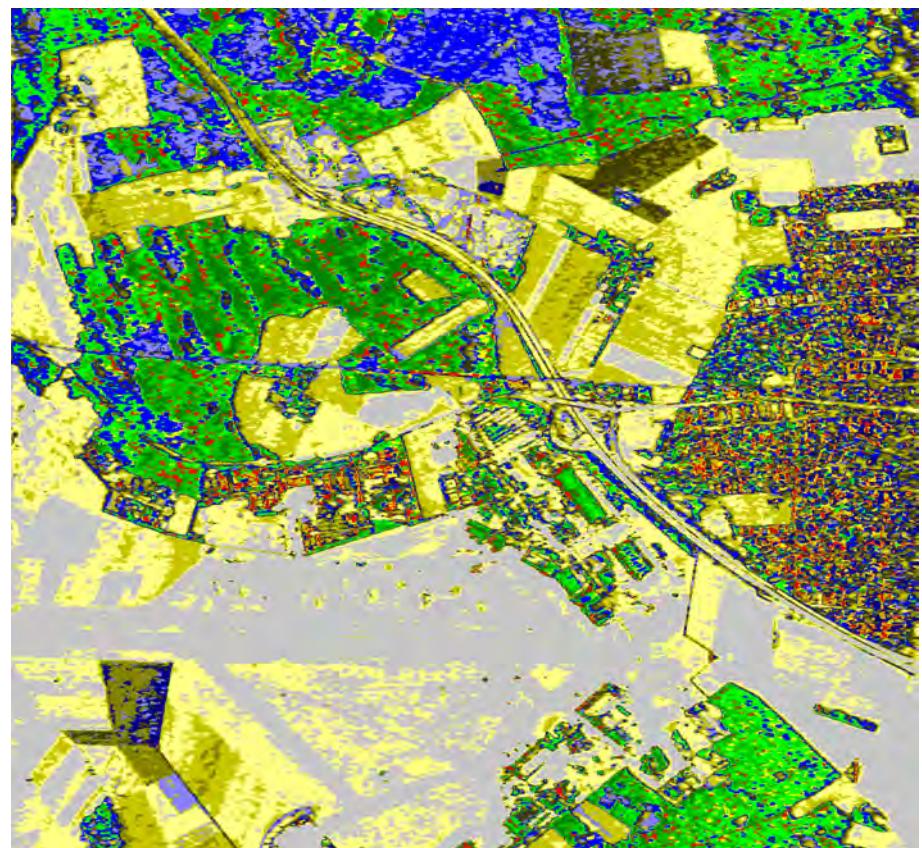
C1	C2	C3	C4	C5	C6	C7	C8
Red	Yellow	Blue	Orange	Green	Light Blue	Dark Green	Purple

→ 7th ADVANCED TRAINING COURSE ON LAND REMOTE SENSING

## SAN FRANCISCO BAY JPL - AIRSAR L-band 1988

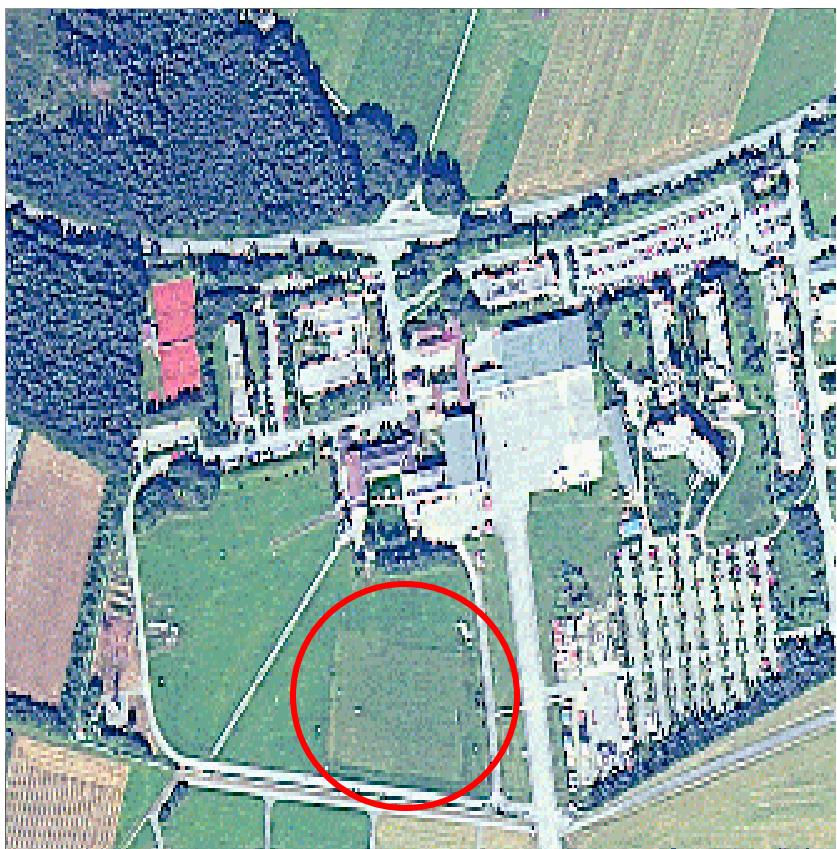
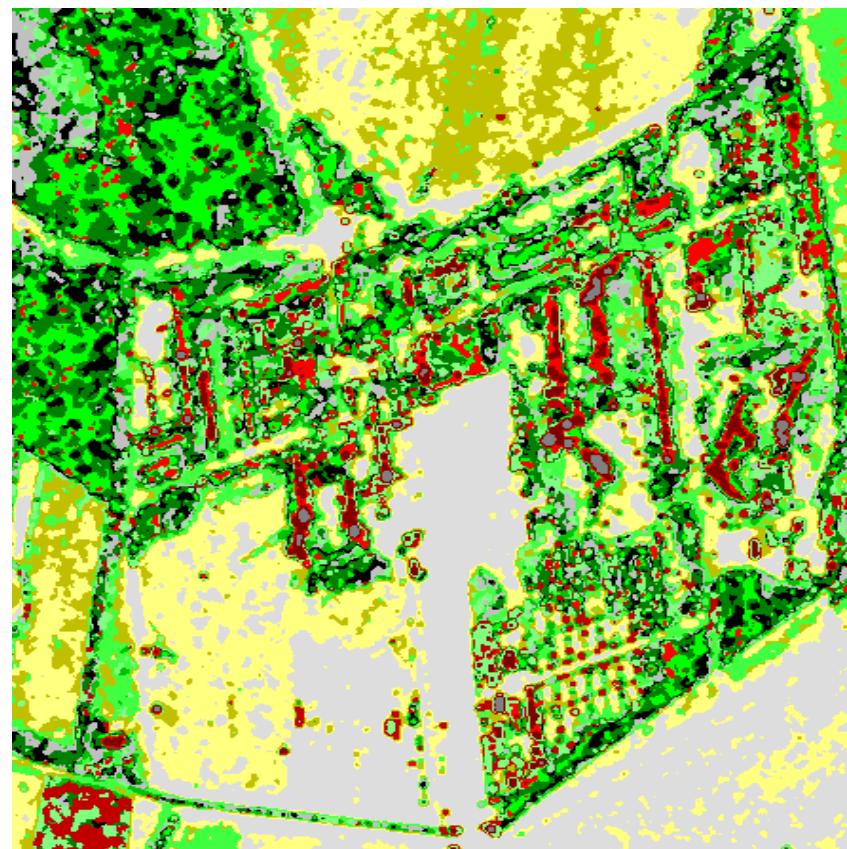
 $2A_0$  $B_0 + B$  $B_0 - B$

OBERPFAFFENHOFEN - ESAR L-band

H/A/ $\alpha$  and WISHART CLASSIFIER $2A_0$  $B_0 + B$  $B_0 - B$ 

C1	C2	C3	C4	C5	C6	C7	C8
C9	C10	C11	C12	C13	C14	C15	C16

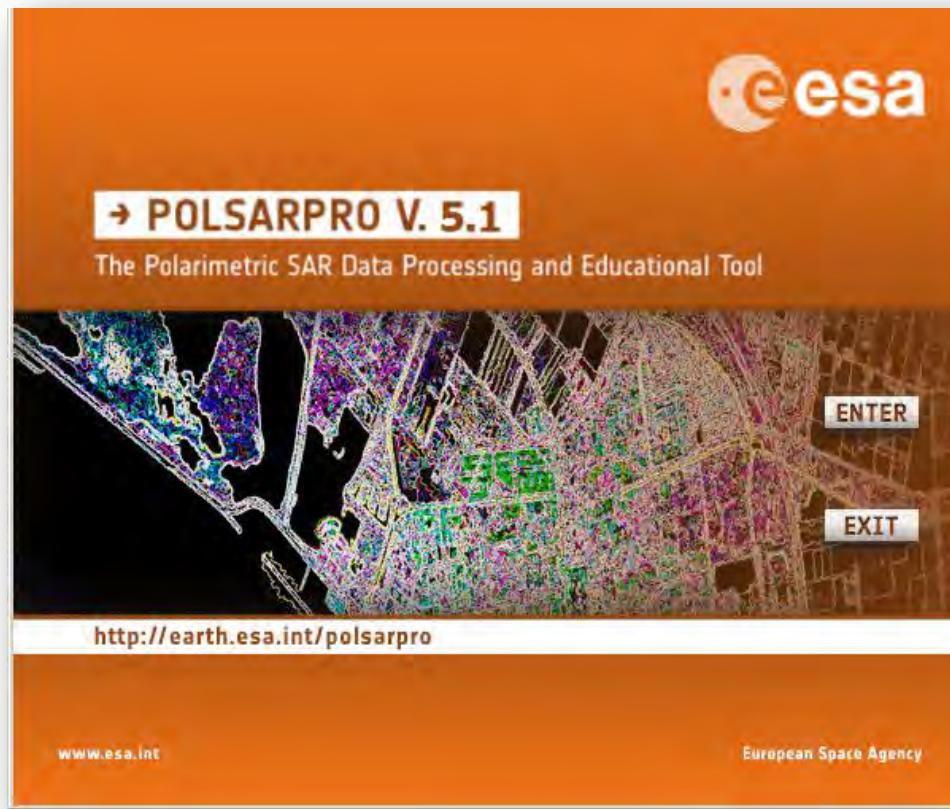
OBERPFAFFENHOFEN - ESAR L-band

H / A /  $\alpha$  and WISHART CLASSIFIER

C1	C2	C3	C4	C5	C6	C7	C8
C9	C10	C11	C12	C13	C14	C15	C16

Questions ?





# PolSARpro v5.1 Software Training Course

→ 7th ADVANCED TRAINING COURSE ON LAND REMOTE SENSING

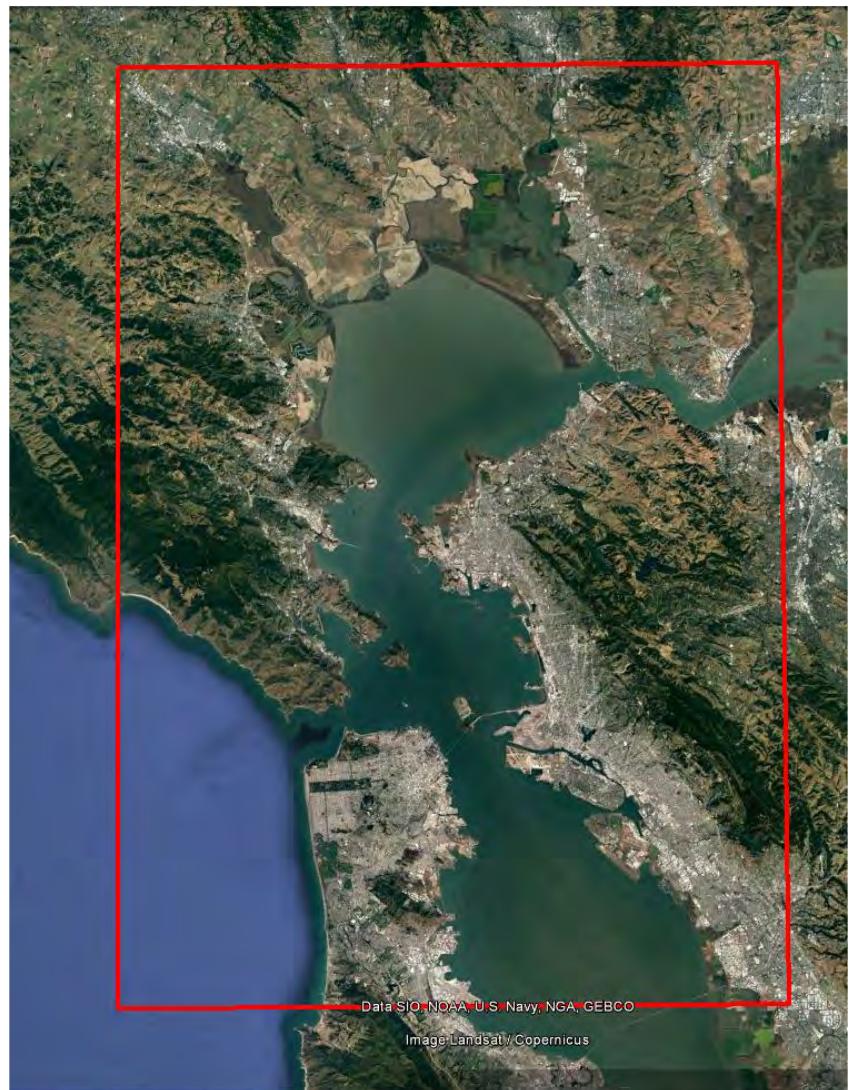
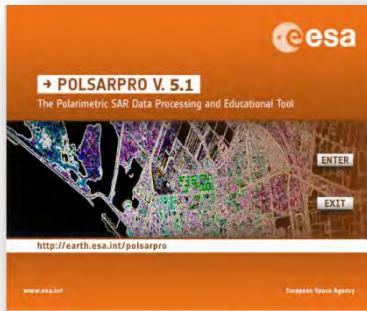
4–9 September 2017 | Szent István University | Gödöllő, Hungary

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**ALOS** ALOS2 - PALSAR   
Advanced Land Observing Satellite

L-Band (Quad - 2015)



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