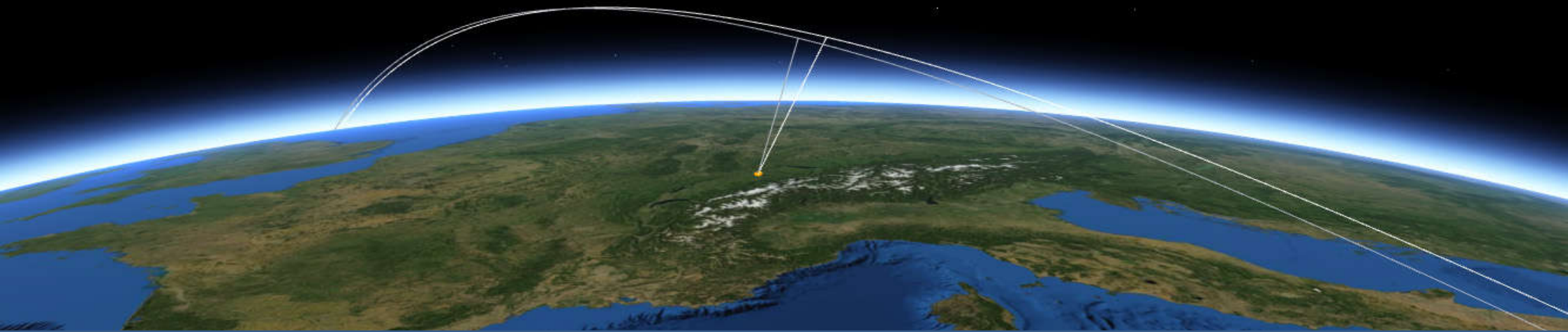


Principles and Basics of InSAR

Irena Hajnsek

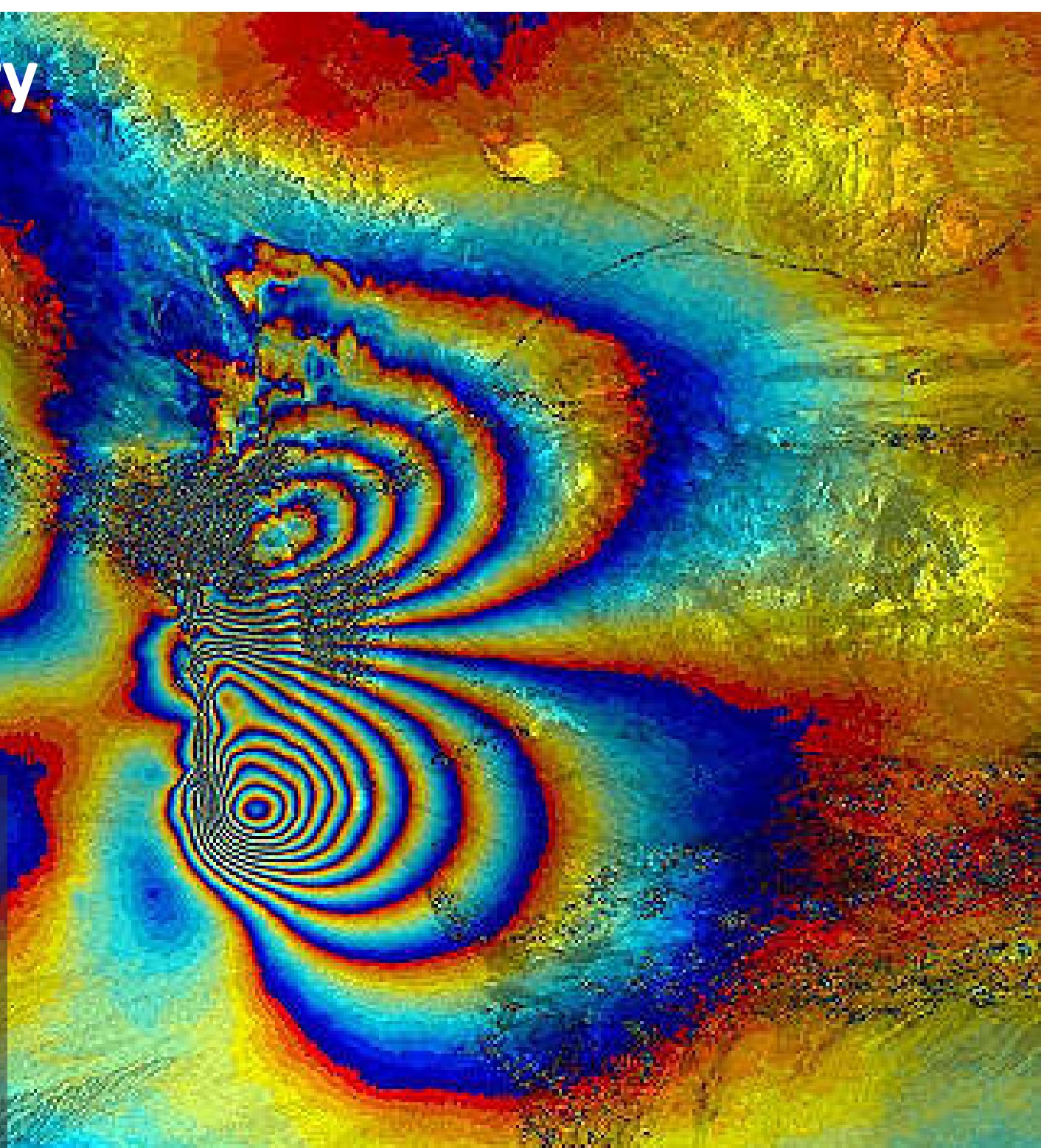
*Earth Observation and Remote Sensing,
Institute of Environmental Engineering, ETH Zürich

*Microwaves and Radar Institut,
German Aerospace Center, Oberpfaffenhofen

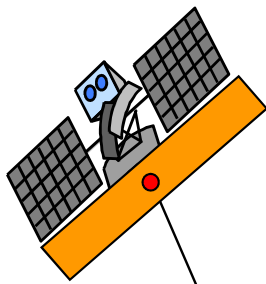
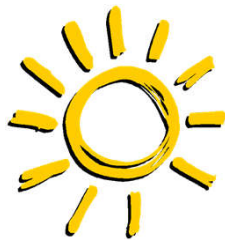


SAR Interferometry

SAR Interferometry refers to the use of phase difference measurements between two (or more) SAR images - acquired separated in space and/or time - to estimate relative distance to an object / scatterer.



SAR Interferometry

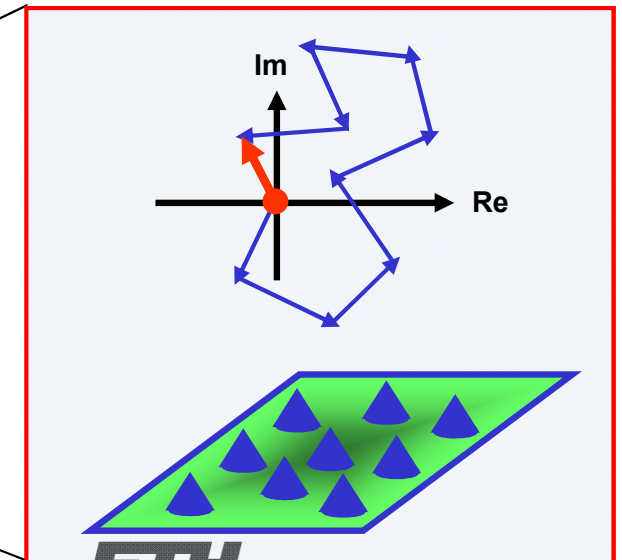
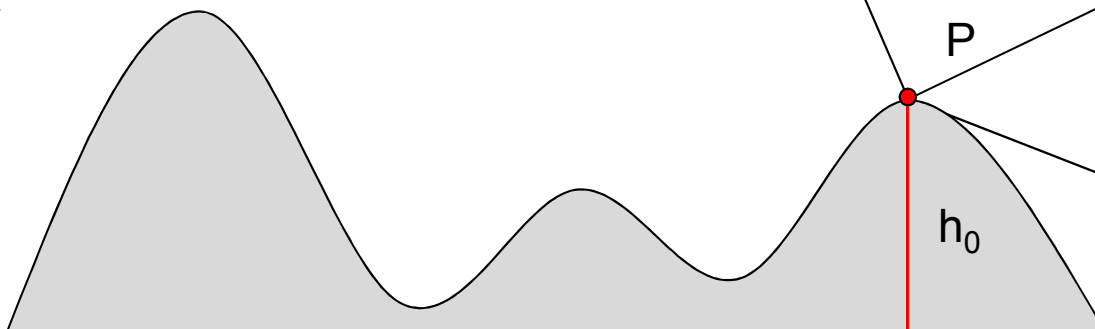
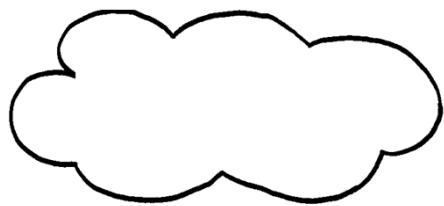


Signal from resolution cell P in Image 1: $i_1 = |i_1| \exp[-i(2\frac{2\pi}{\lambda}R_1) + \varphi_{S1}]$

Phase: $\varphi_1 = \arg(i_1) = \boxed{(2\frac{2\pi}{\lambda}R_1)} + \boxed{\varphi_{S1}}$

Term 1: Deterministic - proportional to the range distance R_1 of P

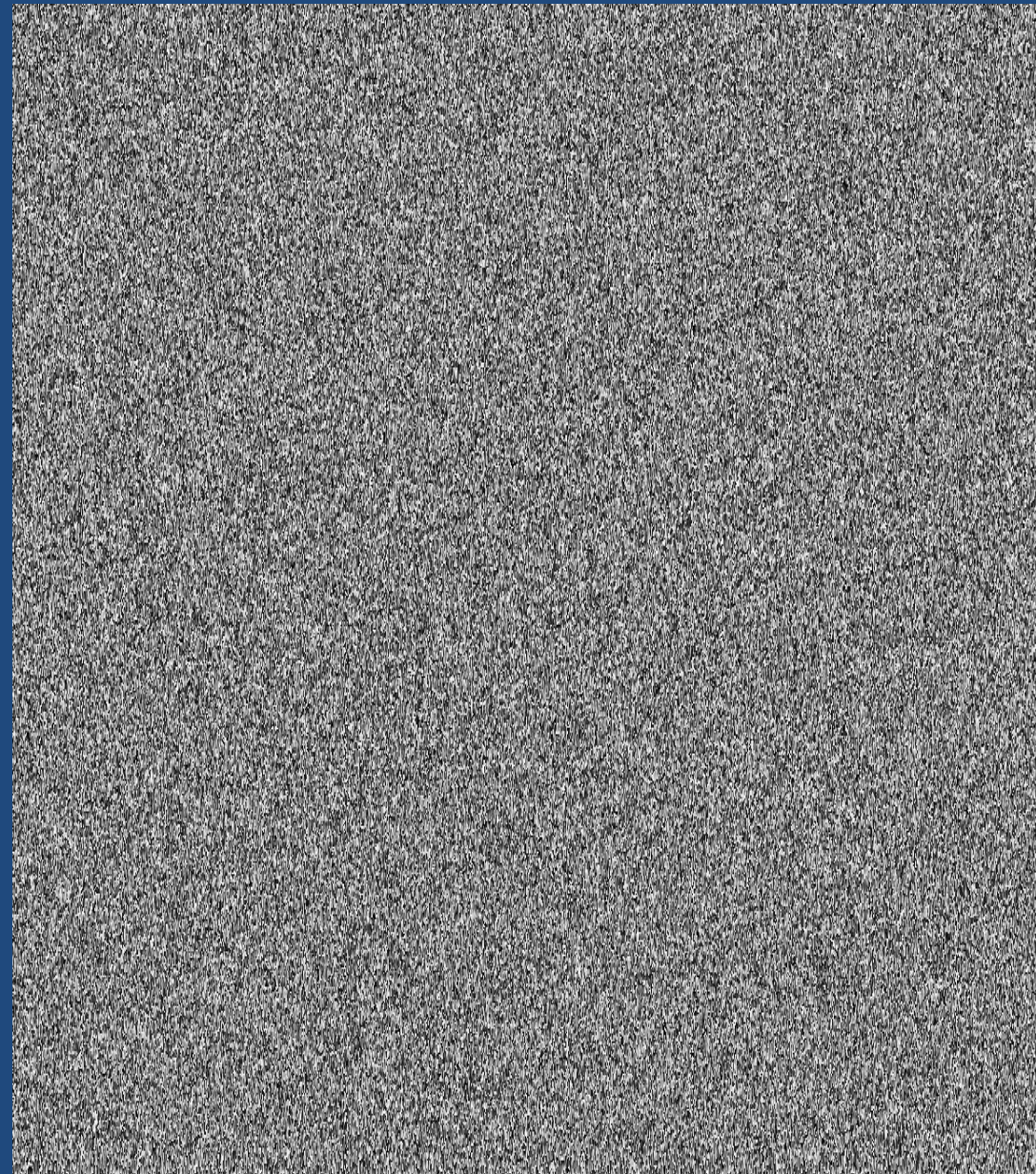
Term 2: Stochastic - induced by the scatterer (Speckle)



ERS – Bachu / China ~ 100 km × 80 km



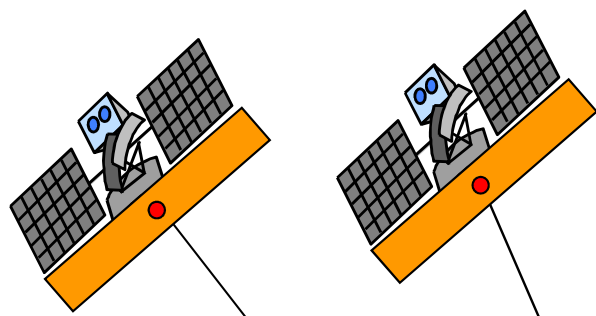
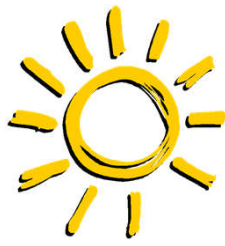
Amplitude of Image 1



Phase of Image 1



SAR Interferometry



$$R_2 = R_1 + \Delta R$$

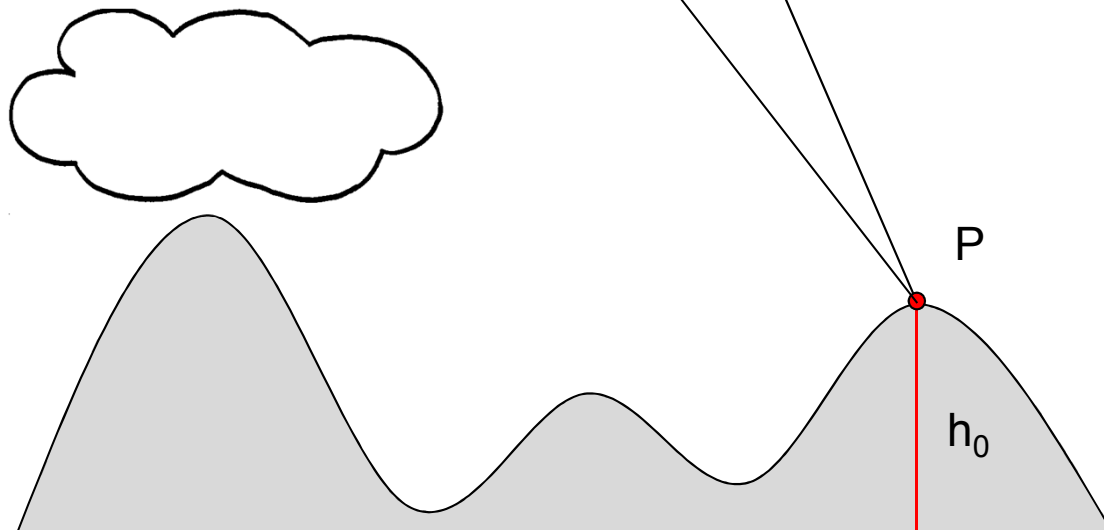
R_1

Signal from resolution cell P in Image 1: $i_1 = |i_1| \exp[-i(2\frac{2\pi}{\lambda}R_1) + \varphi_{s1}]$

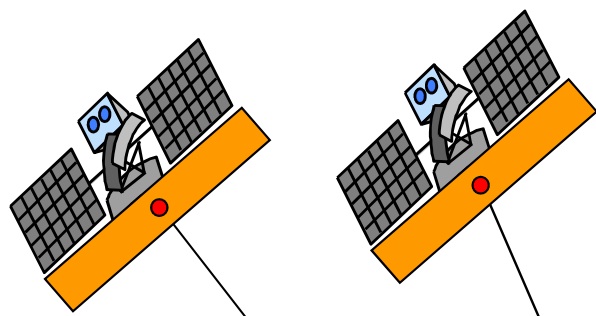
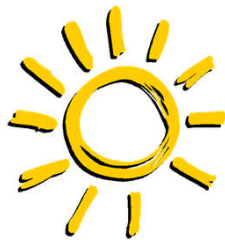
Phase: $\varphi_1 = \arg(i_1) = \boxed{(2\frac{2\pi}{\lambda}R_1)} + \boxed{\varphi_{s1}}$

Signal from resolution cell P in Image 2: $i_2 = |i_2| \exp[-i(2\frac{2\pi}{\lambda}R_2) + \varphi_{s2}]$

Phase: $\varphi_2 = \arg(i_2) = \boxed{(2\frac{2\pi}{\lambda}R_2)} + \boxed{\varphi_{s2}}$



SAR Interferometry



Signal from resolution cell P in Image 1: $i_1 = |i_1| \exp[-i(2\frac{2\pi}{\lambda}R_1) + \varphi_{s1}]$

Phase: $\varphi_1 = \arg(i_1) = \boxed{2\frac{2\pi}{\lambda}R_1} + \varphi_{s1}$

Signal from resolution cell P in Image 2: $i_2 = |i_2| \exp[-i(2\frac{2\pi}{\lambda}R_2) + \varphi_{s2}]$

Phase: $\varphi_2 = \arg(i_2) = \boxed{2\frac{2\pi}{\lambda}R_2} + \varphi_{s2}$

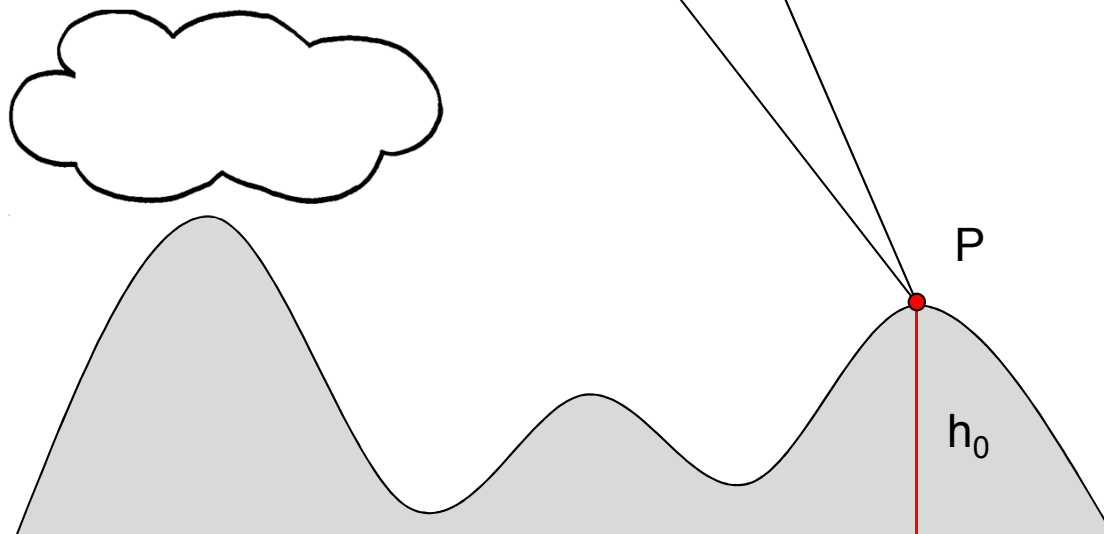


Assuming $\varphi_{s1} = \varphi_{s2} !!!$

Interferogram: $i_1 i_2^* = |i_1 i_2^*| \exp[-i(2\frac{2\pi}{\lambda}\Delta R)]$

Phase: $\varphi_{\text{Int}} = \frac{\text{Re}\{i_1 i_2^*\}}{\text{Im}\{i_1 i_2^*\}} = \boxed{2\frac{2\pi}{\lambda}\Delta R}$

Deterministic !!!



ERS – Bachu / China ~ 100 km × 80 km



Amplitude of Image 1



Amplitude of Image 2



Earth Observation and
Remote Sensing

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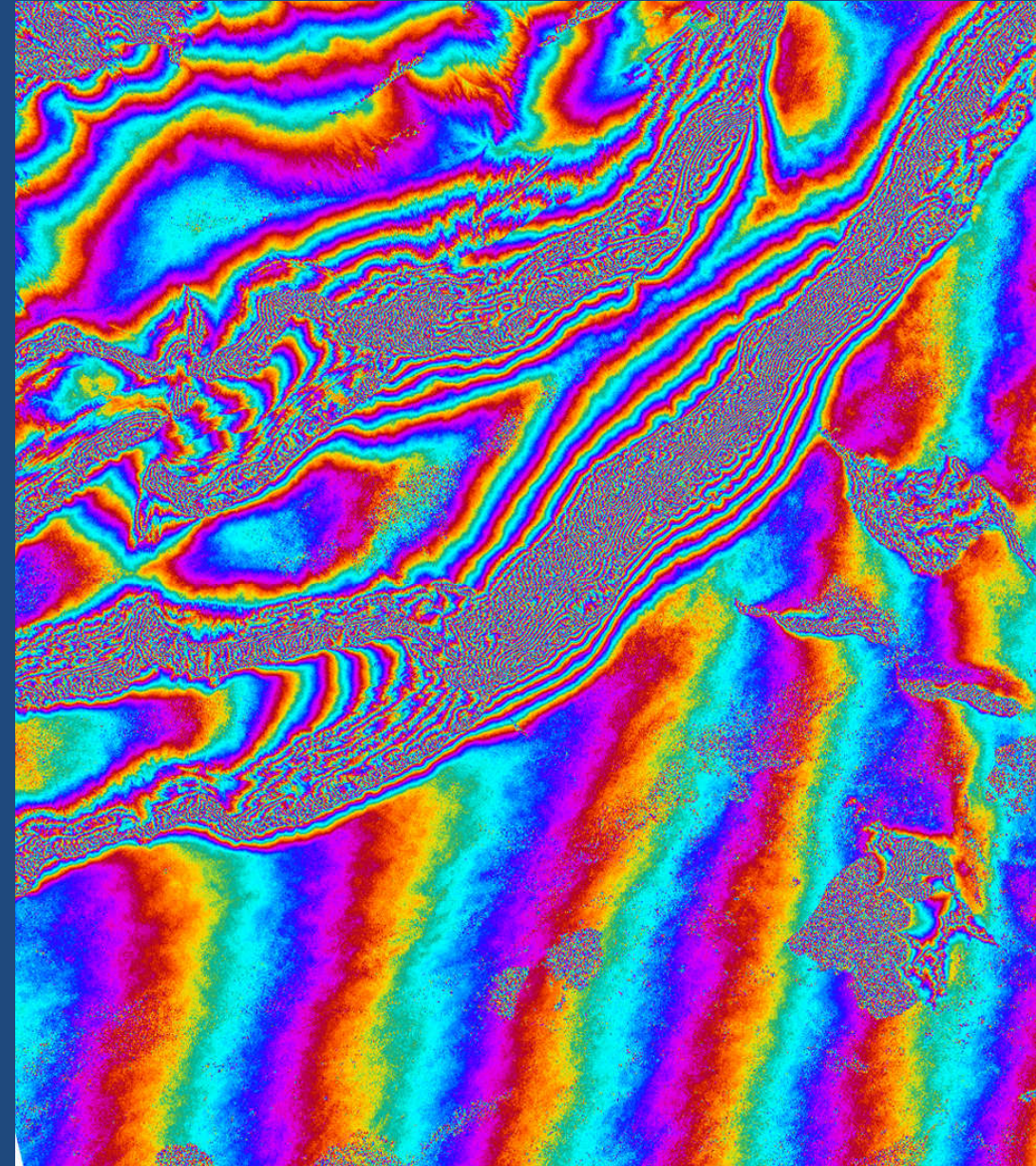


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Swiss Federal Institute of Technology Zurich

ERS – Bachu / China ~ 100 km × 80 km



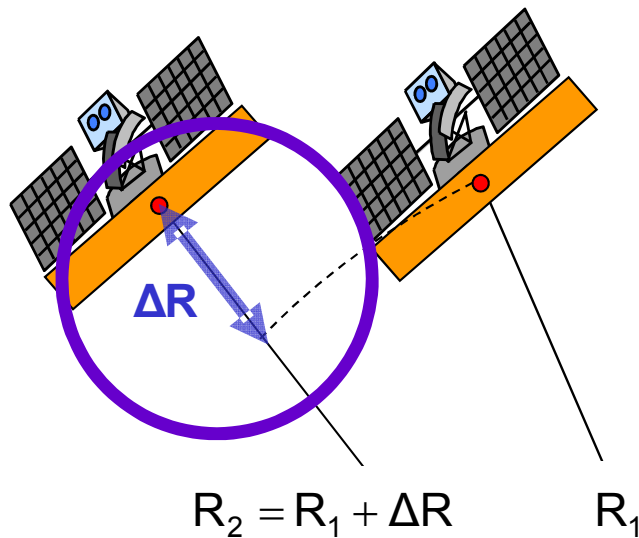
Amplitude of Image 1



Interferometric Phase Image

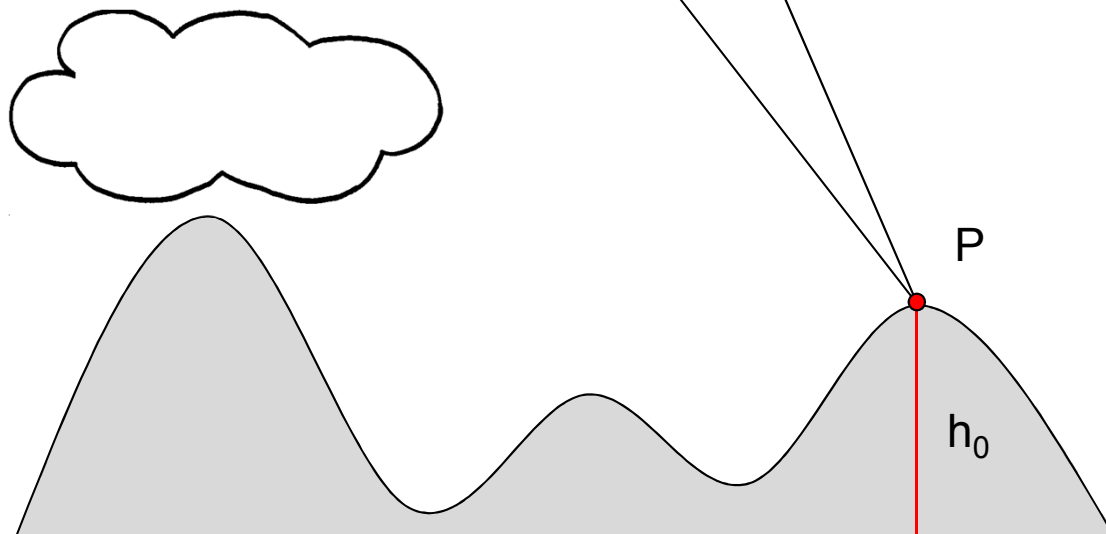
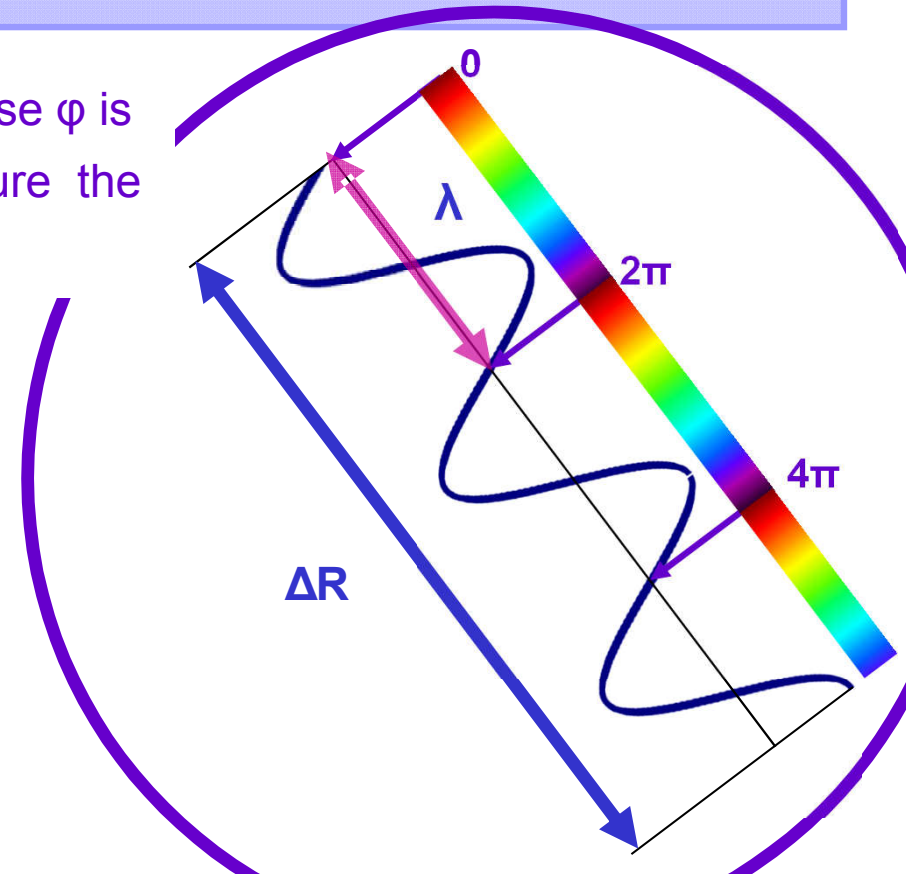


SAR Interferometry



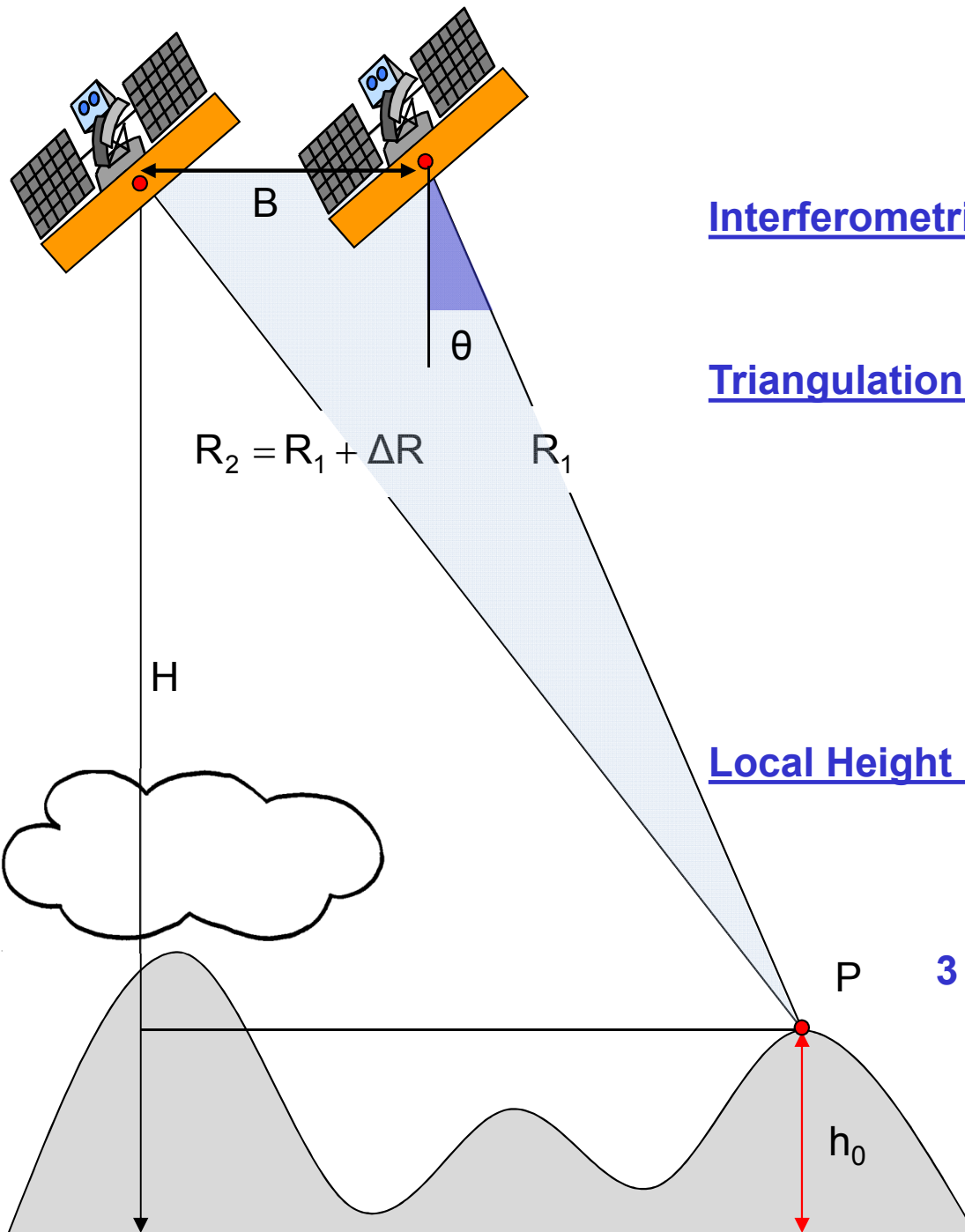
$$\text{Interferometric Phase: } \varphi = 2\frac{2\pi}{\lambda} \Delta R$$

The interferometric phase φ is another way to measure the (relative) distance ΔR :



Phase measurements in interferometric systems can be made with a degree level accuracy. At radar wavelengths of 1-90cm (Ku to P-band) this corresponds to millimeter accuracy !!!

DEM Generation



Interferometric Phase (1): $\varphi = 2 \frac{2\pi}{\lambda} \Delta R + 2\pi N \quad N = 0, \pm 1, \pm 2$

Triangulation (2): $(R_1 + \Delta R)^2 = R_1^2 + B^2 - 2R_1B \cos(\pi/2 + \theta) \rightarrow$

$$\rightarrow \sin(\theta) = \frac{(R_1 + \Delta R)^2 - R_1^2 - B^2}{2R_1B}$$

Local Height (3): $h_0 = H - (R_1 + \Delta R) \cos(\theta)$



3 non-linear equations for 3 unknowns (h_0 , θ , ΔR)

B ... Spatial baseline and

R_1 ... Range distance in Image 1 are known

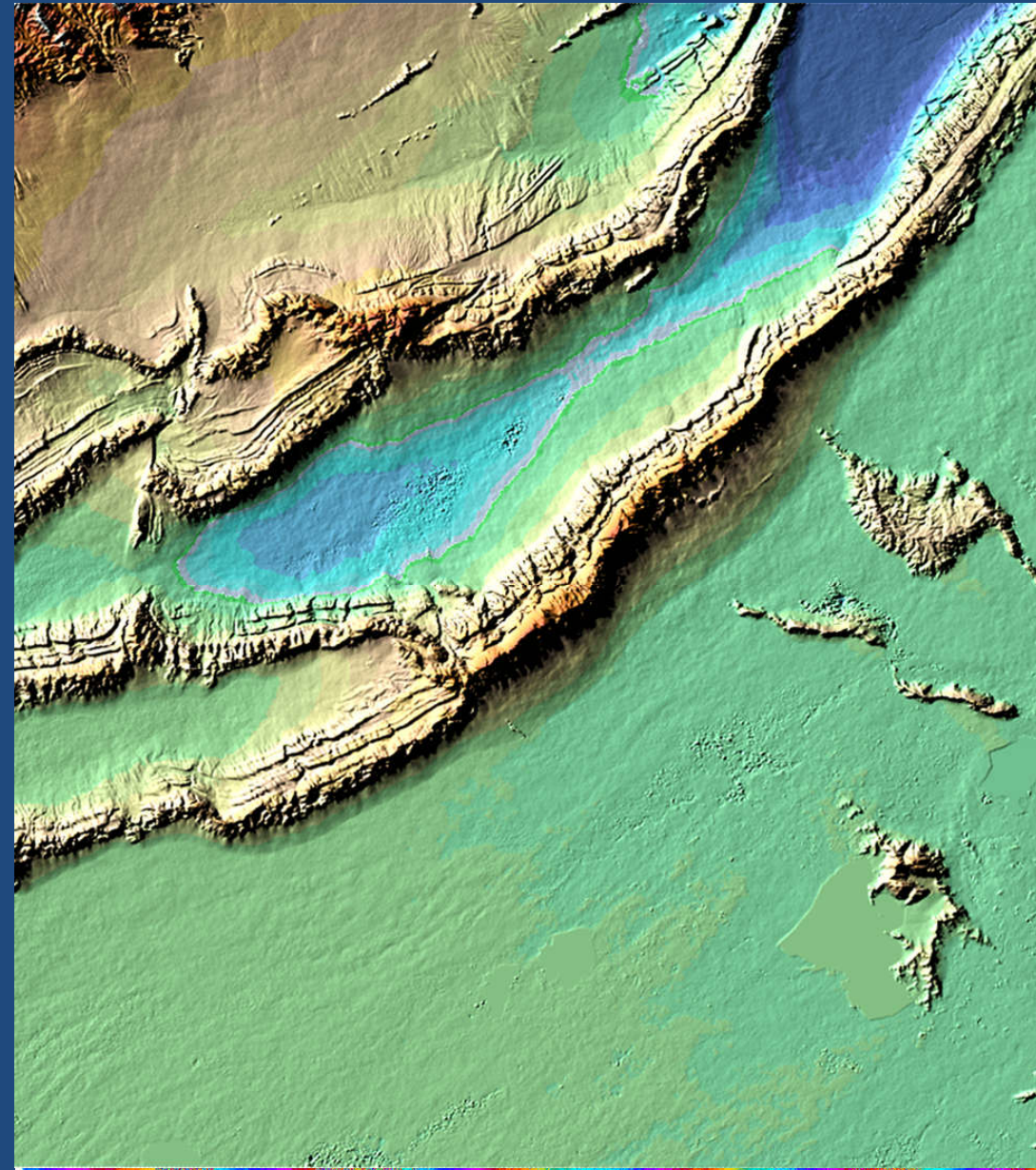
Critical is the fact that the interferometric phase φ is initially measured modulo 2π ► Phase Unwrapping



ERS – Bachu / China ~ 100 km × 80 km



Amplitude Image



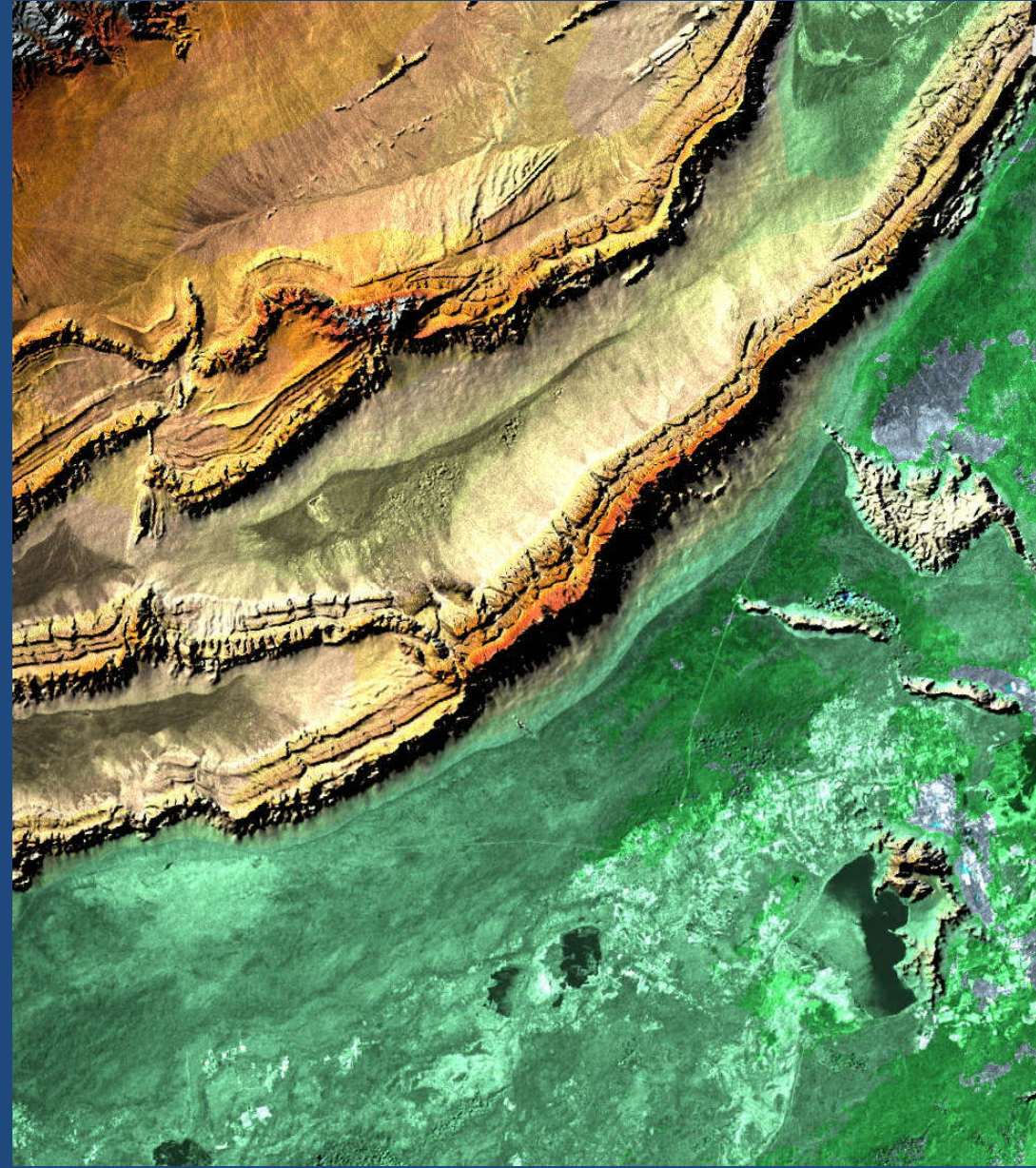
Digital Elevation Model with false colors



ERS – Bachu / China ~ 100 km × 80 km

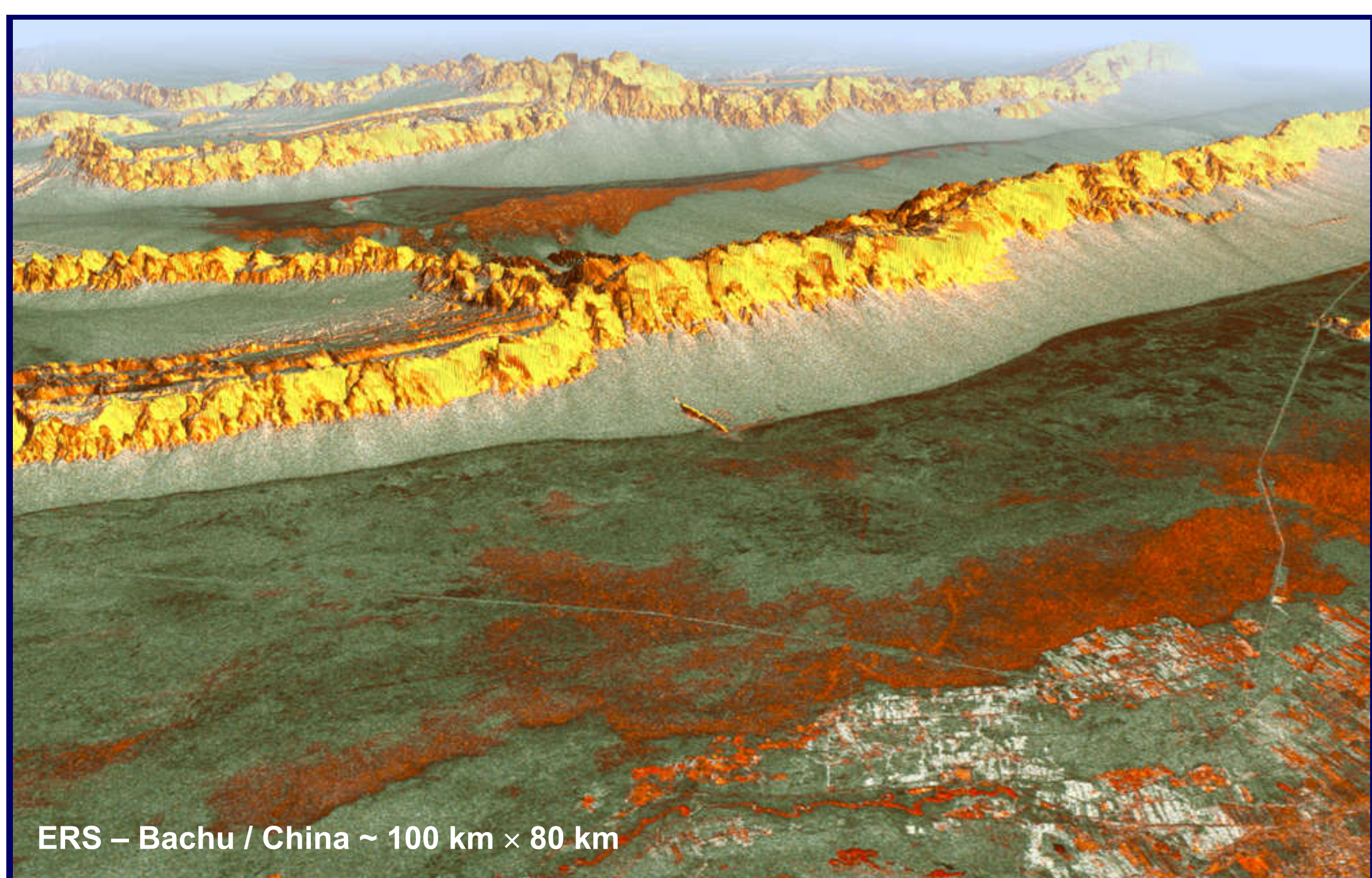


Amplitude Image



Digital Elevation Model and SAR image





ERS – Bachu / China ~ 100 km × 80 km



Earth Observation and
Remote Sensing

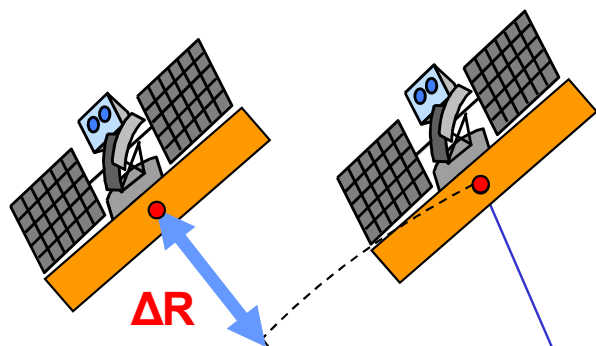
hajnsek@ifu.baug.ethz.ch
irena.hajnsek@dlr.de

- 13



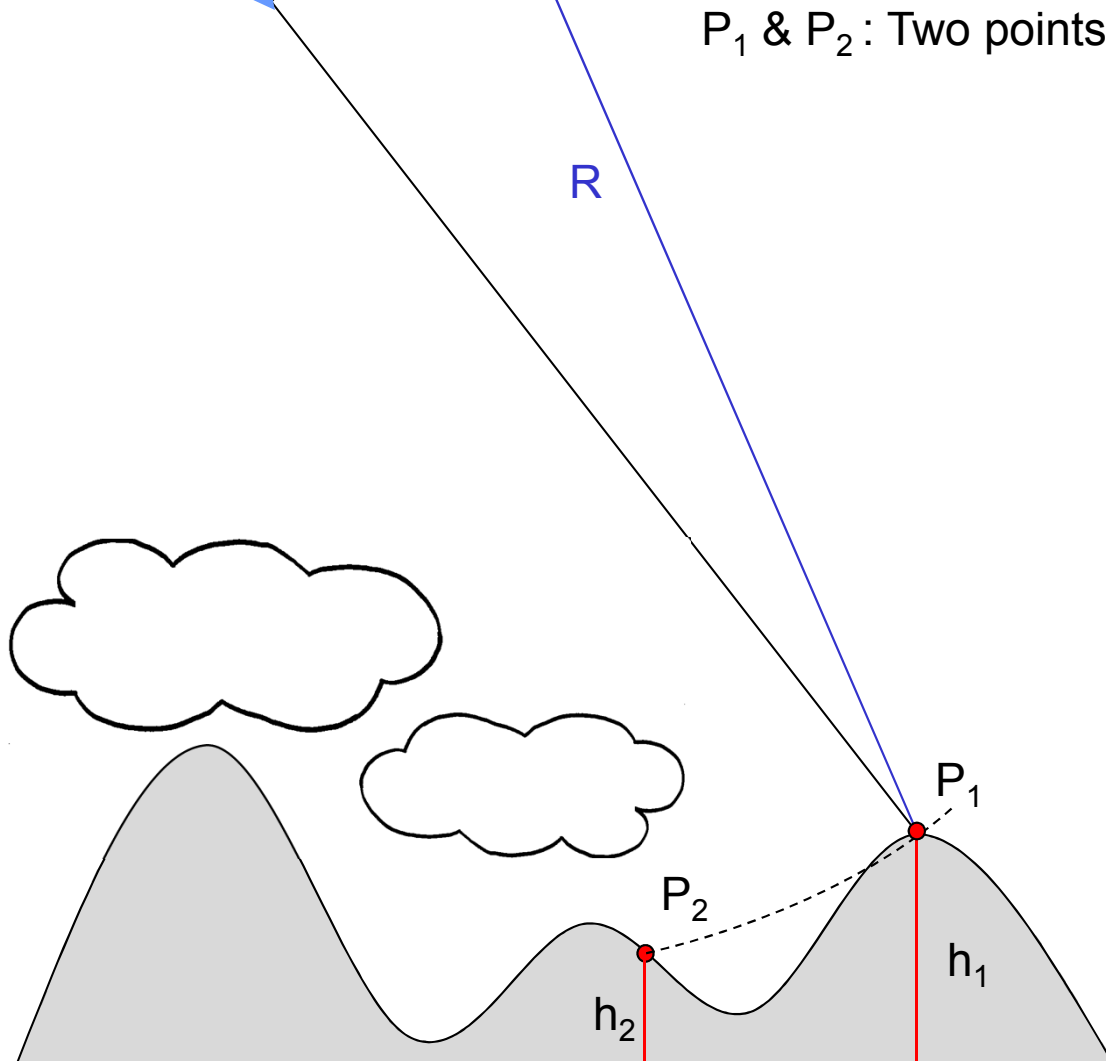
Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zurich

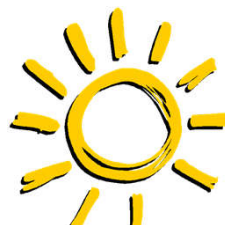
InSAR Phase: Height Sensitivity



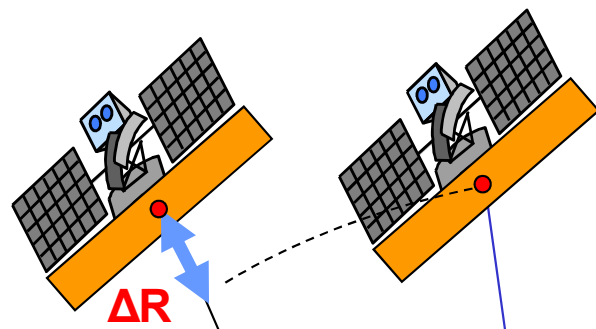
Interferometric Phase: $\varphi = 2\frac{2\pi}{\lambda}\Delta R + 2\pi N$ where $N = 0, \pm 1, \pm 2$

P_1 & P_2 : Two points at the same range but different heights h_1 & h_2 :





InSAR Phase: Height Sensitivity



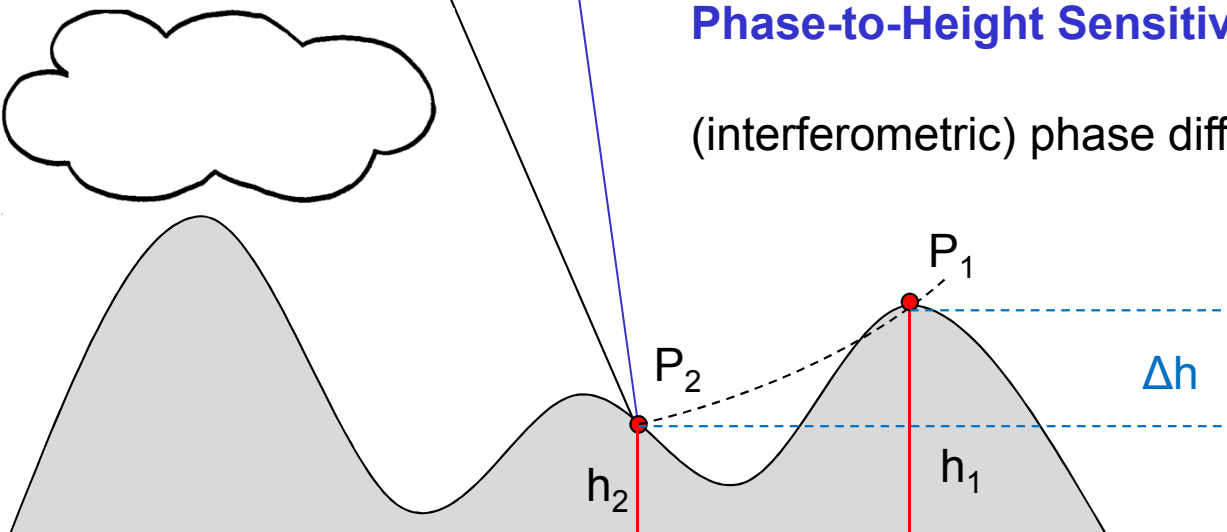
Interferometric Phase: $\varphi = 2\frac{2\pi}{\lambda}\Delta R + 2\pi N$ where $N = 0, \pm 1, \pm 2$

P_1 & P_2 : Two points at the same range but different heights h_1 & h_2

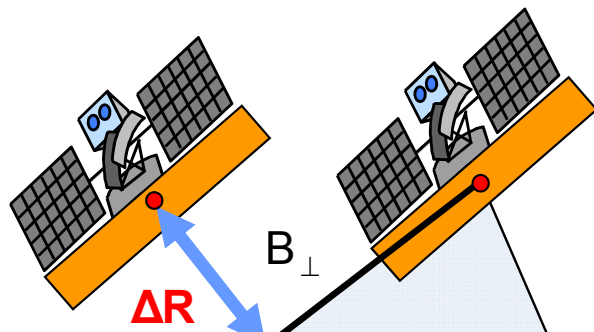
ΔR changes implying a different interferometric phase at each point

In other words: The height difference $\Delta h = h_1 - h_2$ causes an (interferometric) phase difference $\Delta\varphi$;

Phase-to-Height Sensitivity $\partial\varphi / \partial z$ [rad/m]: is defined by the (interferometric) phase difference caused by a given height difference (1m)



InSAR Phase: Height Sensitivity



Interferometric Phase: $\varphi = 2\frac{2\pi}{\lambda} \Delta R + 2\pi N$ where $N = 0, \pm 1, \pm 2$

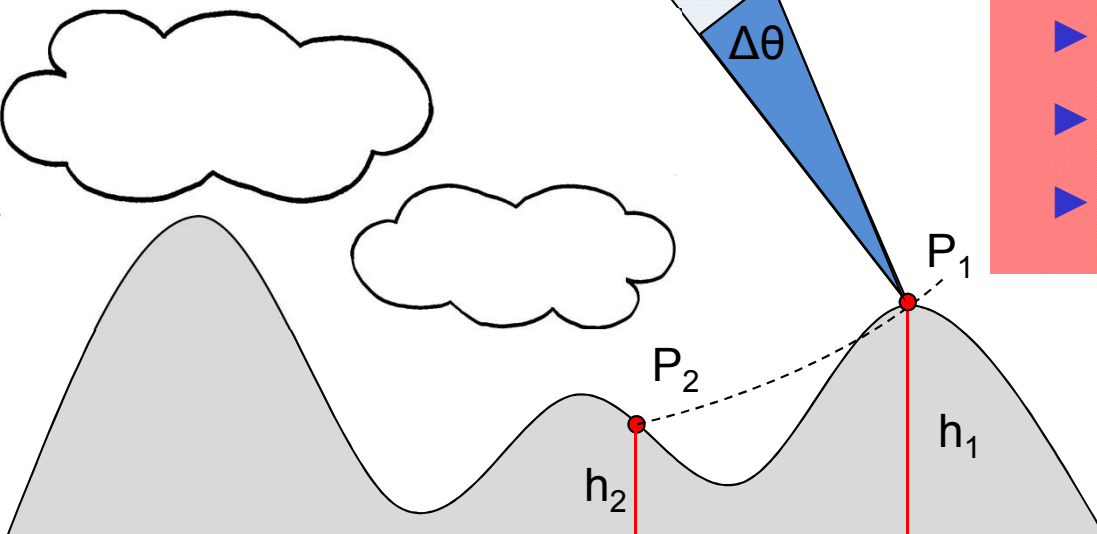
P_1 & P_2 : Two points at the same range but different heights h_1 & h_2 :

Phase-to-Height Sensitivity:

$$\frac{\partial \varphi}{\partial z} := \kappa_z = \frac{4\pi}{\lambda} \frac{\Delta \theta}{\sin(\theta)} \approx \frac{4\pi}{\lambda} \frac{B_{\perp}}{R \sin(\theta)} \quad \text{using} \quad \Delta \theta \approx \frac{B_{\perp}}{R}$$

The Phase-to-Height Sensitivity increases with:

- ▶ Increasing the spatial baseline (i.e. $\Delta \theta$ or B_{\perp});
- ▶ Increasing the system frequency (i.e. decreasing λ);
- ▶ At steeper (i.e. smaller) incidence angles θ .



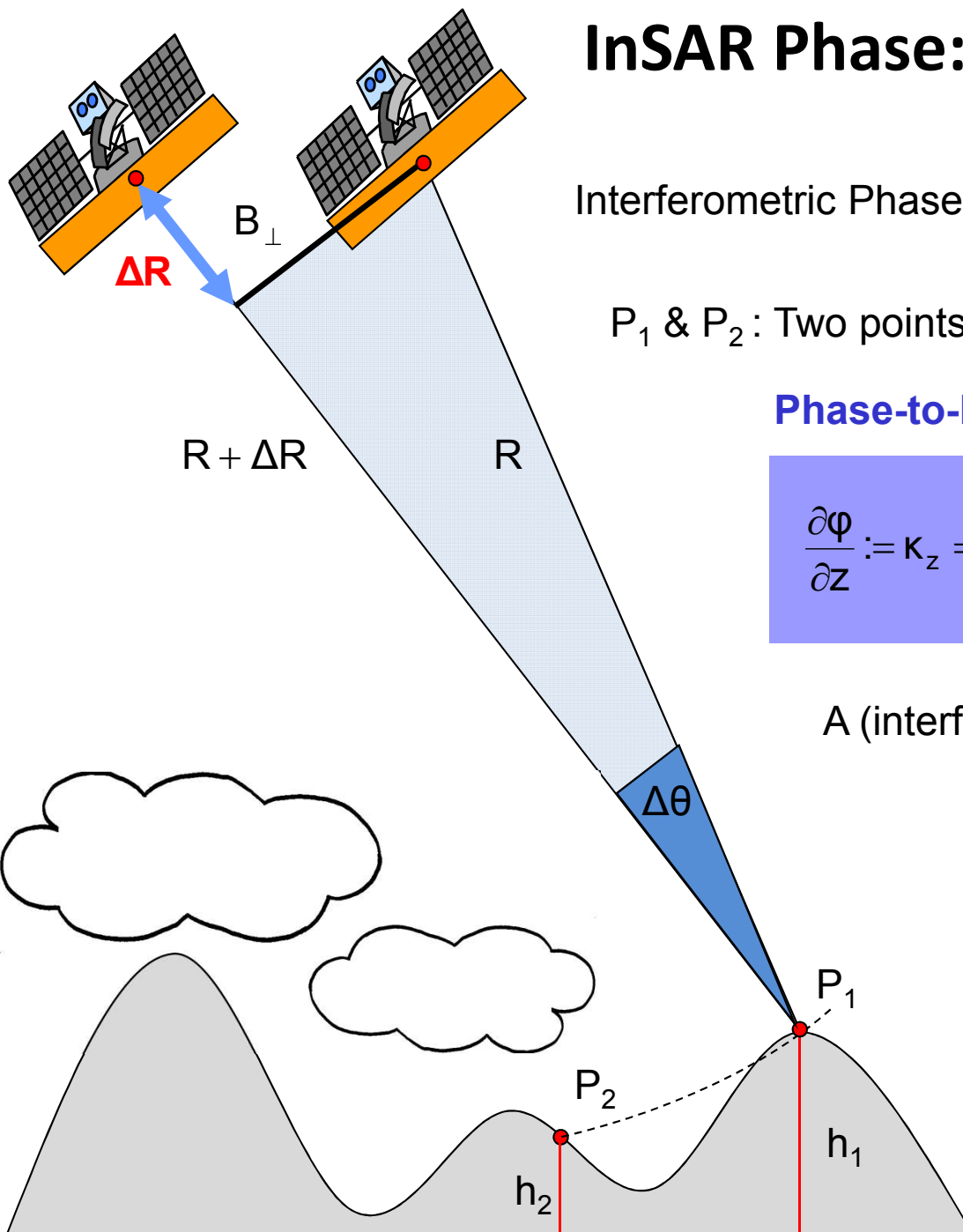
Height of Ambiguity (HoA):

the height that causes a 2π phase difference:

$$\text{HoA} = \frac{\lambda}{4\pi} \frac{R \sin(\theta)}{B_{\perp}} 2\pi = \frac{\lambda}{2} \frac{R \sin(\theta)}{B_{\perp}}$$



InSAR Phase: Height Sensitivity



Interferometric Phase: $\varphi = 2\frac{2\pi}{\lambda} \Delta R + 2\pi N$ where $N = 0, \pm 1, \pm 2$

P_1 & P_2 : Two points at the same range but different heights h_1 & h_2 :

Phase-to-Height Sensitivity [rad/m]:

$$\frac{\partial \varphi}{\partial z} := \kappa_z = \frac{4\pi}{\lambda} \frac{\Delta \theta}{\sin(\theta)} \approx \frac{4\pi}{\lambda} \frac{B_{\perp}}{R \sin(\theta)} \quad \text{using} \quad \Delta \theta \approx \frac{B_{\perp}}{R}$$

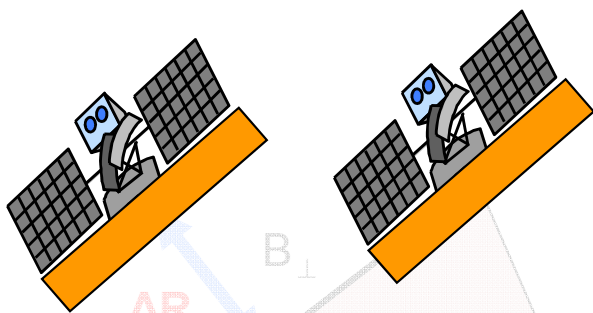
A (interferometric) phase error σ_{φ} induces a **height error σ_z** :

$$\sigma_z = \frac{1}{\partial \varphi / \partial z} \sigma_{\varphi} = \frac{1}{\kappa_z} \sigma_{\varphi} \approx \frac{\lambda}{4\pi} \frac{R \sin(\theta)}{B_{\perp}} \sigma_{\varphi}$$

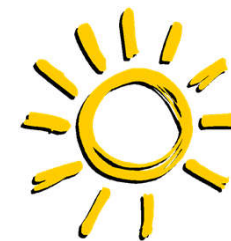
For the same (interferometric) phase error σ_{φ} the induced **height error decreases** with:

- Increasing the spatial baseline;
- Increasing the system frequency;
- At steeper incidence angles θ .





InSAR Phase: Height Sensitivity



Example: ERS-1 / 2 Interferometry at C-band $\lambda=5.6 \text{ cm}=0.056\text{m}$, $R=870\text{km}$, $\theta=23^\circ=23 \pi/180 \text{ rad}$

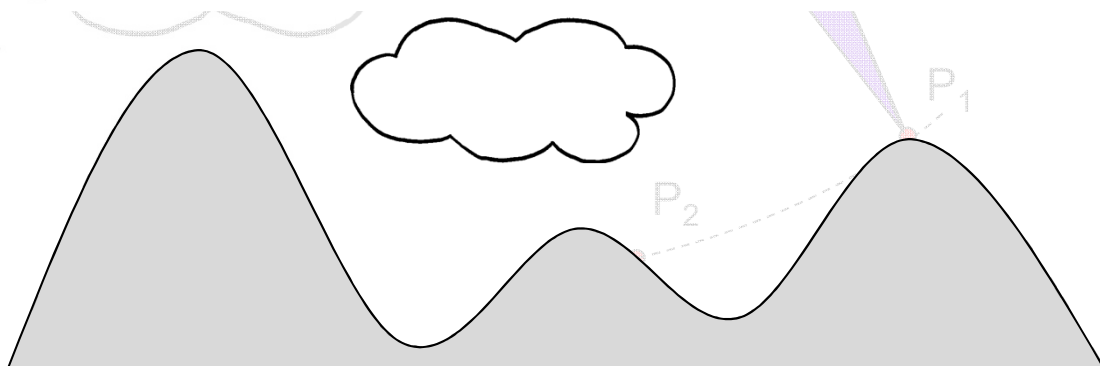
Phase-to-Height Sensitivity:
$$\frac{\partial \phi}{\partial z} = \frac{4\pi}{\lambda} \frac{B_{\perp}}{R \sin(\theta)} \approx 2\pi \frac{B_{\perp}}{100^2}$$

... with increasing B_{\perp} the Phase-to-Height Sensitivity increases

B_{\perp}	$\partial \phi / \partial z$ [rad/m]	HoA
50 m	≈ 0.0314	$\approx 200 \text{ m}$
100 m	≈ 0.0628	$\approx 100 \text{ m}$
200 m	≈ 0.1256	$\approx 50 \text{ m}$

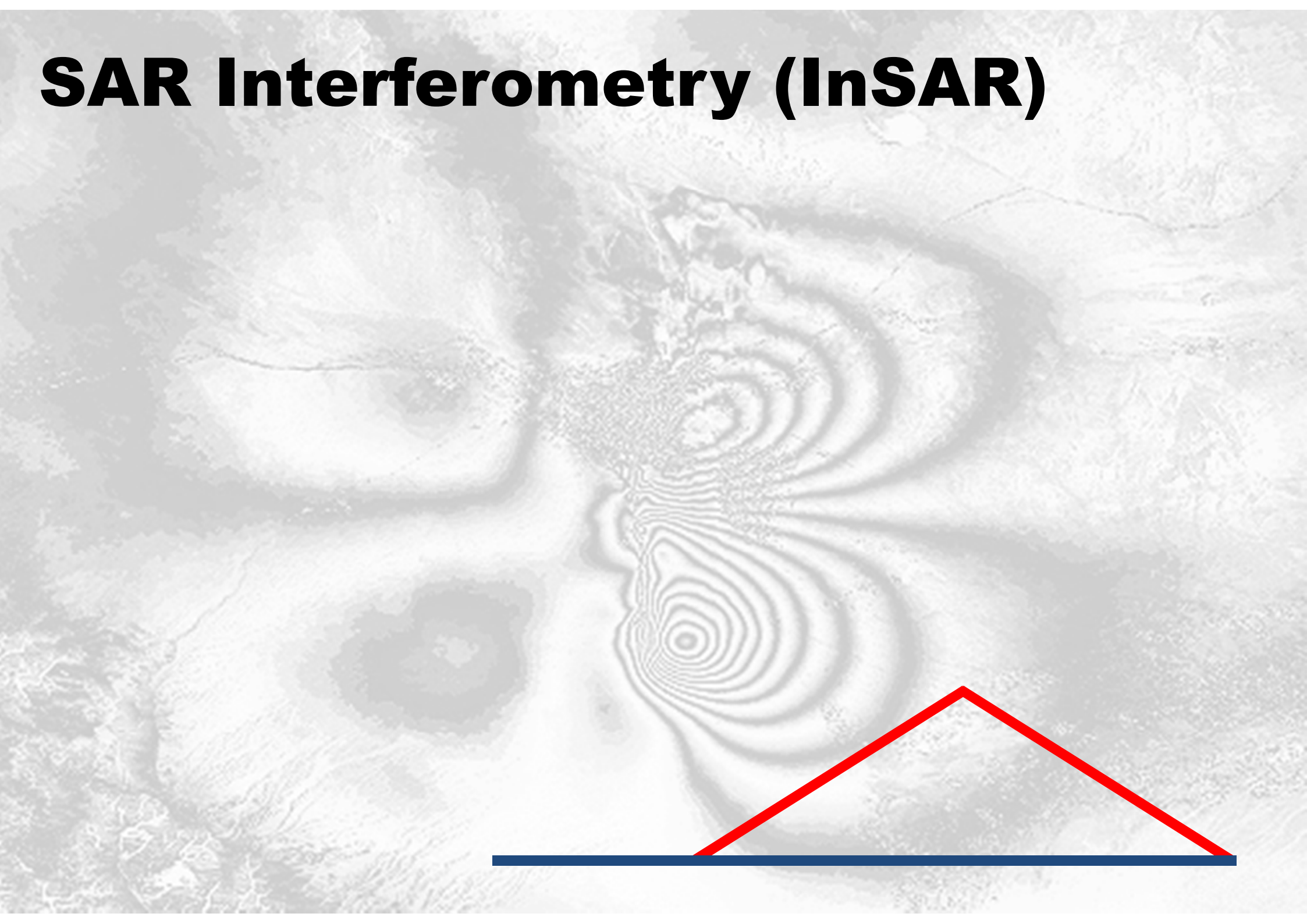
Height Error:
$$\sigma_z = \frac{1}{\partial \phi / \partial z} \sigma_{\phi} \approx \frac{1}{2\pi} \frac{100^2}{B_{\perp}} \sigma_{\phi}$$

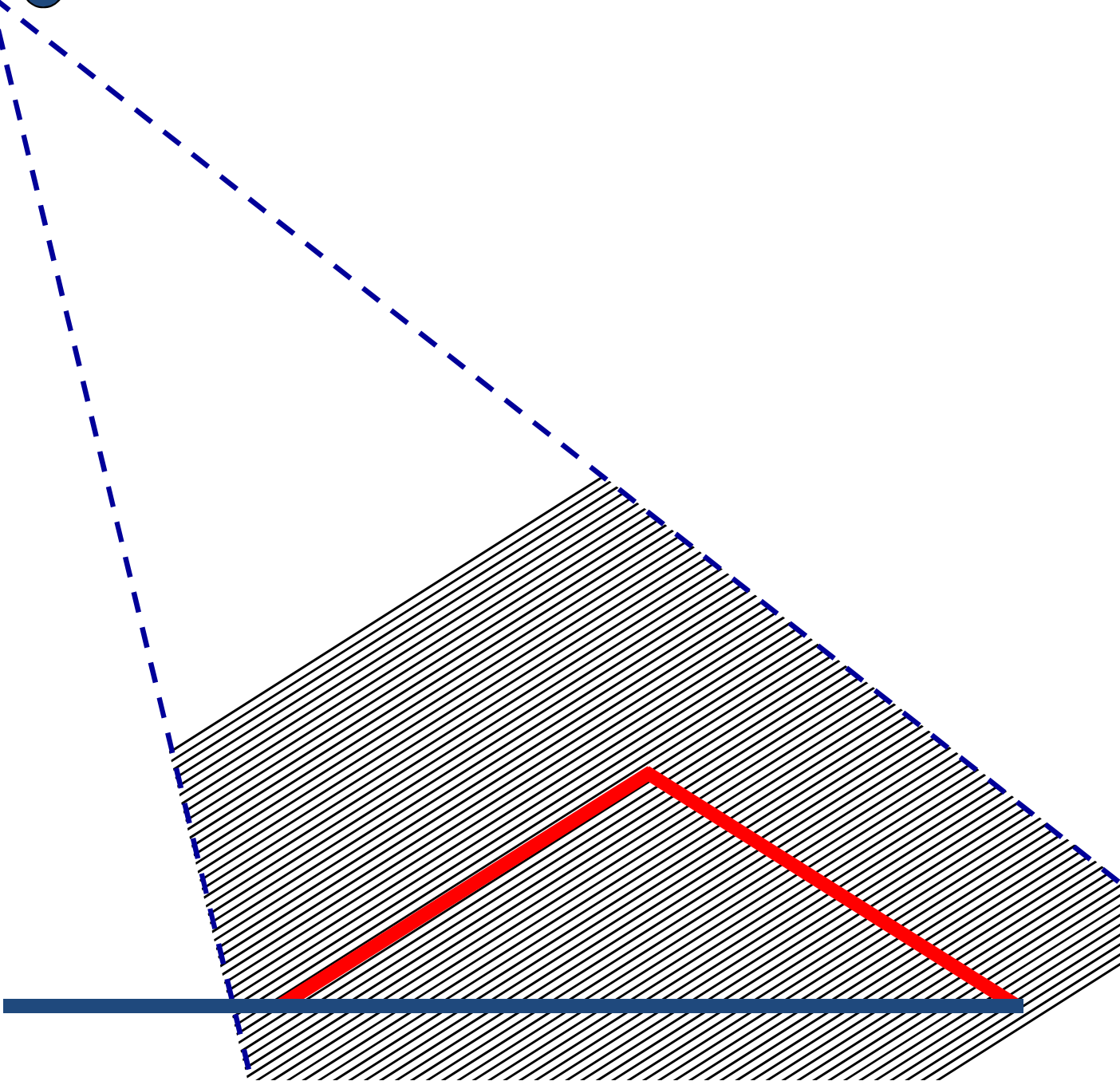
Assuming that one can estimate the interferometric phase with an accuracy of 30° ($\sigma_{\phi}=30 \pi/180 \text{ rad}$)

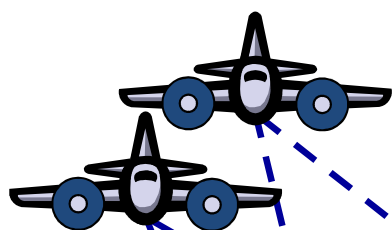


B_{\perp}	$\partial \phi / \partial z$ [rad/m]	σ_z
50 m	≈ 0.0314	$\approx 16.6 \text{ m}$
100 m	≈ 0.0628	$\approx 8.3 \text{ m}$
200 m	≈ 0.1256	$\approx 4.2 \text{ m}$

SAR Interferometry (InSAR)



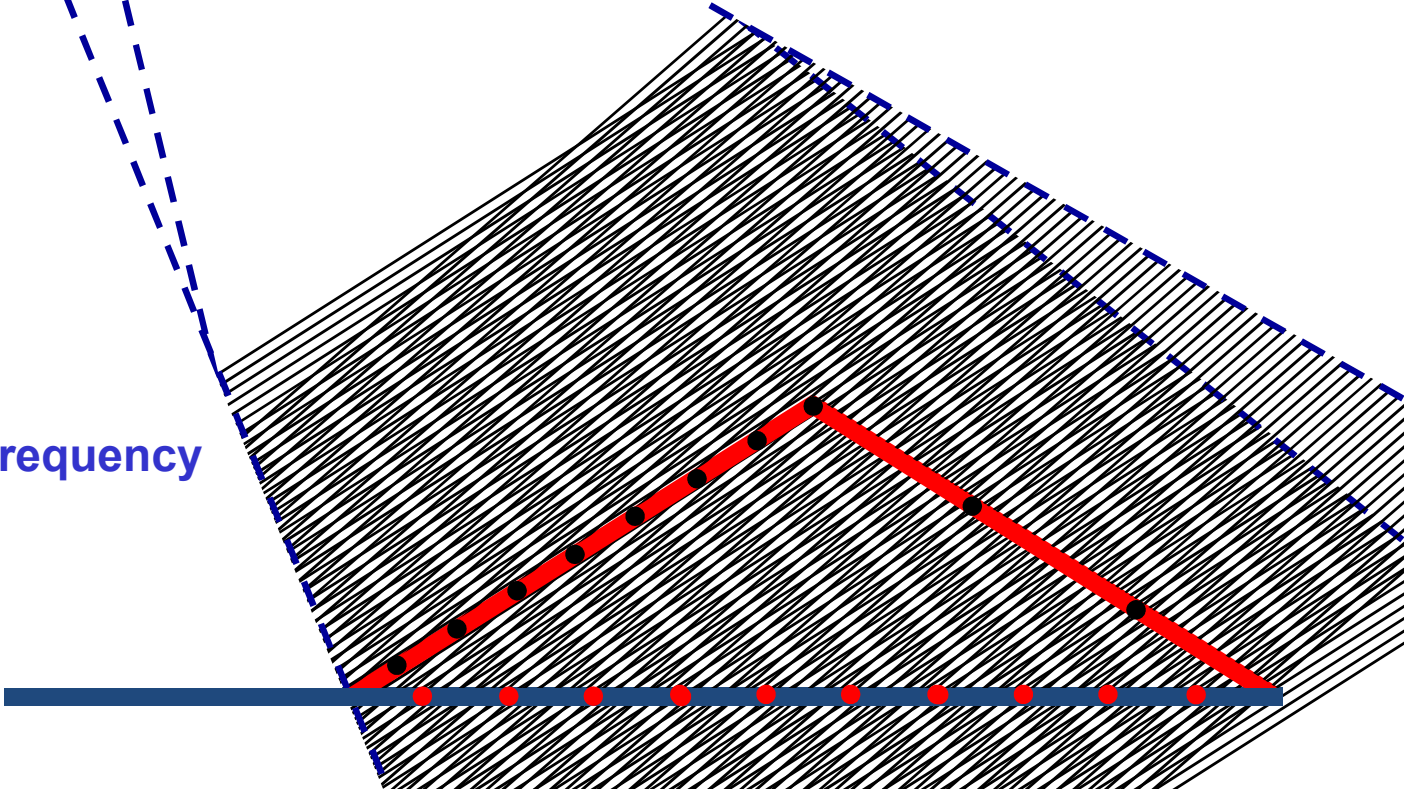


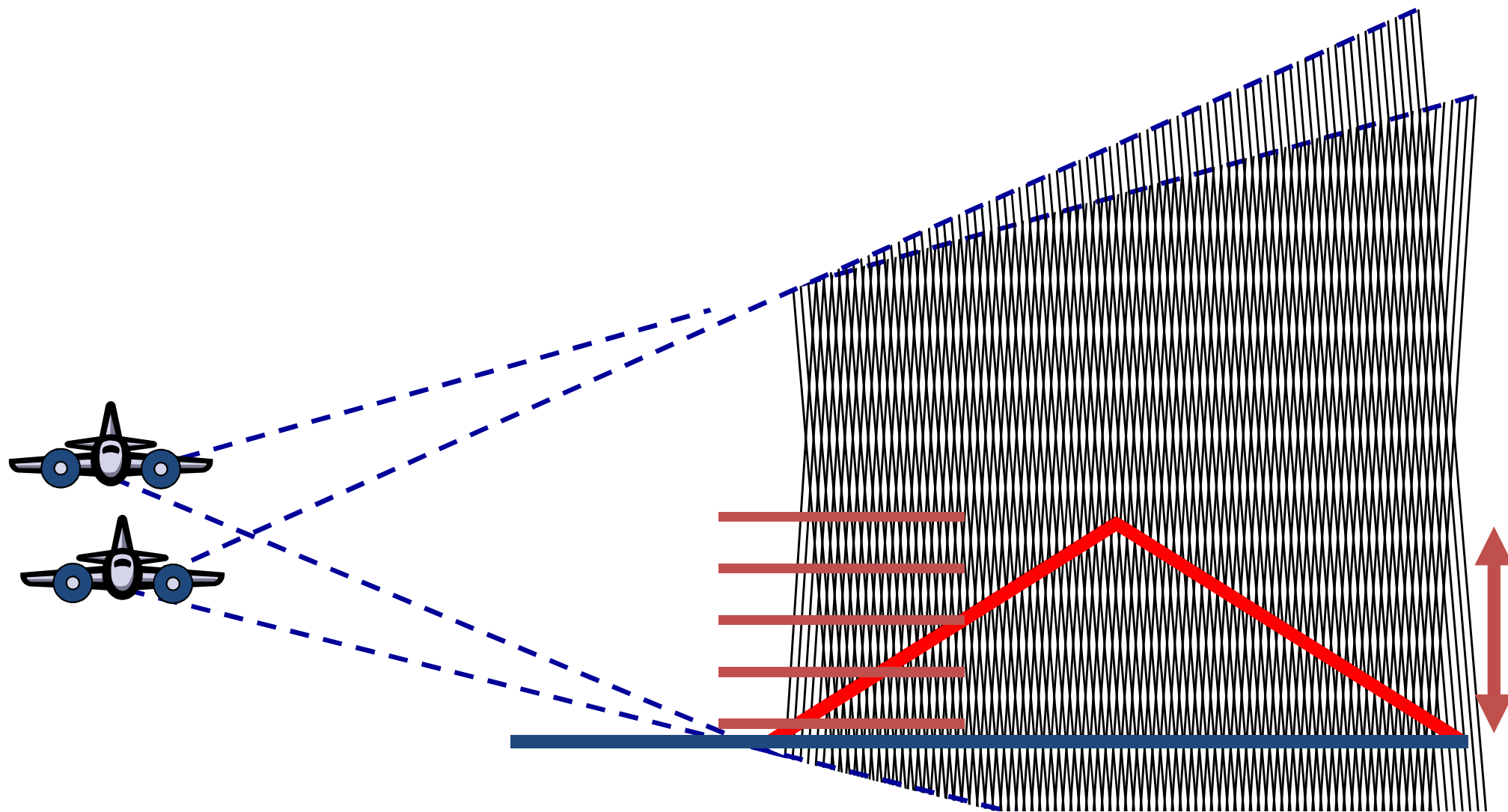


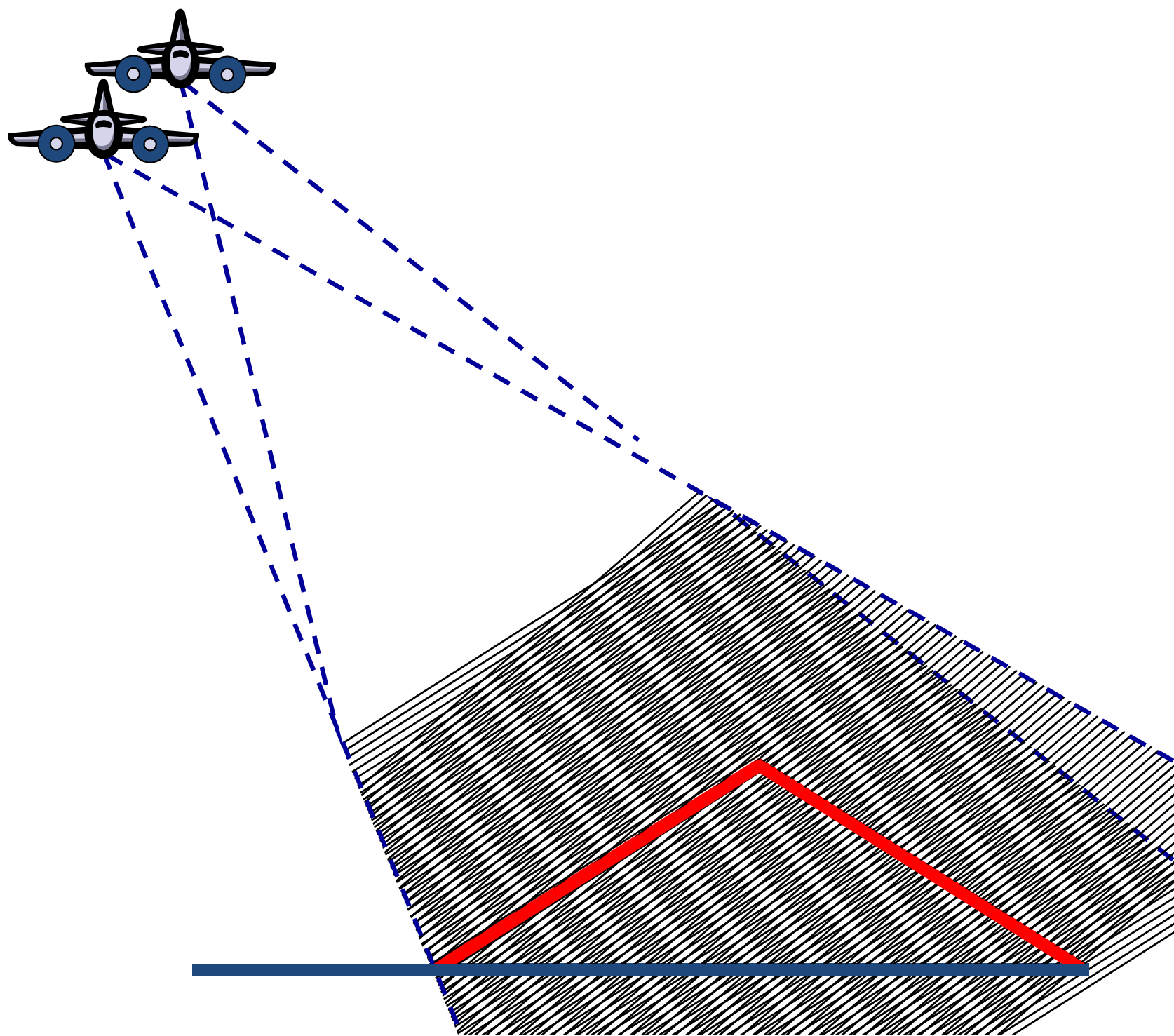
Interference pattern in the far field consists of equidistant parallel lines (parallel ray approx.).

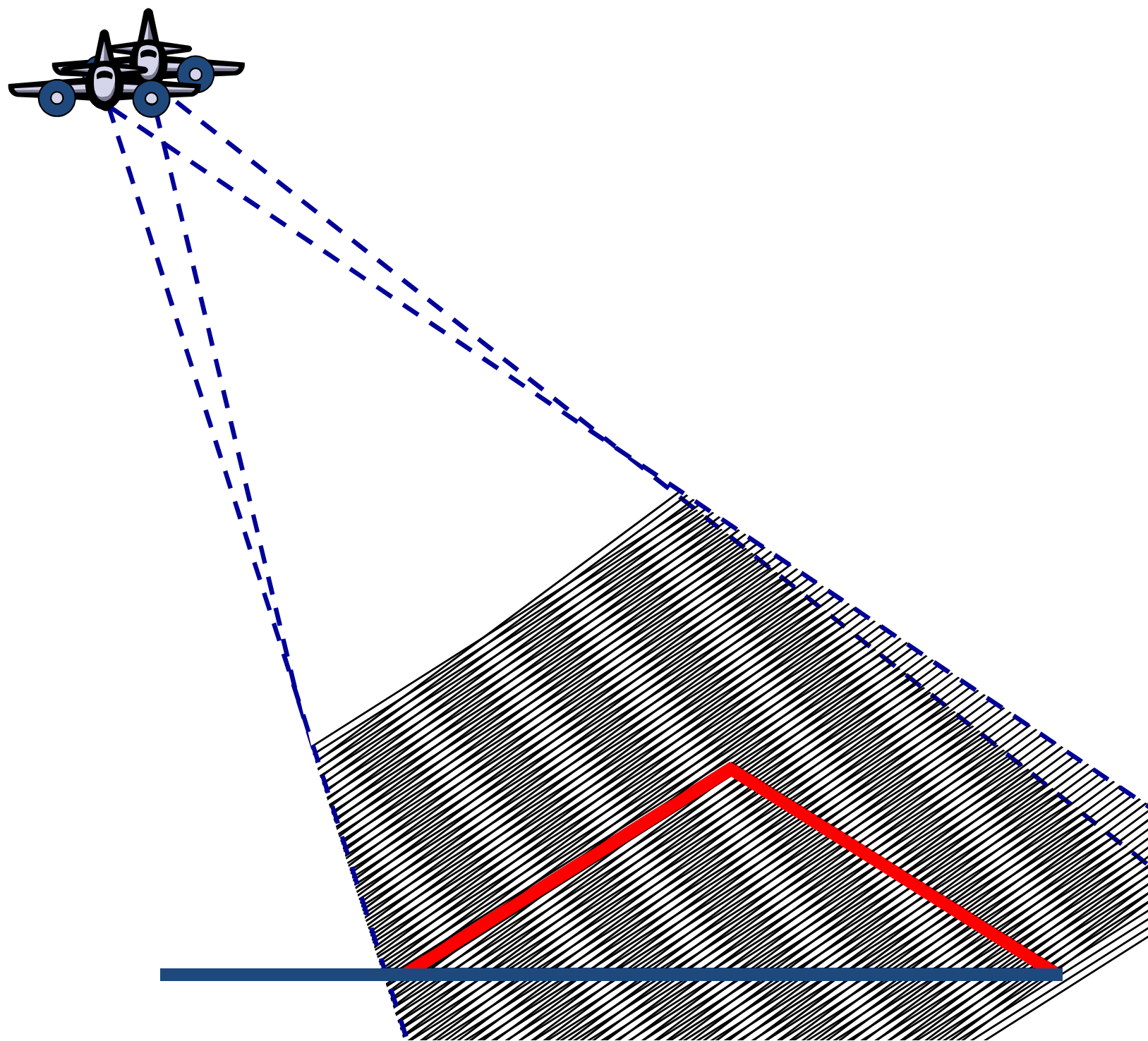
With respect to flat terrain, **the spatial frequency** of the interference pattern

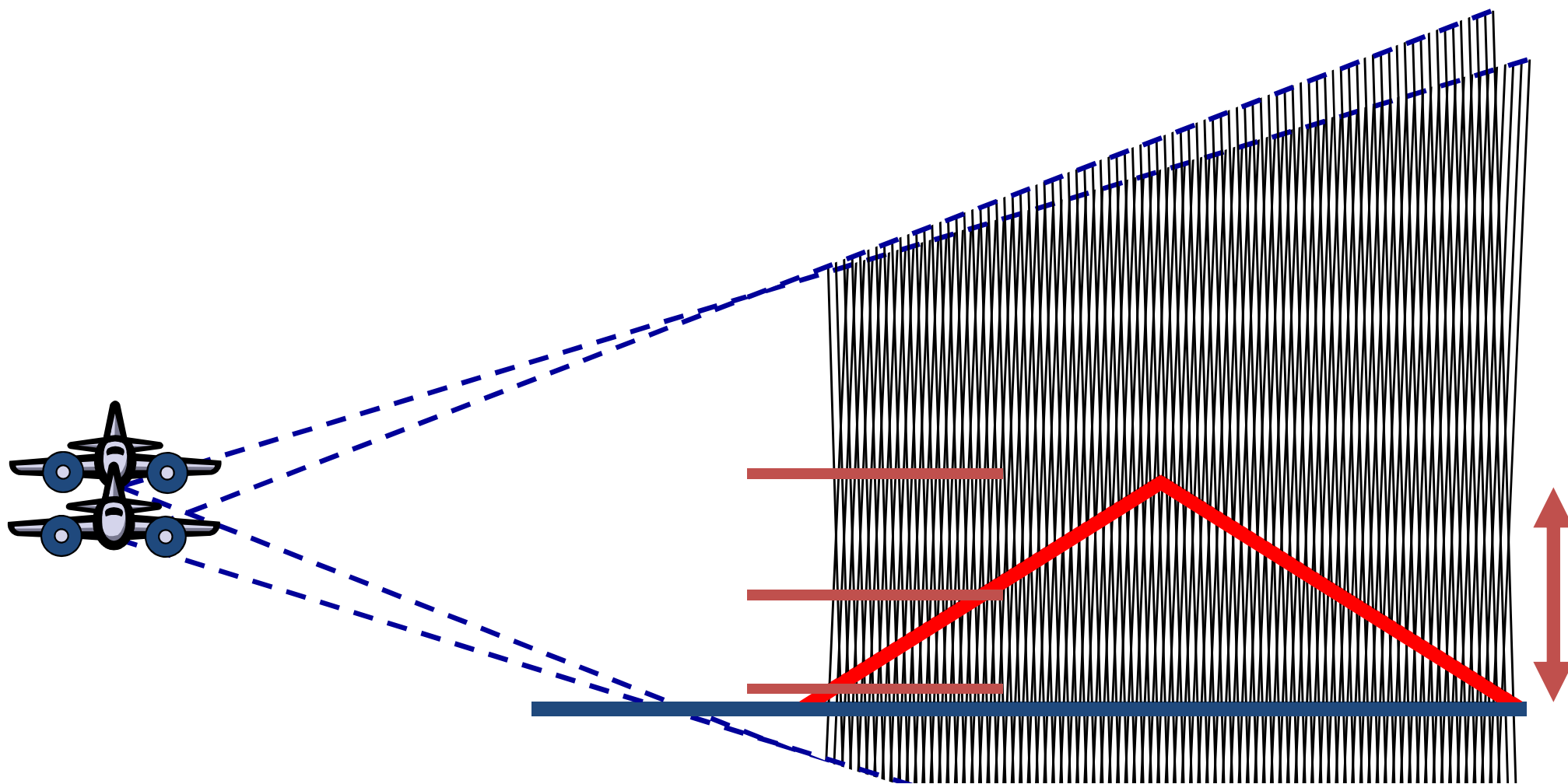
- **increases at positive slopes and,**
- **decreases at negative slopes**



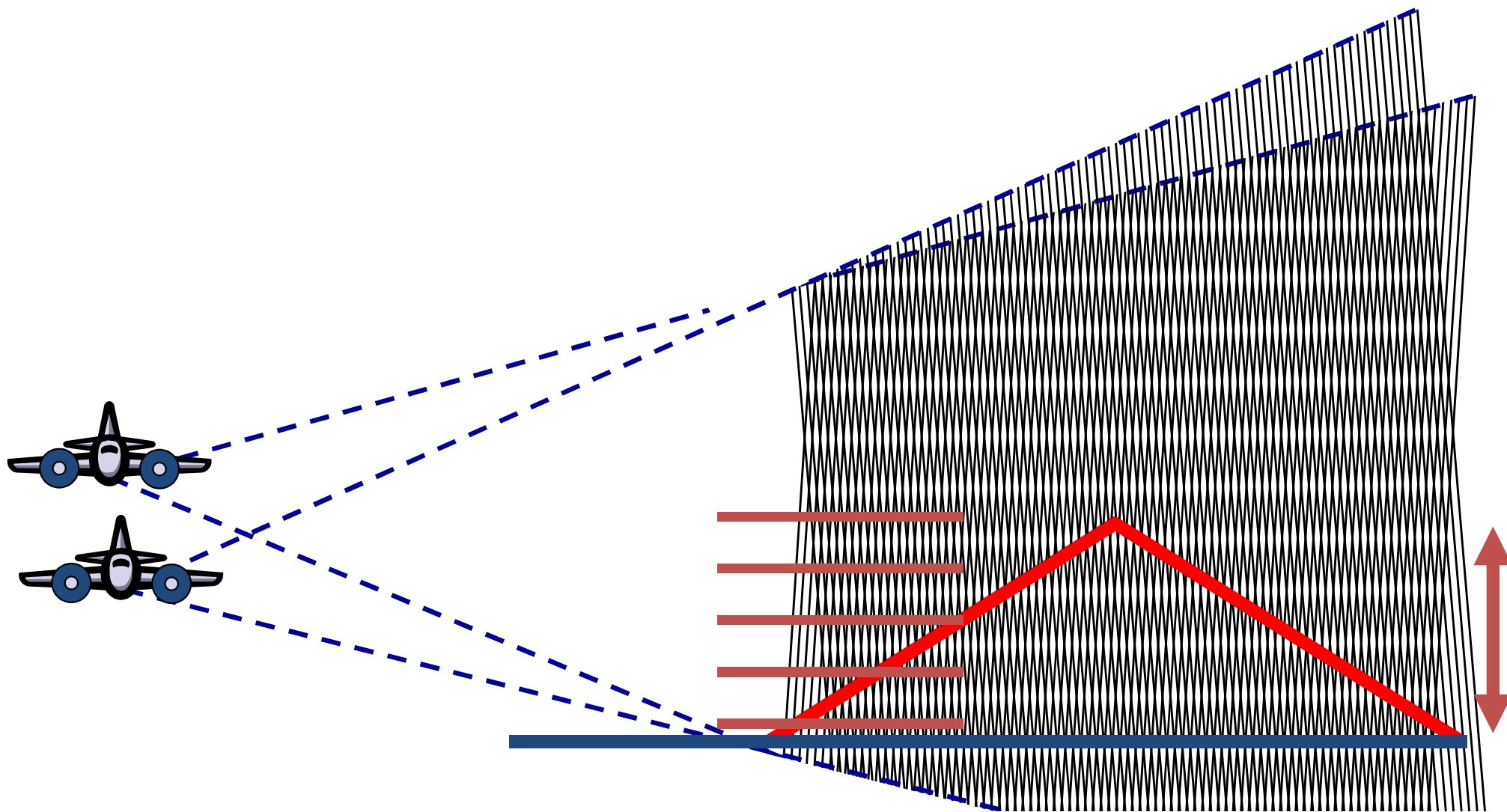


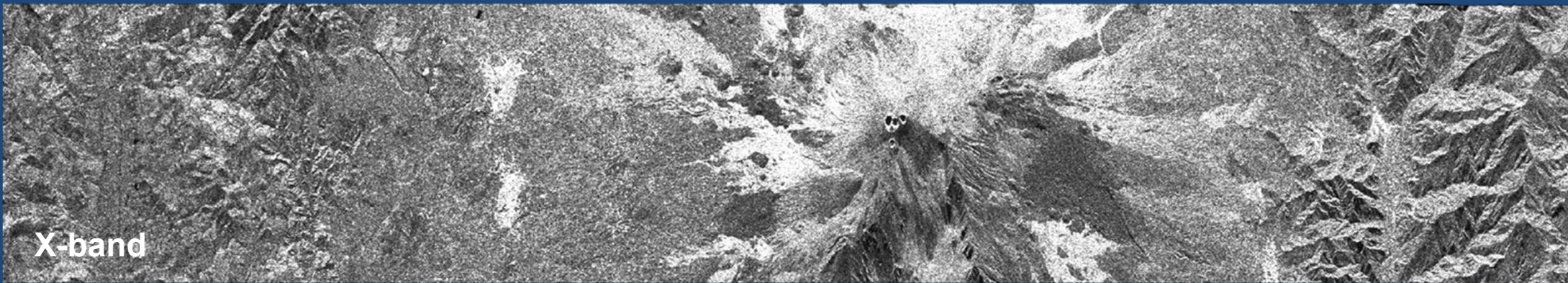






The Phase-to-Height Sensitivity increases with increasing the spatial baseline (i.e. $\Delta\theta$ or $B\theta$);





Amplitude Images



24 Hours Temporal Baseline

SIR-C / Test Site: Mt. Etna, Italy



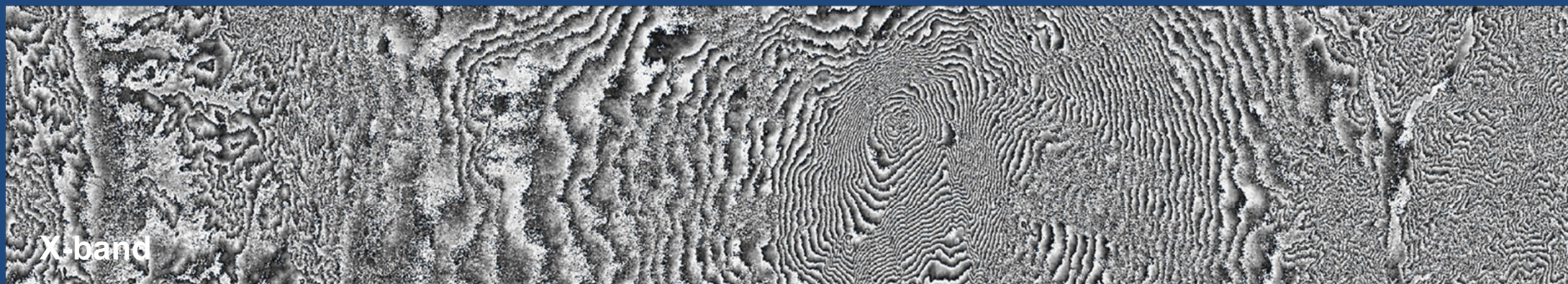
X-band

Phase Images

C-band

SIR-C / Test Site: Mt. Etna, Italy

L-band

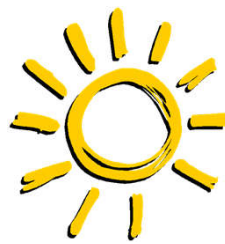


Phase Images



SIR-C / Test Site: Mt. Etna, Italy





Interferometric Coherence

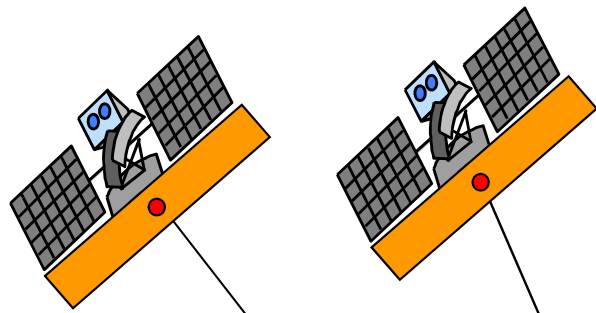


Image 1: $i_1 = |i_1| \exp[-i(2\frac{2\pi}{\lambda}R_1) + \varphi_{S1}]$

Image 2: $i_2 = |i_2| \exp[-i(2\frac{2\pi}{\lambda}R_2) + \varphi_{S2}]$

Interferometric Coherence: Normalised Complex Correlation Coefficient

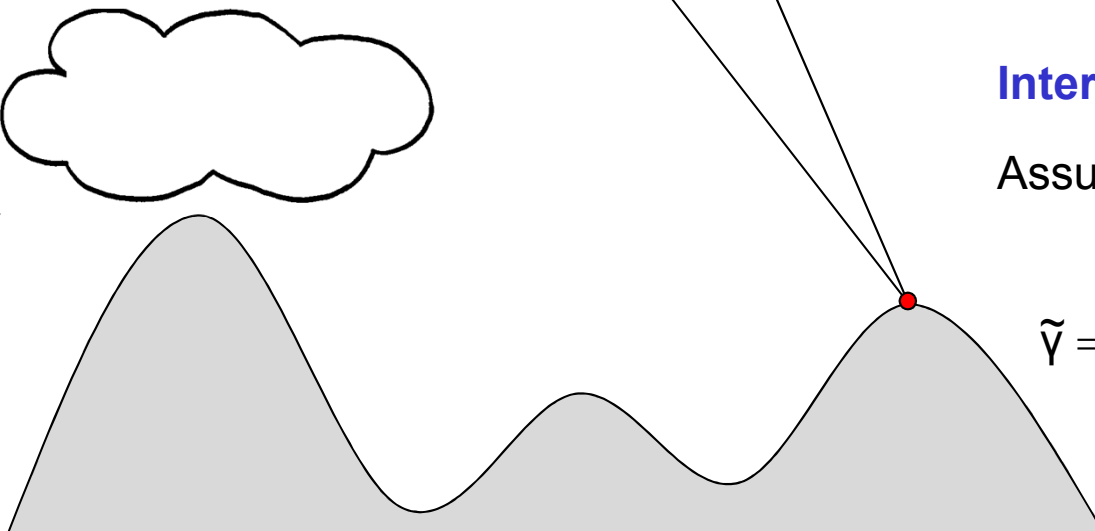
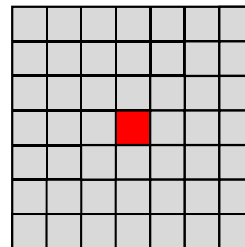
$$\tilde{\gamma} = \frac{E\{i_1 i_2^*\}}{\sqrt{E\{i_1 i_1^*\} E\{i_2 i_2^*\}}} = \frac{|E\{i_1 i_2^*\}| \exp(i\varphi)}{\sqrt{E\{|i_1|^2\} E\{|i_2|^2\}}} \quad 0 \leq |\tilde{\gamma}| \leq 1$$

Interferometric Coherence Estimation:

Assuming stationarity within the estimation window:

$$\tilde{\gamma} = \frac{\sum_W i_1[i,j] i_2^*[i,j]}{\sqrt{\sum_W |i_1[i,j]|^2 \sum_W |i_2[i,j]|^2}} = \frac{\langle i_1 i_2^* \rangle}{\sqrt{\langle i_1 i_1^* \rangle \langle i_2 i_2^* \rangle}}$$

Typical window size: 10 (3x3) – >100 pixels



InSAR Coherence

... is a measure of interferogram quality:

Standard Deviation of the InSAR Phase φ :

$$\sigma_{\varphi} = \sqrt{\int_{-\pi}^{\pi} \varphi^2 \text{pdf}(\varphi) \cdot d\varphi}$$

depends on ► the underlying coherence &
► the number of looks N.

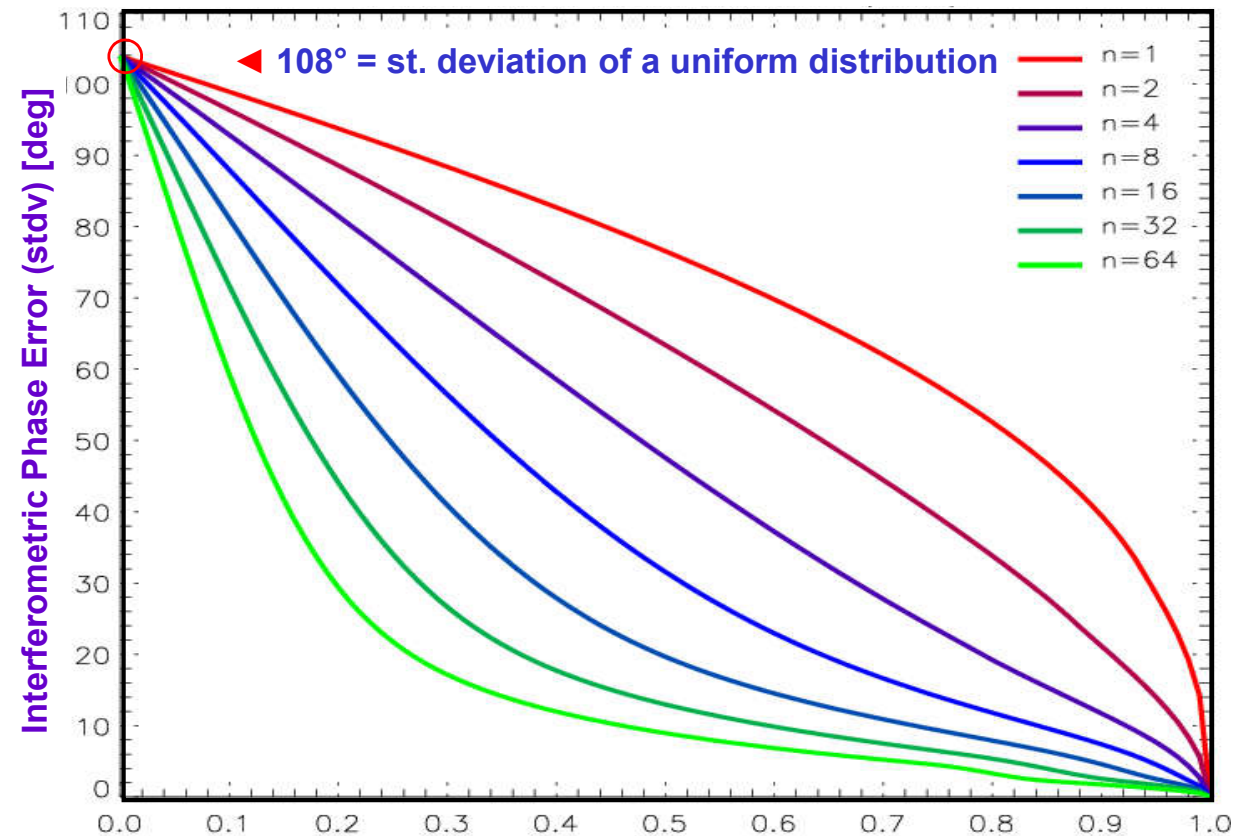
An increase in decorrelation (= loss in coherence) is associated with an increase in the phase variance;

► Increased phase variance leads to increased height errors.

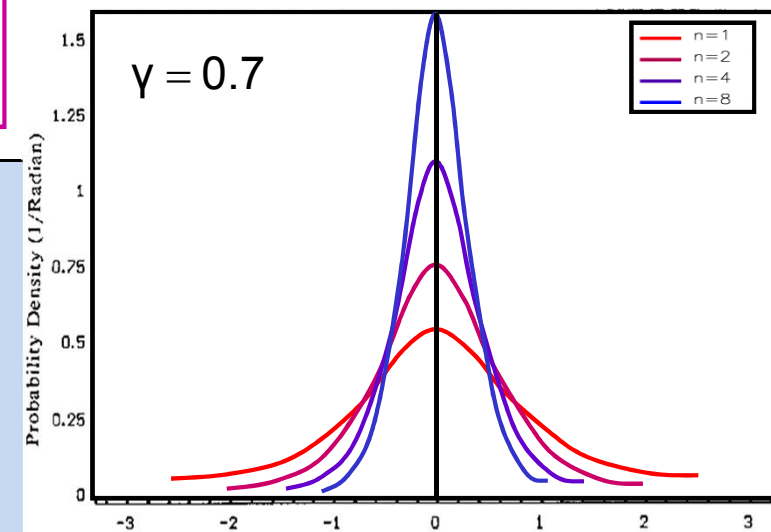
where: $\text{pdf}(\varphi, N) = \frac{\Gamma(N + 1/2)(1 - |\gamma|^2)^2 \beta}{2\sqrt{\pi}\Gamma(N)(1 - \beta^2)^{N+1/2}} + \frac{(1 - |\gamma|^2)^N}{2\pi} F(N, 1; 1/2; \beta^2)$

► F is a Gauss hypergeometric function and $\beta = |\gamma| \cos(\varphi - \bar{\varphi})$

► N is the number of Looks

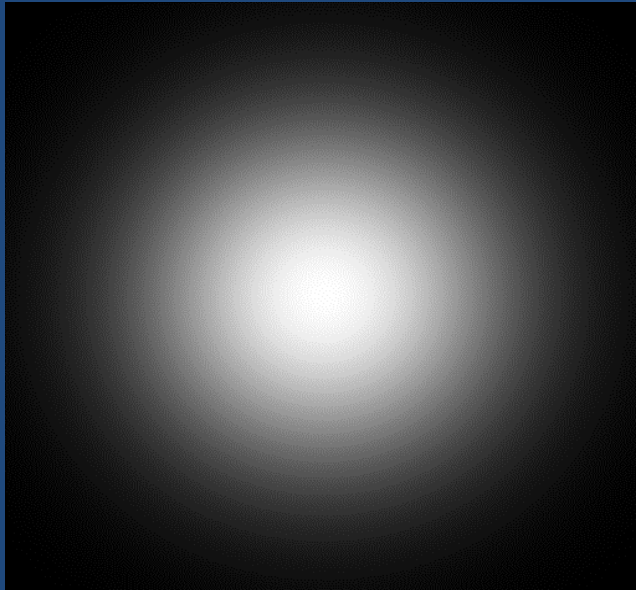


Interferometric Coherence

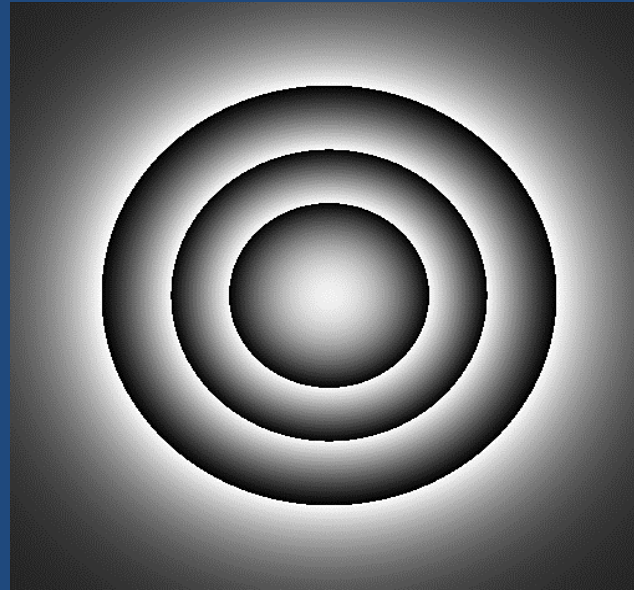


Interferometric Phase Images

Simulation

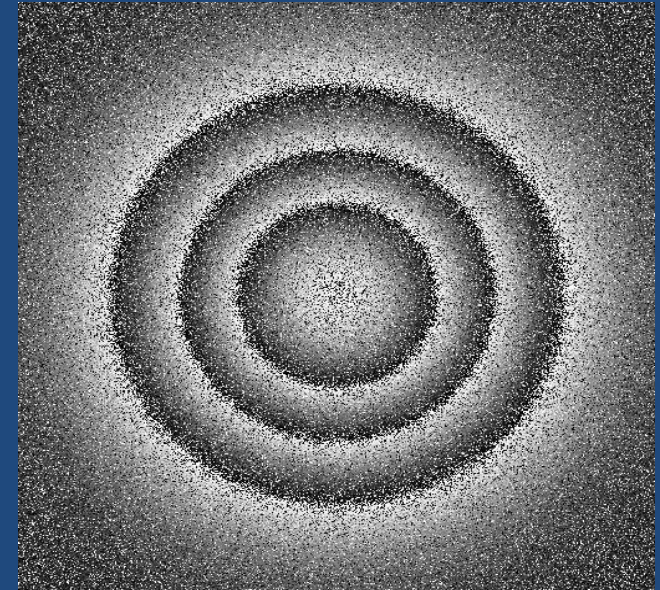


Absolute Phase



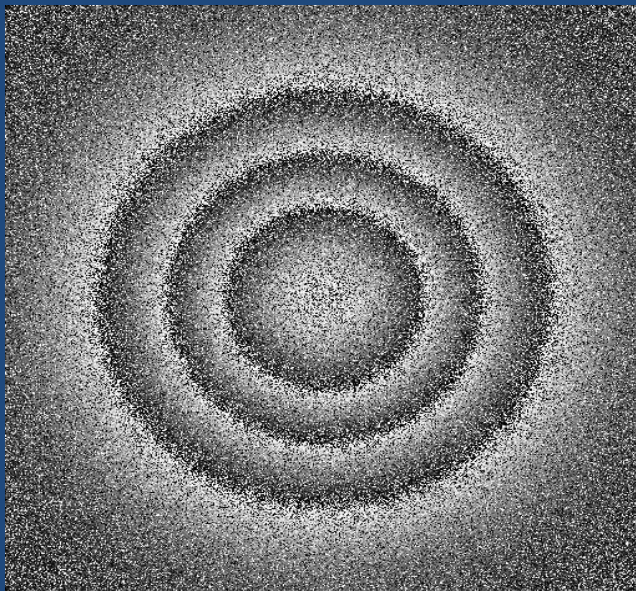
Coherence=1.0

Looks=1



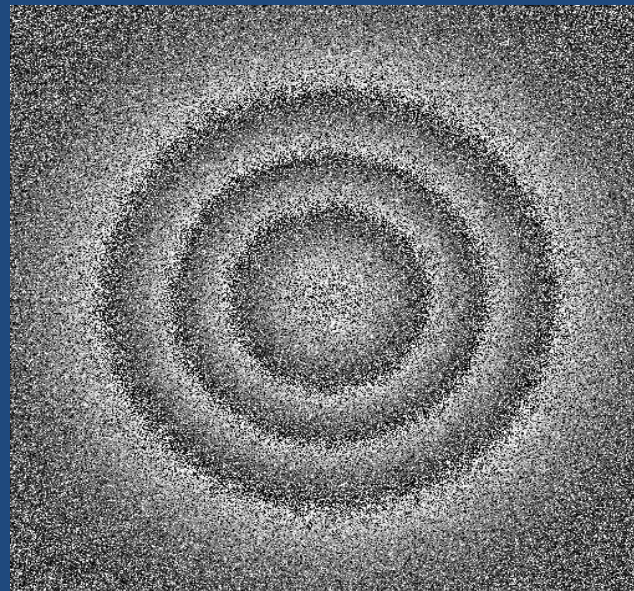
Coherence=0.8

Looks=1



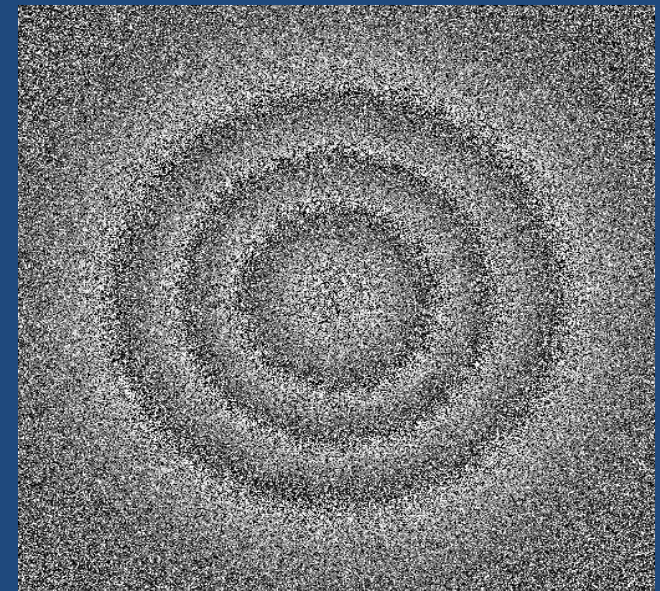
Coherence=0.6

Looks=1



Coherence=0.4

Looks=1



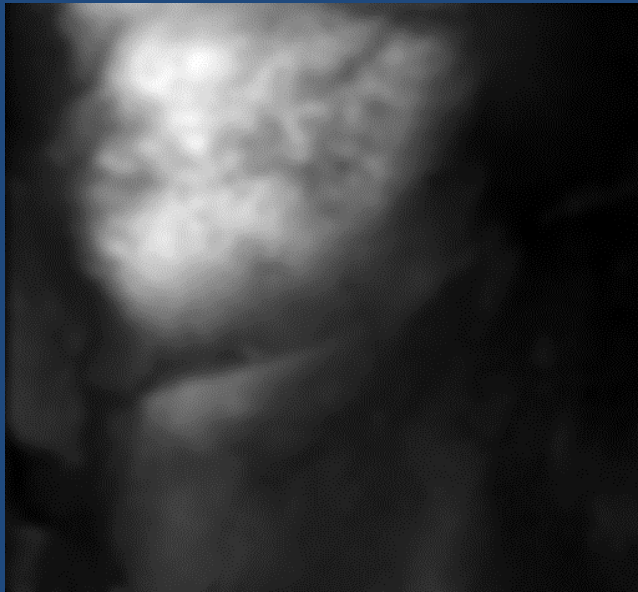
Coherence=0.2

Looks=1

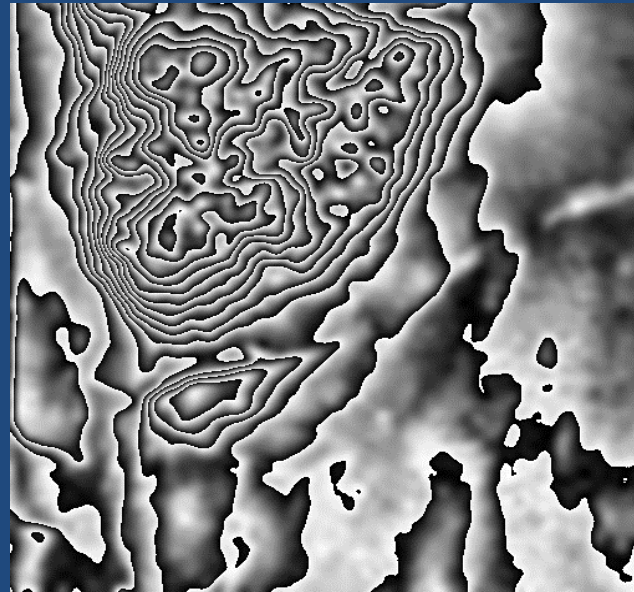


Interferometric Phase Images

Simulation

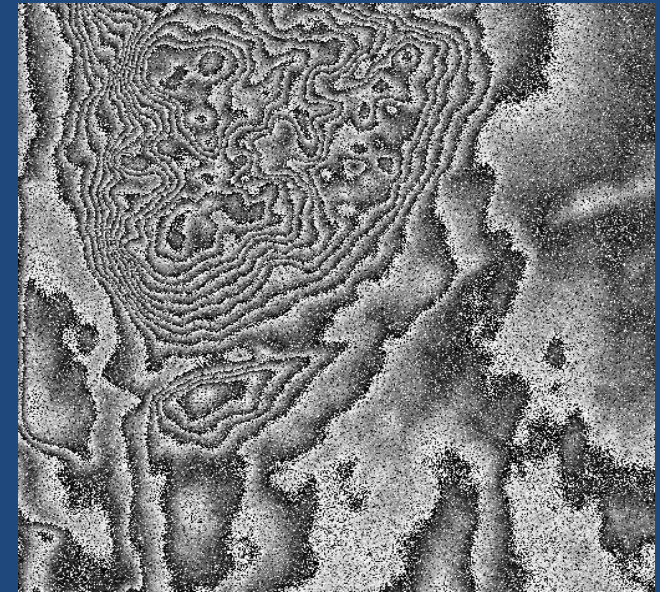


Absolute Phase



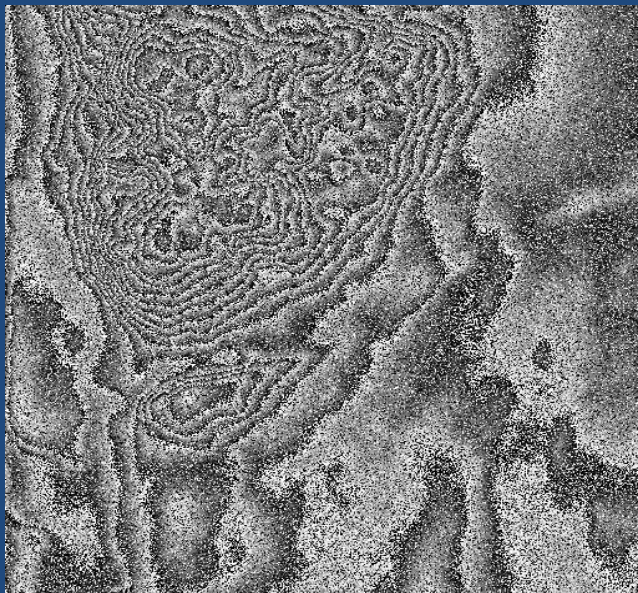
Coherence=1.0

Looks=1



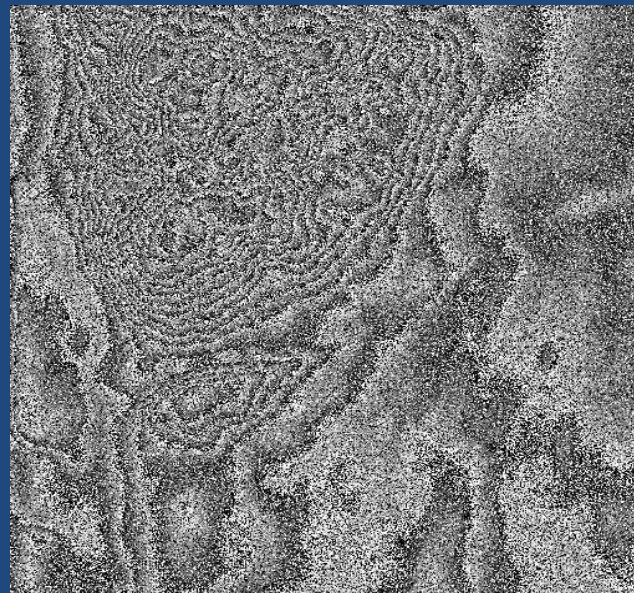
Coherence=0.8

Looks=1



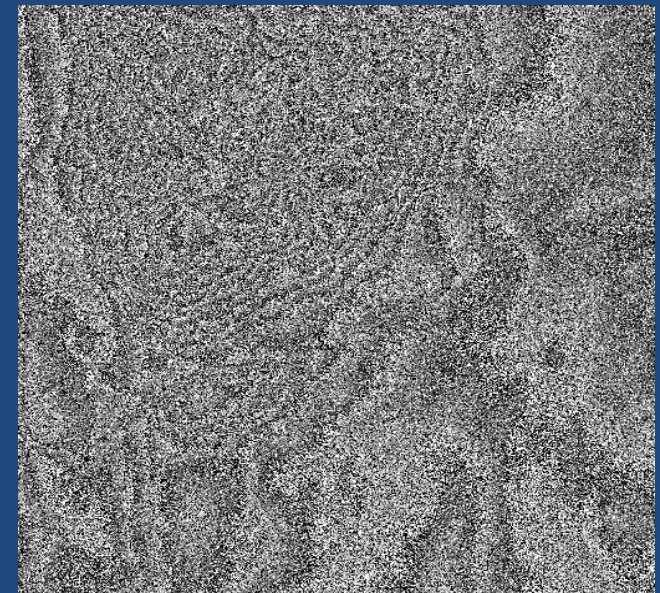
Coherence=0.6

Looks=1



Coherence=0.4

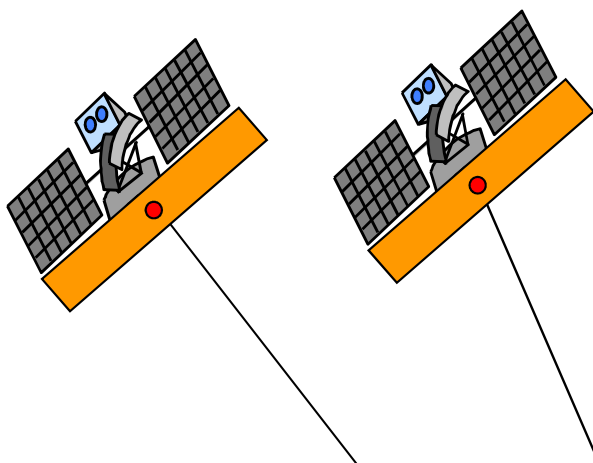
Looks=1



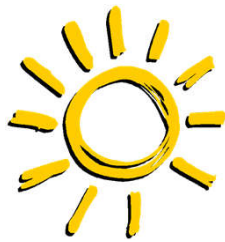
Coherence=0.2

Looks=1





Repeat-Pass SAR Interferometry



The interferometric images are acquired at different times

... the so called temporal baseline may range from seconds to years

Signal from P in Image 1 @ time t_1 :

$$i_1 = |i_1| \exp[-i(2\frac{2\pi}{\lambda}R_1) + \varphi_S(t_1) + \varphi_{\text{Prop}}(t_1)]$$

Signal from P in Image 2 @ time t_2 :

$$i_2 = |i_2| \exp[-i(2\frac{2\pi}{\lambda}R_2) + \varphi_S(t_2) + \varphi_{\text{Prop}}(t_2)]$$

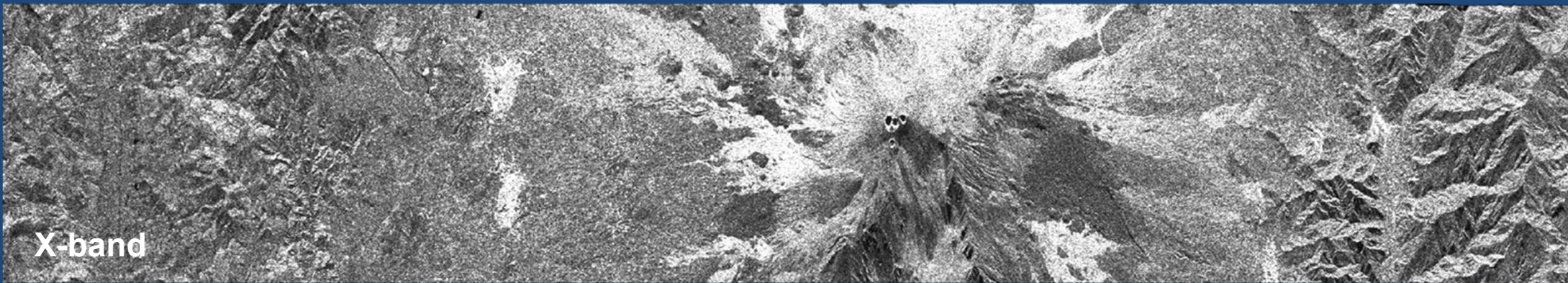
$$R_2 = R_1 + \Delta R$$

R_1



The location of the scatterers in the resolution cell and/or their properties may change in the time between the two acquisitions: $\varphi_S(t_1) \neq \varphi_S(t_2)$ **Temporal decorrelation**

The phase induced by the propagation medium (atmosphere or ionosphere) varies in the time between the two acquisitions: $\varphi_{\text{Prop}}(t_1) \neq \varphi_{\text{Prop}}(t_2)$



Amplitude Images



24 Hours Temporal Baseline

SIR-C / Test Site: Mt. Etna, Italy



A grayscale coherence image of a mountainous terrain, likely Mt. Etna, captured in the X-band. The image shows a complex pattern of light and dark patches, indicating varying surface roughness and structural coherence. The texture is highly detailed, with many small-scale features visible.

X-band

Coherence Images

A grayscale coherence image of the same mountainous terrain as the X-band image, but captured in the C-band. The coherence pattern is different, with larger, more distinct light and dark regions, reflecting the longer wavelength of the C-band radar.

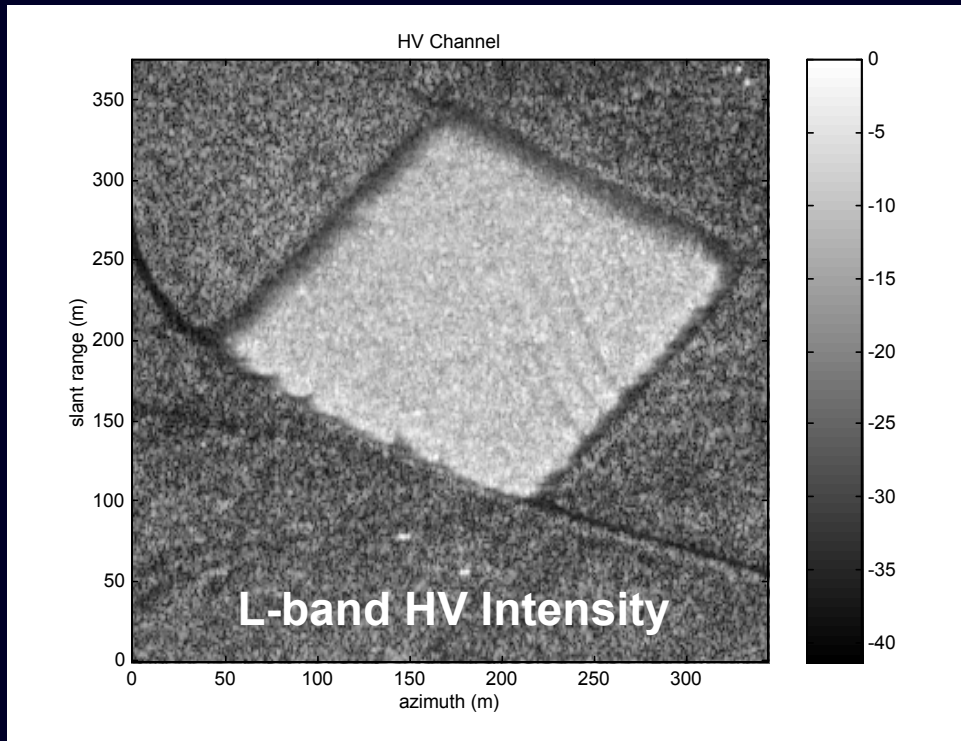
C-band

SIR-C / Test Site: Mt. Etna, Italy

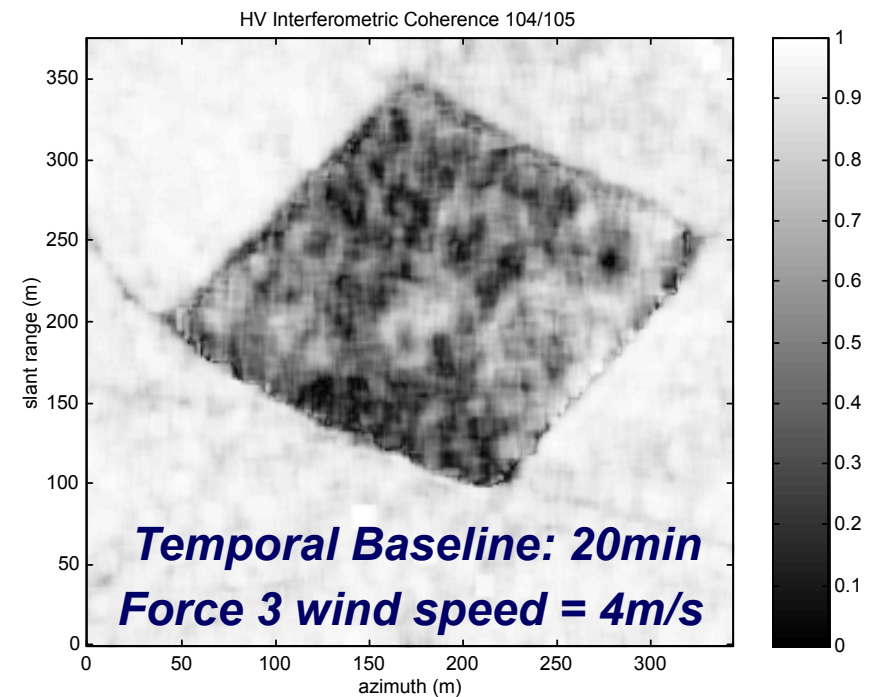
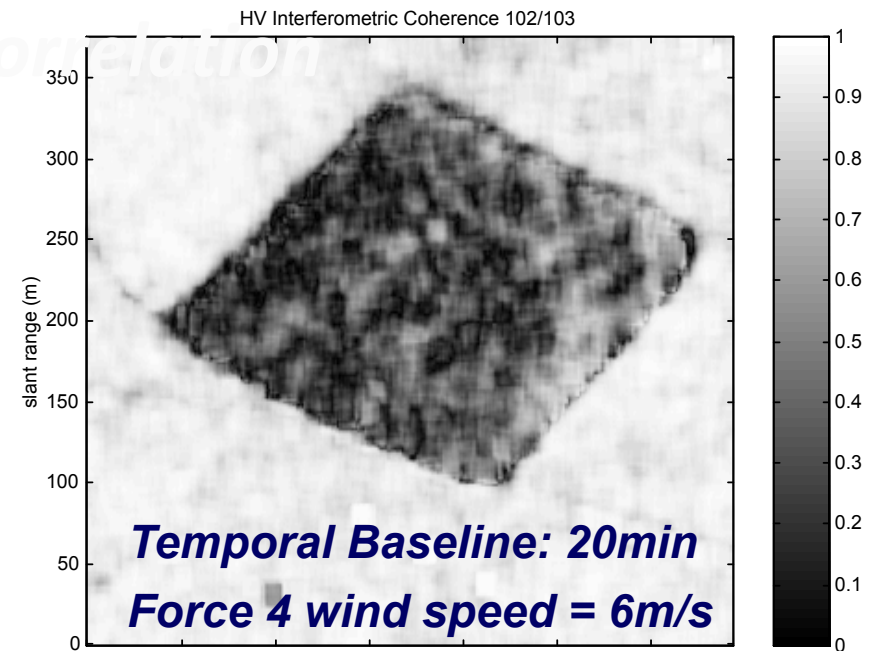
A grayscale coherence image of the same mountainous terrain, captured in the L-band. This image shows the most significant coherence, with large, smooth, light-colored areas and fewer dark patches, indicating that the longer wavelength of the L-band is less sensitive to small-scale surface features.

L-band

Temporal Decorrelation



E-SAR / Test Site: Fox Covert, England

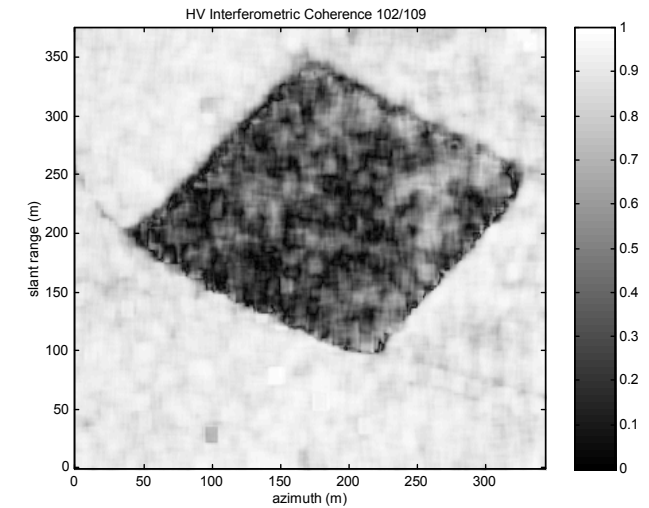
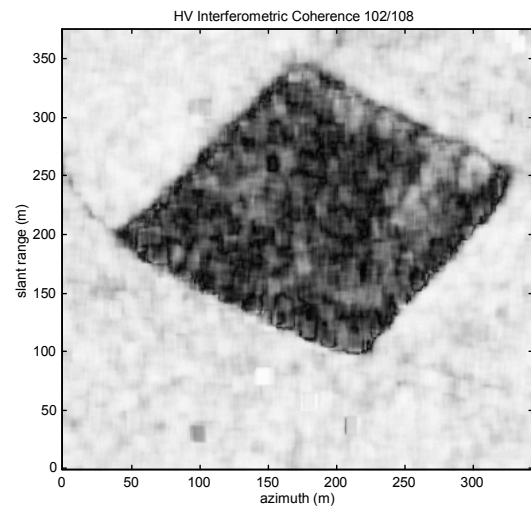
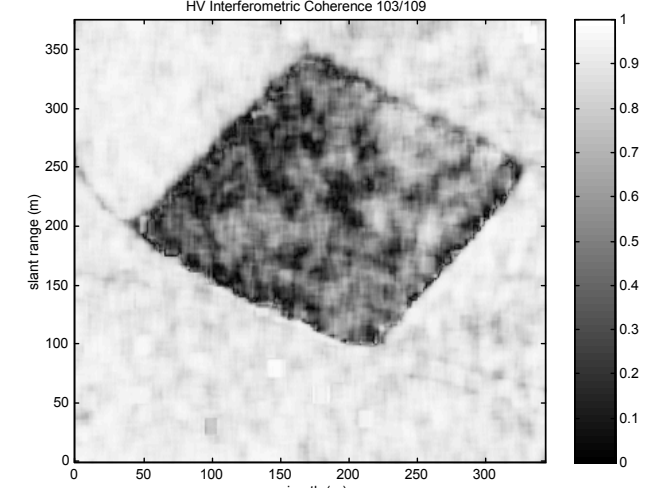
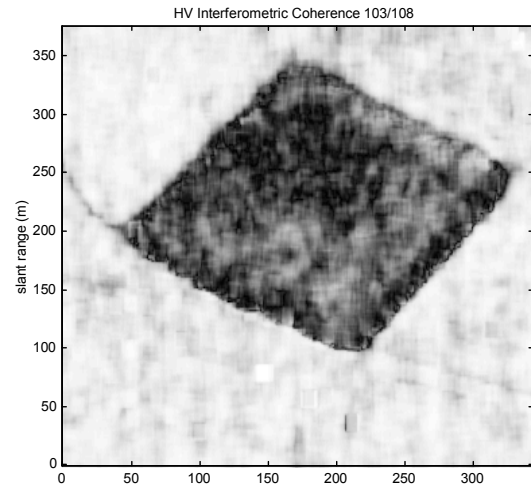
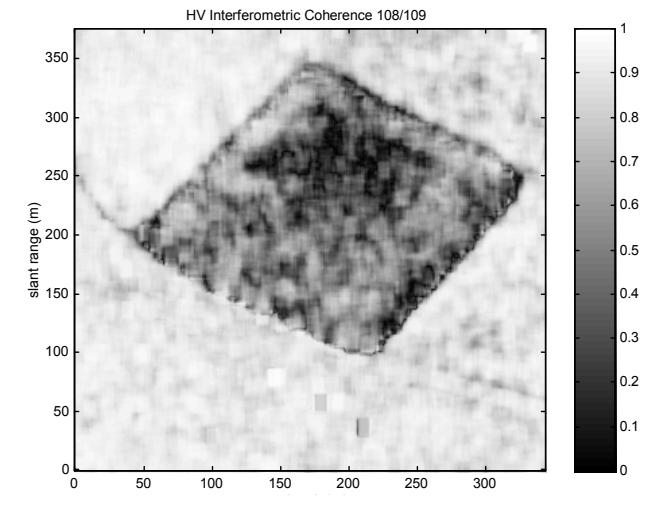
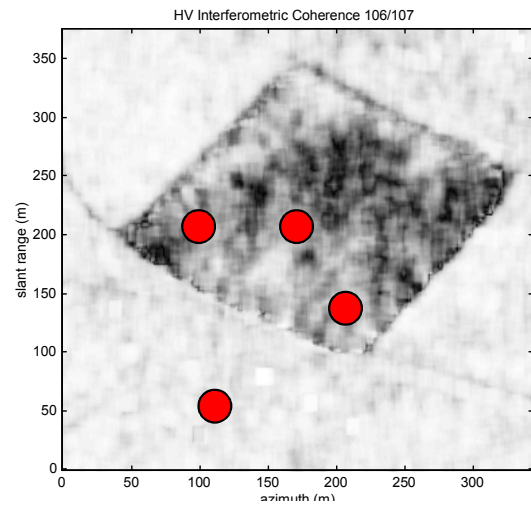
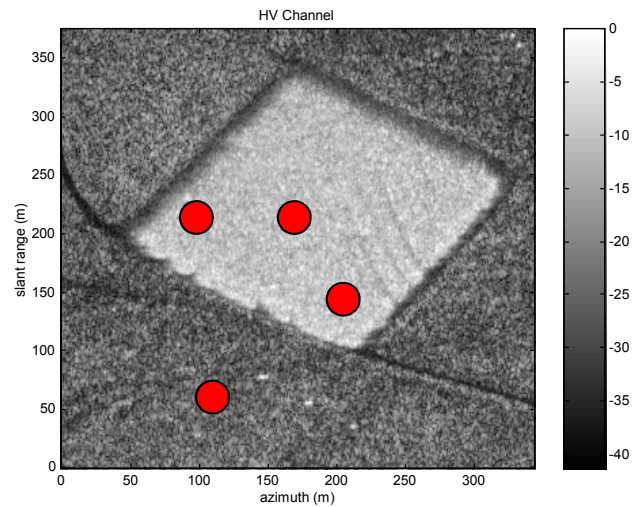


Earth Observation and
Remote Sensing

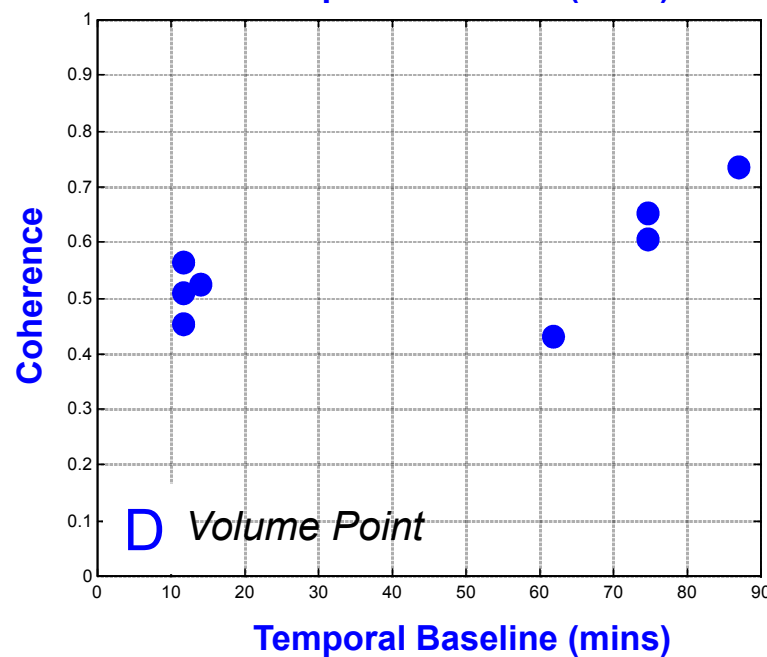
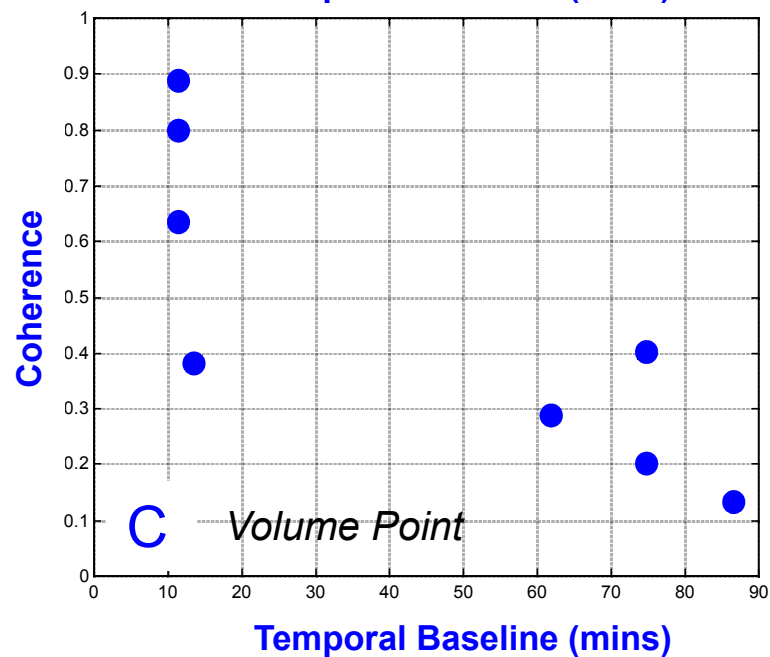
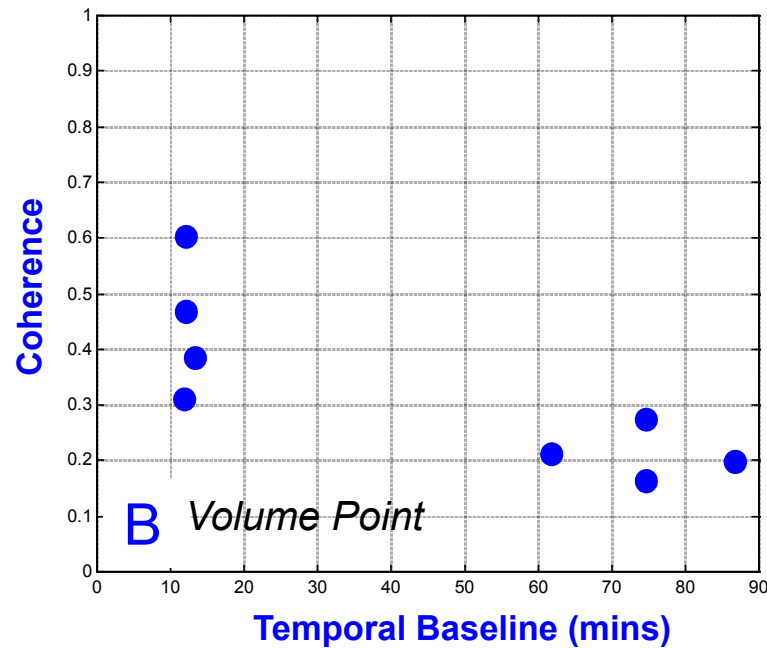
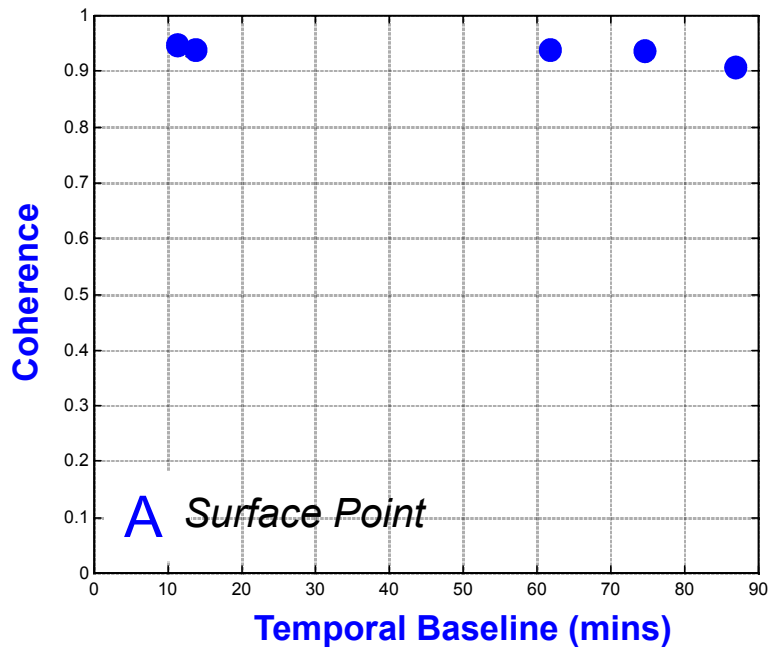
hajnsek@ifu.baug.ethz.ch
irena.hajnsek@dlr.de

Temporal Decorrelation

E-SAR / Test Site: Fox Covert, England

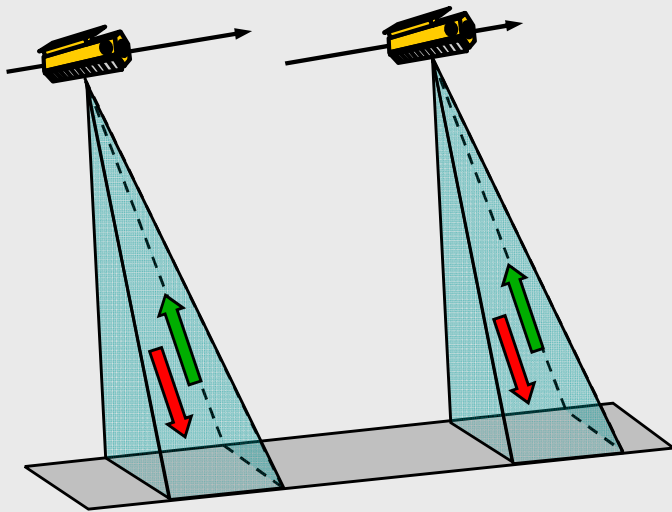


Forest Height Estimation – Decorrelation Effects



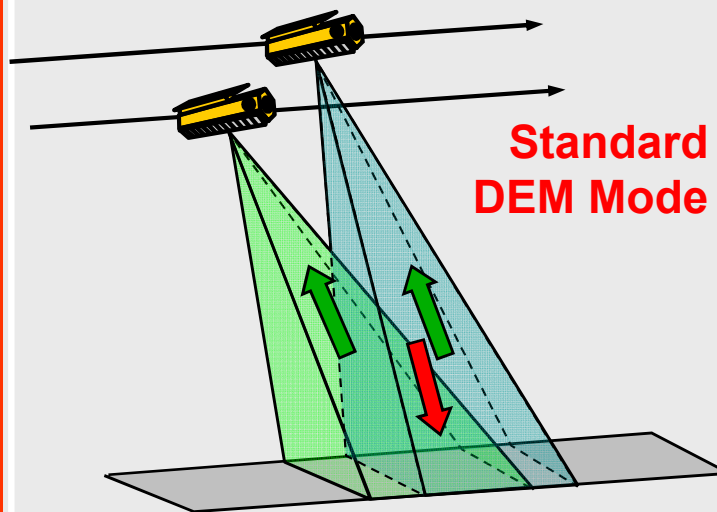
TanDEM-X Data Acquisition Modes

Pursuit Monostatic



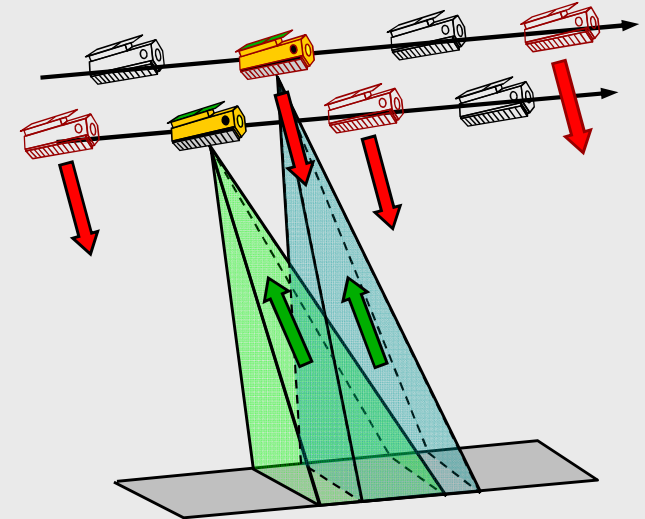
- both satellites transmit and receive independently
- susceptible to temporal decorrelation and atmospheric disturbances
- no PRF and phase synchronisation required (backup solution)

Bistatic



- one satellite transmits and both satellites receive simultaneously
- small along-track displacement required for Doppler spectra overlap
- requires PRF and phase synchronisation

Alternating Bistatic



- transmitter alternates between PRF pulses
- provides three interferograms with two baselines in a single pass
- enables precise phase synchronisation, calibration & verification

TSX-TDX Monostatic Mission Phase



Test Site Mawas / Borneo

24.07.2010 HH Pol / Baseline: 38m

04.08. 2010 HH Pol / Baseline: 35m

06.09.2010 HH Pol / Baseline: 54m

TSX-TDX Monostatic Mission Phase

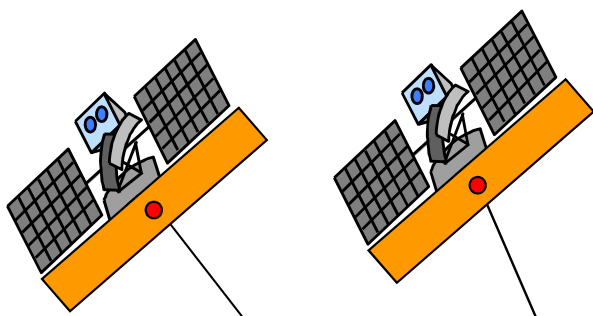
Test Site Mawas / Borneo

24.07.2010 HH Pol Baseline: 38m

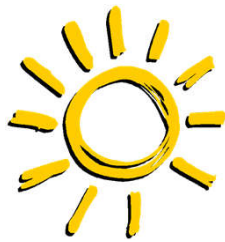
04.08. 2010 HH Pol Baseline: 35m

06.09.2010 HH Pol Baseline: 54m





Single-Pass SAR Interferometry



The interferometric images are acquired at the same time

Signal from P in Image 1 @ time t_1 :

$$i_1 = |i_1| \exp[-i(2\frac{2\pi}{\lambda}R_1) + \varphi_{S1}(t_1) + \varphi_{Prop}(t_1)]$$

$$R_2 = R_1 + \Delta R$$

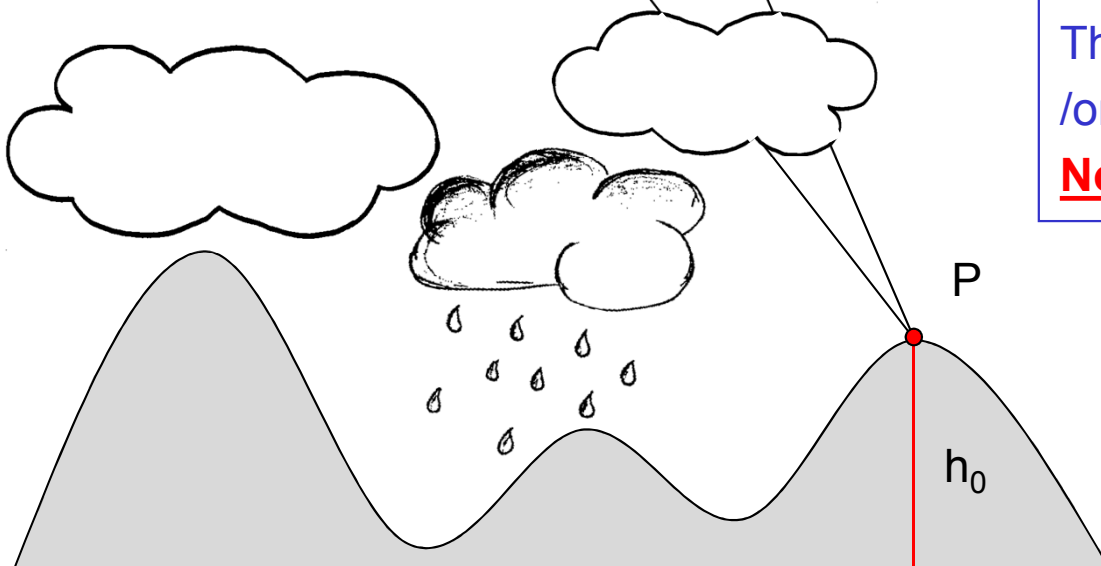
R_1

Signal from P in Image 2 @ time t_2 :

$$i_2 = |i_2| \exp[-i(2\frac{2\pi}{\lambda}R_2) + \varphi_{S1}(t_1) + \varphi_{Prop}(t_1)]$$

The location of the scatterers in the resolution cell and /or their properties are the same for both acquisitions:
No temporal decorrelation

Both signals travel through the same atmosphere and ionosphere): $\varphi_{Prop}(t_1) = \varphi_{Prop}(t_1)$



Earth Observation and
Remote Sensing

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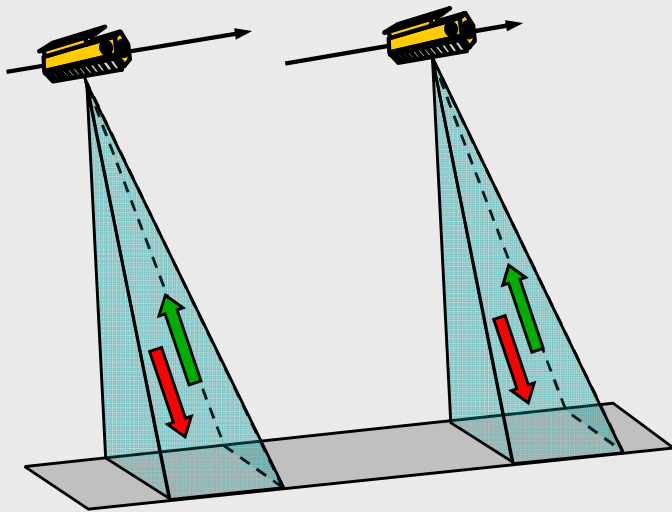
- 43

ETH

Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zurich

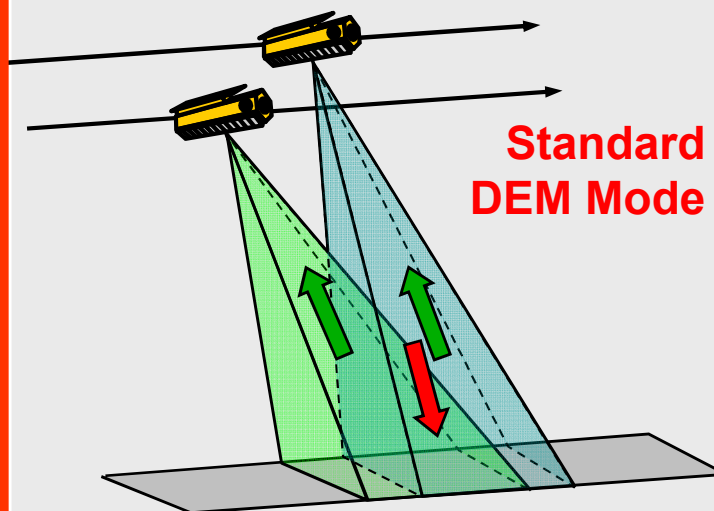
TanDEM-X Data Acquisition Modes

Pursuit Monostatic



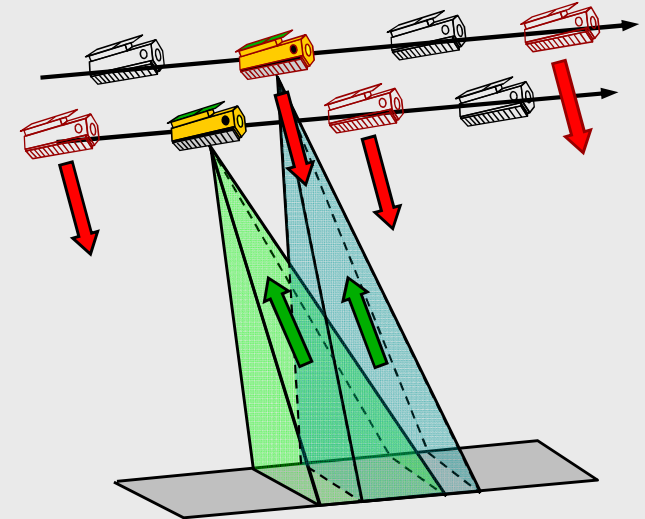
- both satellites transmit and receive independently
- susceptible to temporal decorrelation and atmospheric disturbances
- no PRF and phase synchronisation required (backup solution)

Bistatic



- one satellite transmits and both satellites receive simultaneously
- small along-track displacement required for Doppler spectra overlap
- requires PRF and phase synchronisation

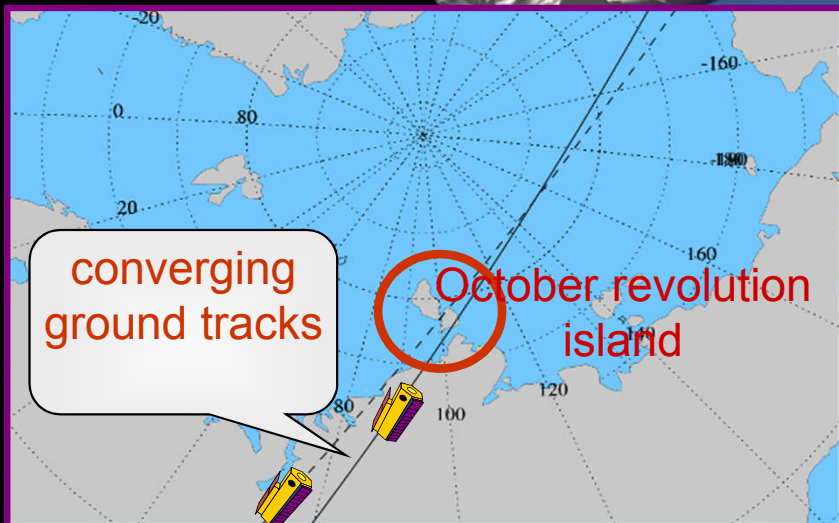
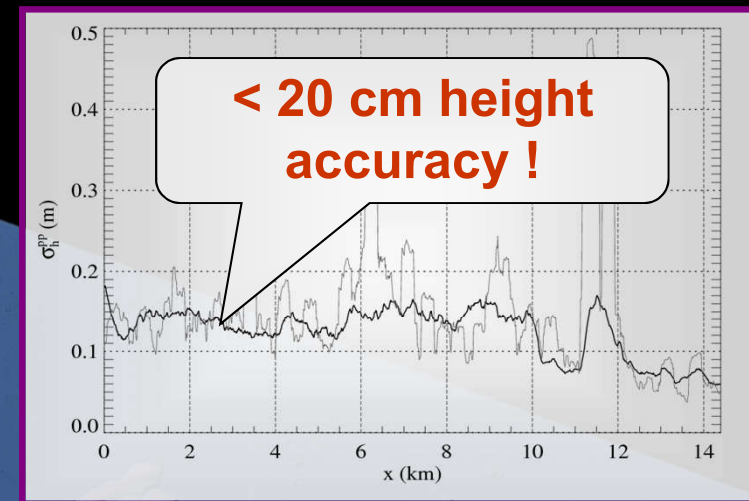
Alternating Bistatic



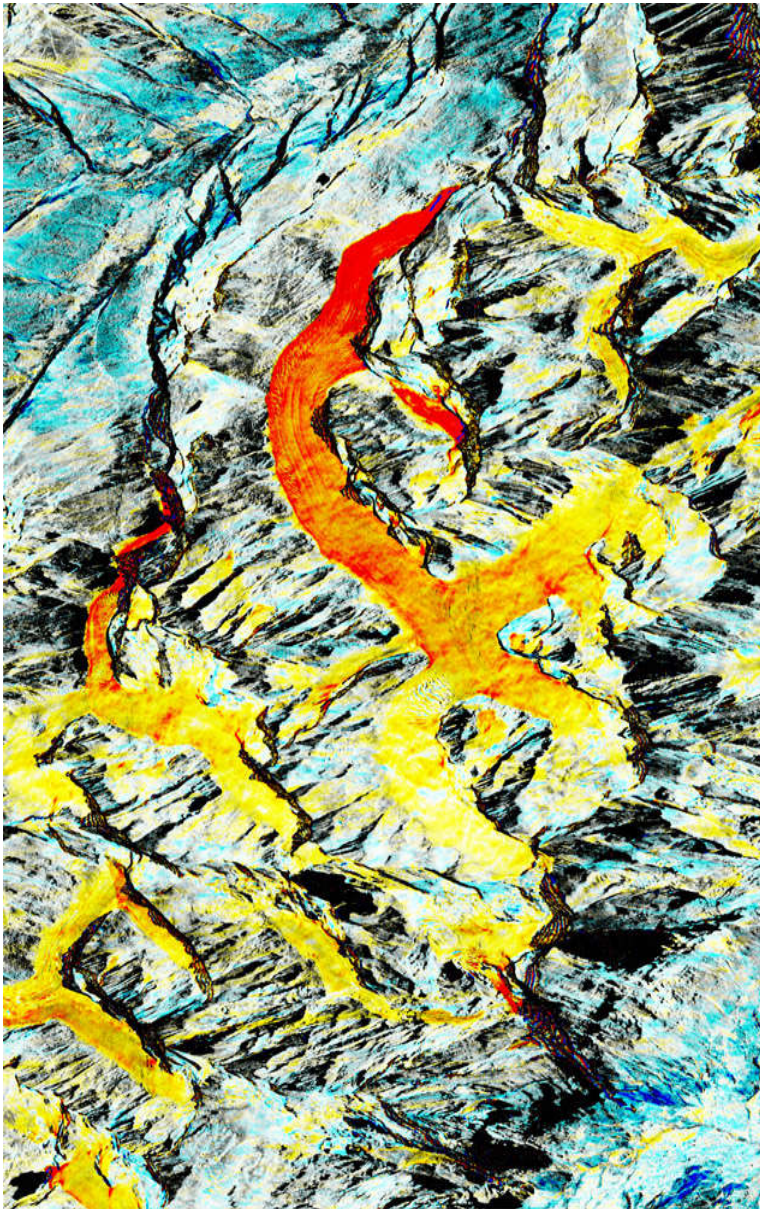
- transmitter alternates between PRF pulses
- provides three interferograms with two baselines in a single pass
- enables precise phase synchronisation, calibration & verification

Large Baseline DEM with TanDEM-X

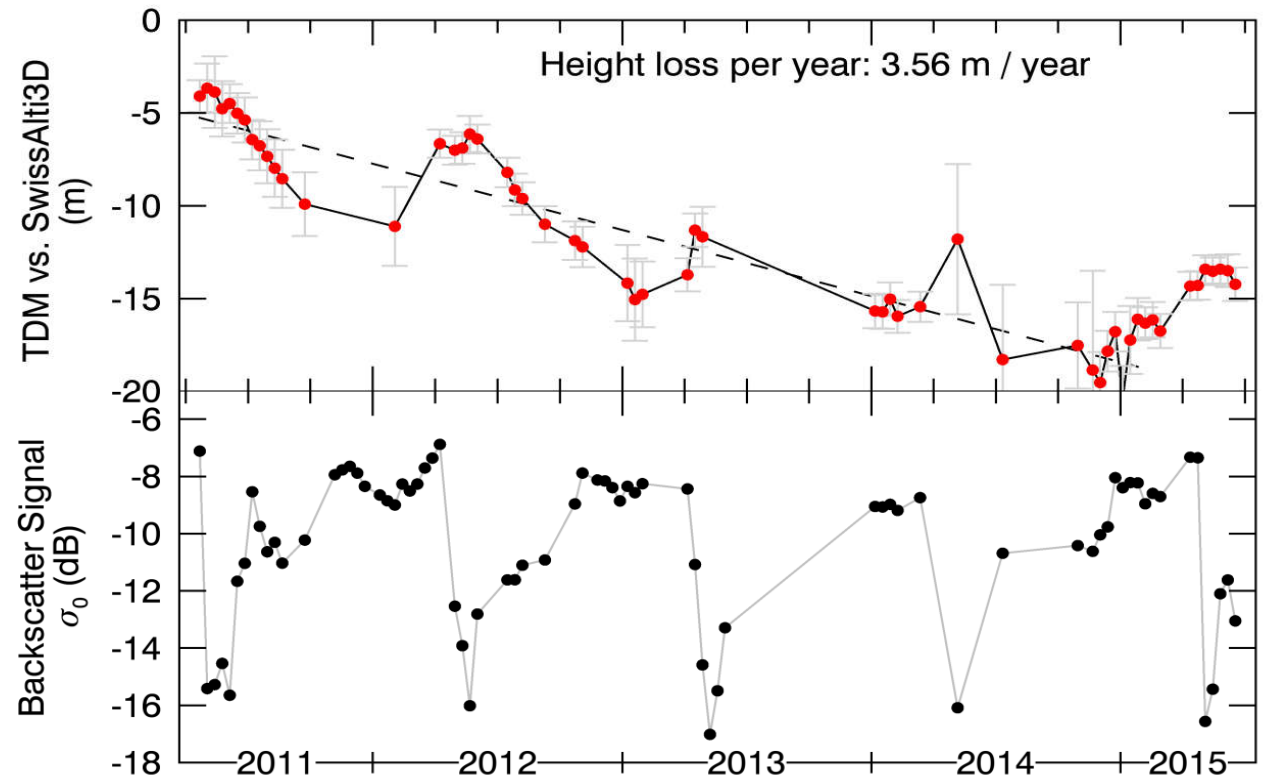
- first TanDEM-X DEM (acquired before reaching 20 km formation)
- large effective baseline (~ 2 km) from Earth rotation
- squint angle ensures coherence



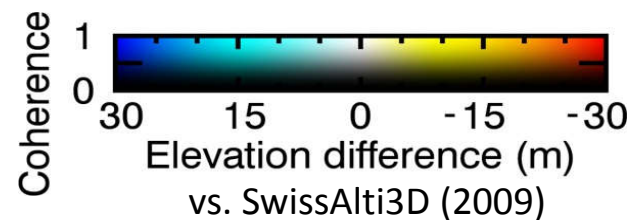
TanDEM-X: Ice loss of Aletschgletscher



00.00.2014

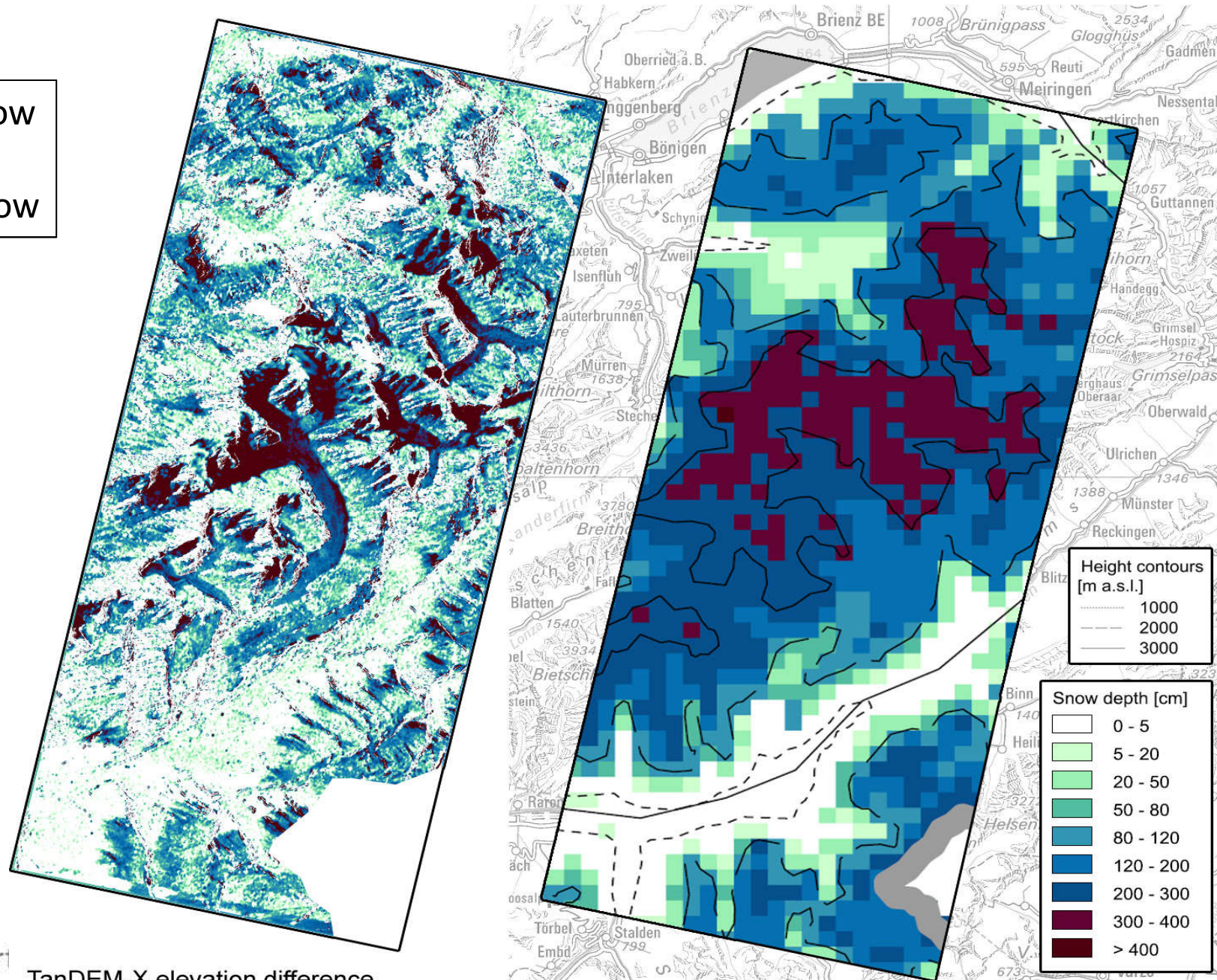


- Results consistent with IceSat data.
- In winter, the apparent elevation stays constant or even decreases(-) during snow accumulation(+) Elevation jumps up at snow melt.



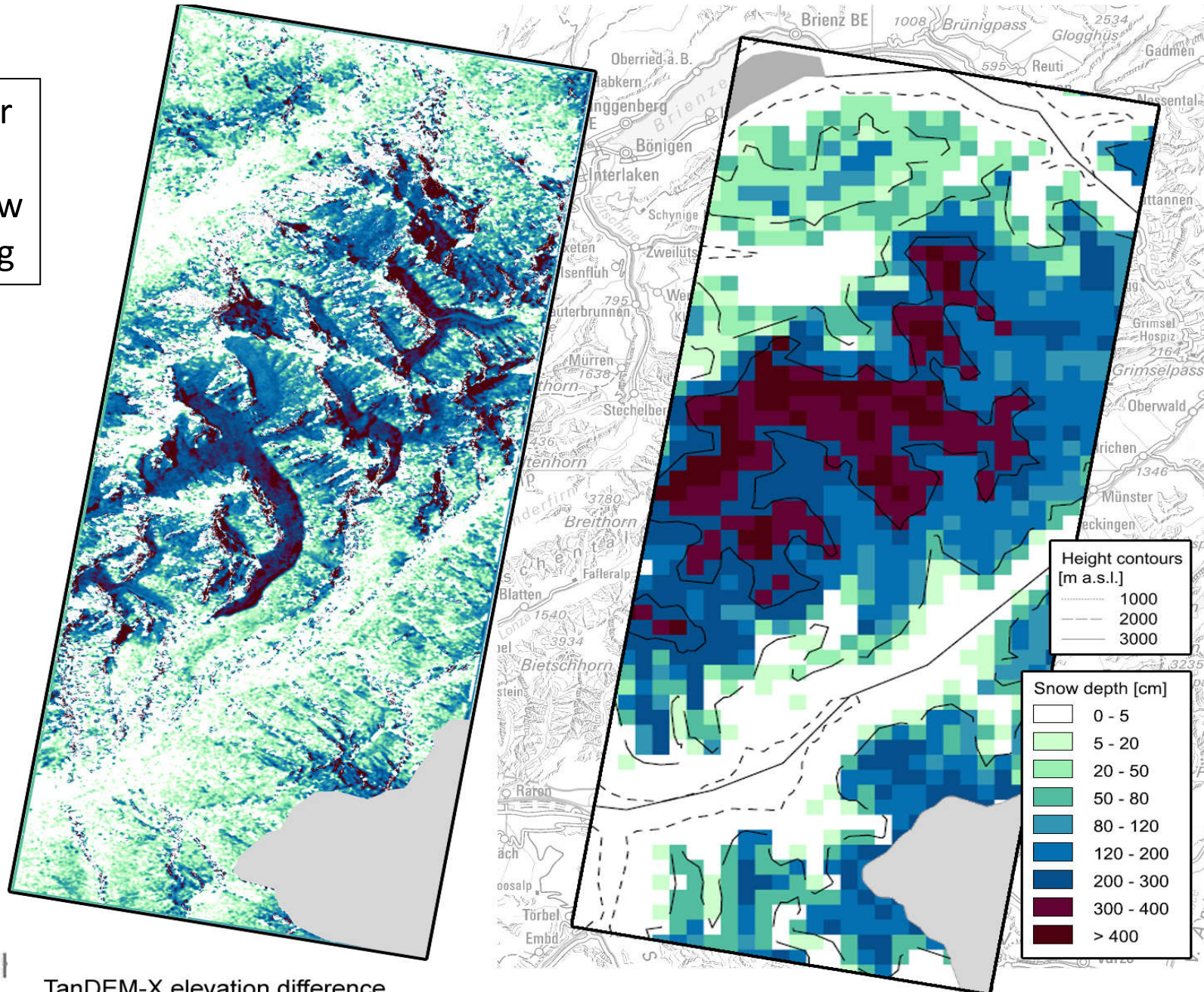
Snow Depth determined by DEM Differencing I

dry snow
vs.
wet snow

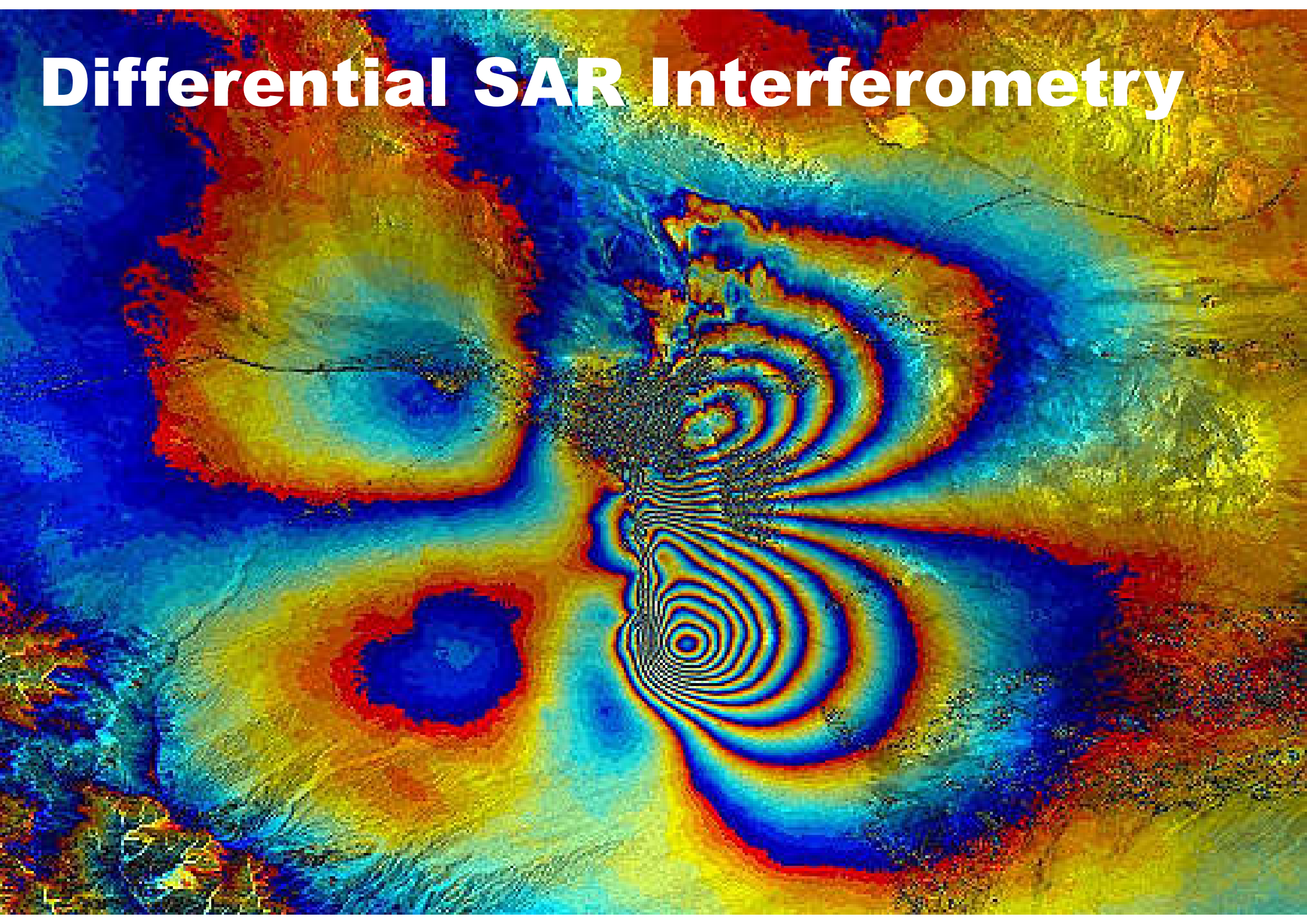


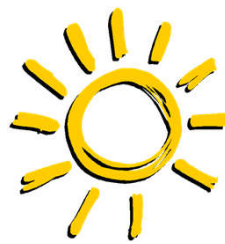
Snow Depth determined by DEM Differencing II

summer
vs.
wet snow
in spring



Differential SAR Interferometry





SAR Interferometry

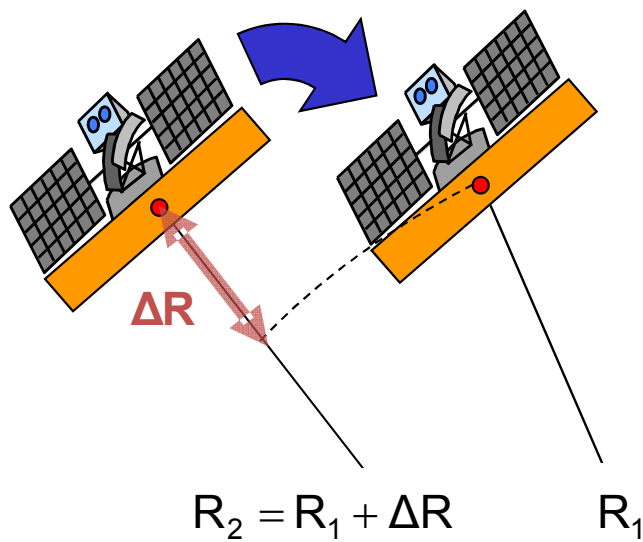


Image 1: $i_1 = |i_1| \exp[-i(2\frac{2\pi}{\lambda}R_1) + \varphi_{s1}]$

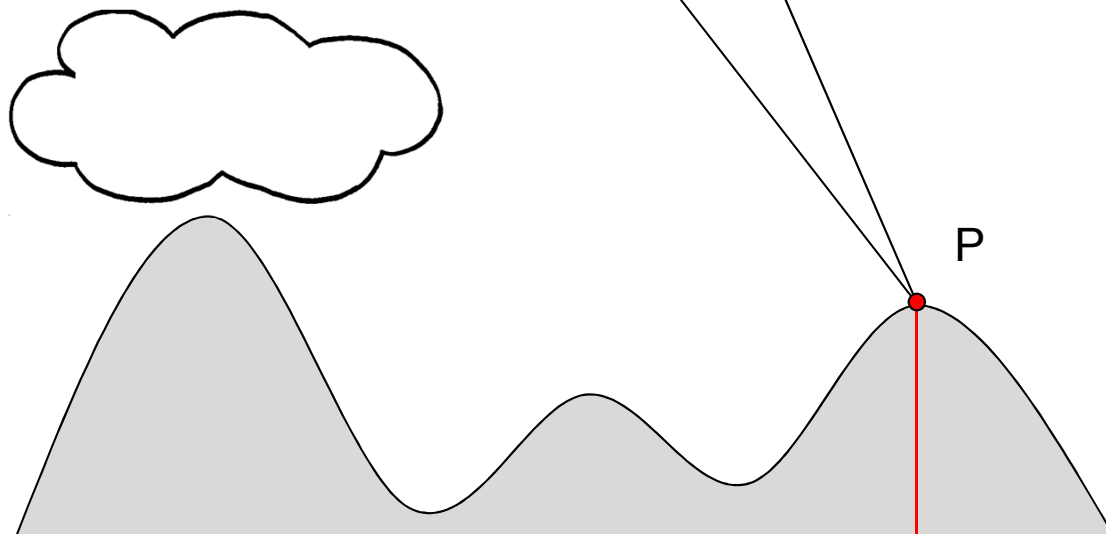
Image 2: $i_2 = |i_2| \exp[-i(2\frac{2\pi}{\lambda}R_1) + \varphi_{s2}]$



Assuming $\varphi_{s1} = \varphi_{s2}$!!!

Interferogram:

$$i_1 i_2^* = |i_1 i_2^*| \exp[-i(2\frac{2\pi}{\lambda}\Delta R)]$$



Differential SAR Interferometry (D-InSAR)

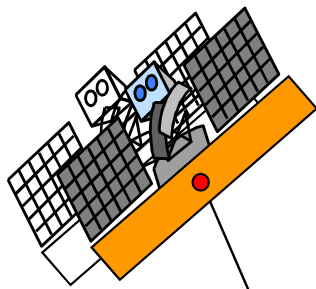
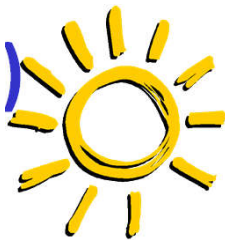


Image 1: $i_1 = |i_1| \exp[-i(2\frac{2\pi}{\lambda}R_1) + \varphi_{s1}]$

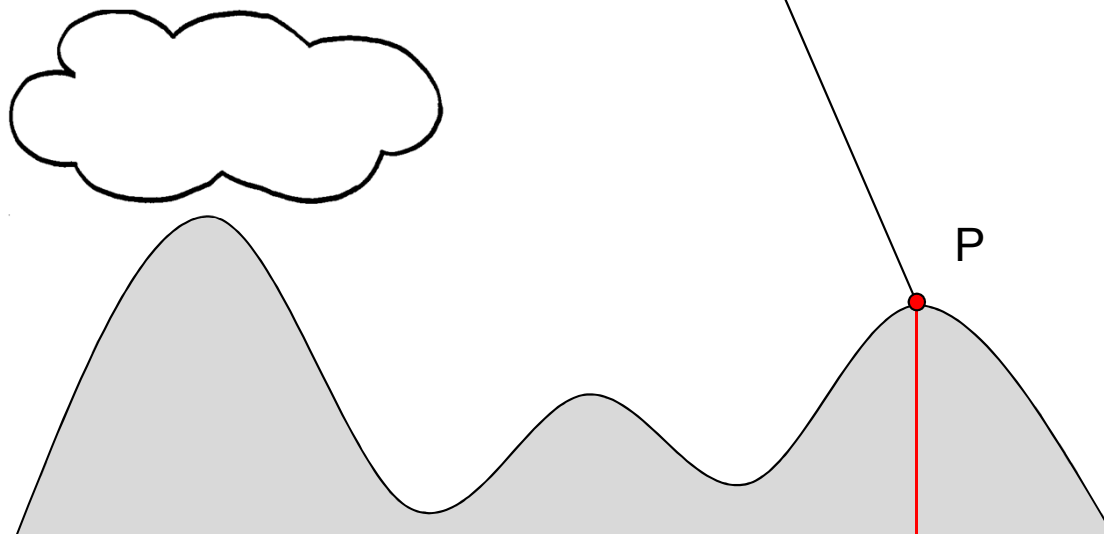
Image 2: $i_2 = |i_2| \exp[-i(2\frac{2\pi}{\lambda}R_1) + \varphi_{s2}]$

$R_2 = R_1$



Assuming $\varphi_{s1} = \varphi_{s2}$!!!

Interferogram: $i_1 i_2^* = |i_1 i_2^*| \exp[-i(2\frac{2\pi}{\lambda}\Delta R)] \xrightarrow{\Delta R=0} |i_1 i_2^*|$



When the images are acquired from the same location i.e. the spatial baseline becomes zero, $\Delta R = 0$, and the interferometric phase loses its sensitivity to terrain elevation.



Differential SAR Interferometry (D-InSAR)

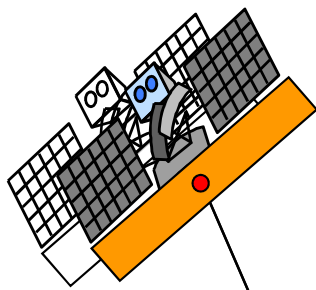
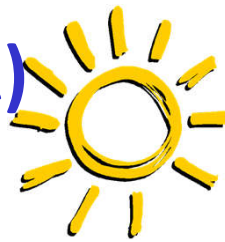


Image 1: $i_1 = |i_1| \exp[-i(2 \frac{2\pi}{\lambda} R_1) + \varphi_{s1}]$

Image 2: $i_2 = |i_2| \exp[-i 2 \frac{2\pi}{\lambda} (R_1 + \Delta R) + \varphi_{s2}]$

$R_2 = R_1$

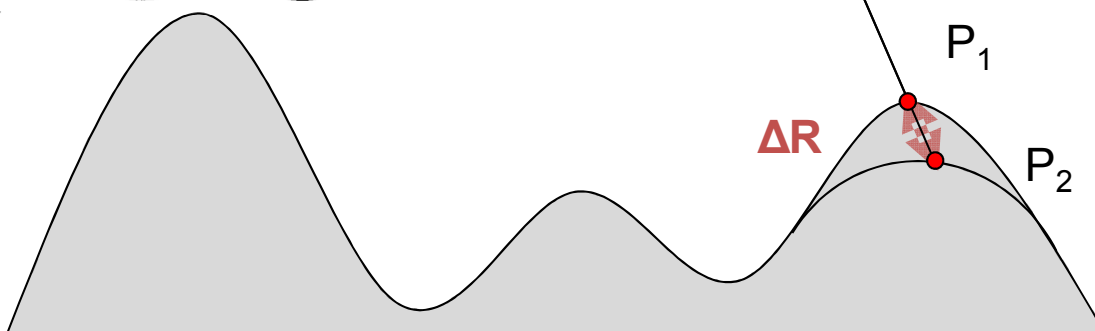
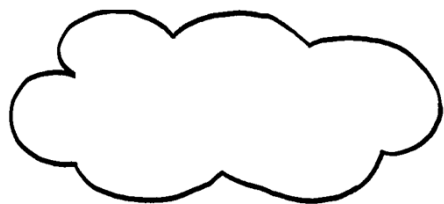


Assuming $\varphi_{s1} = \varphi_{s2}$!!!

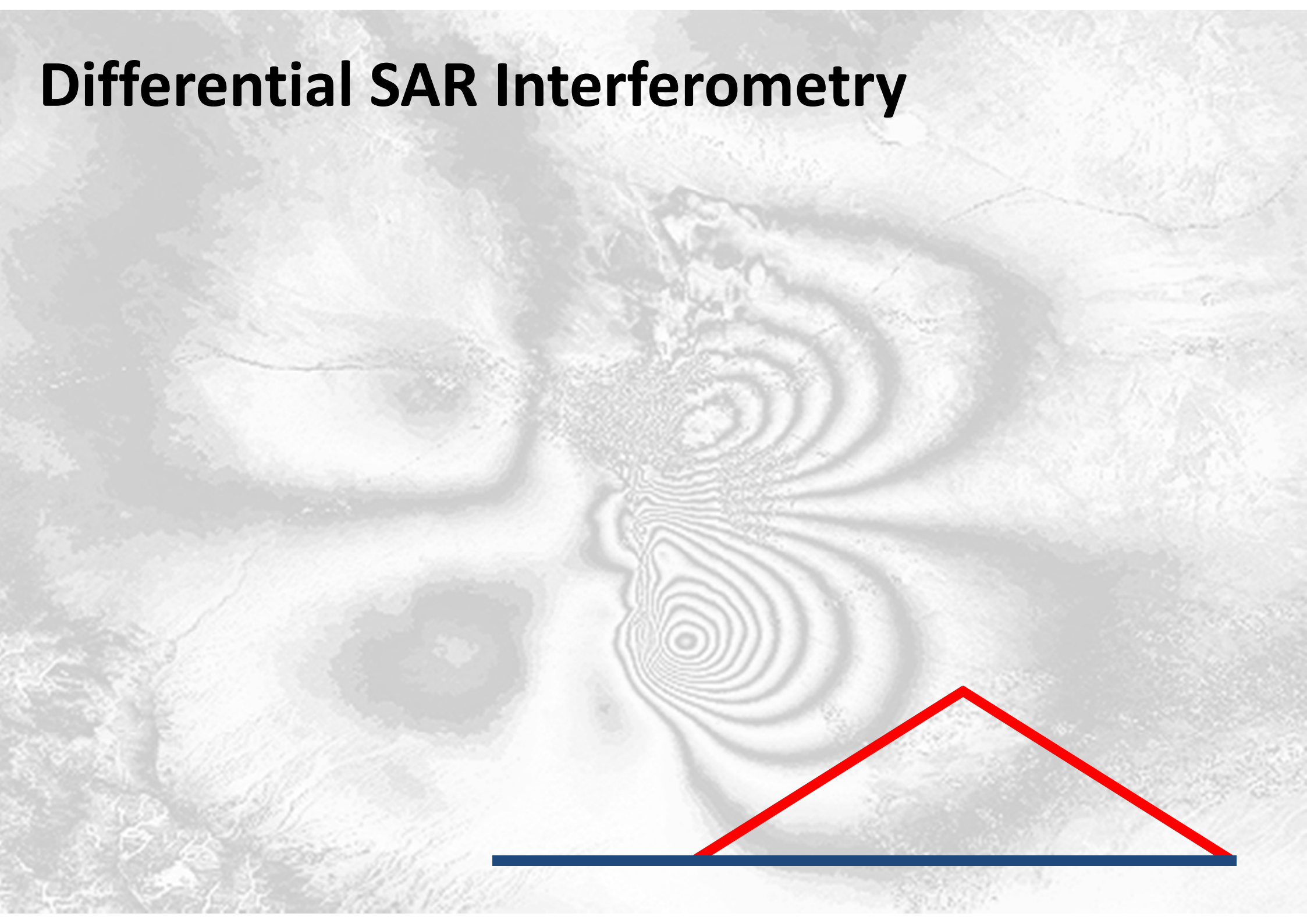
Interferogram: $i_1 i_2^* = |i_1 i_2^*| \exp[-i(2 \frac{2\pi}{\lambda} \Delta R)]$

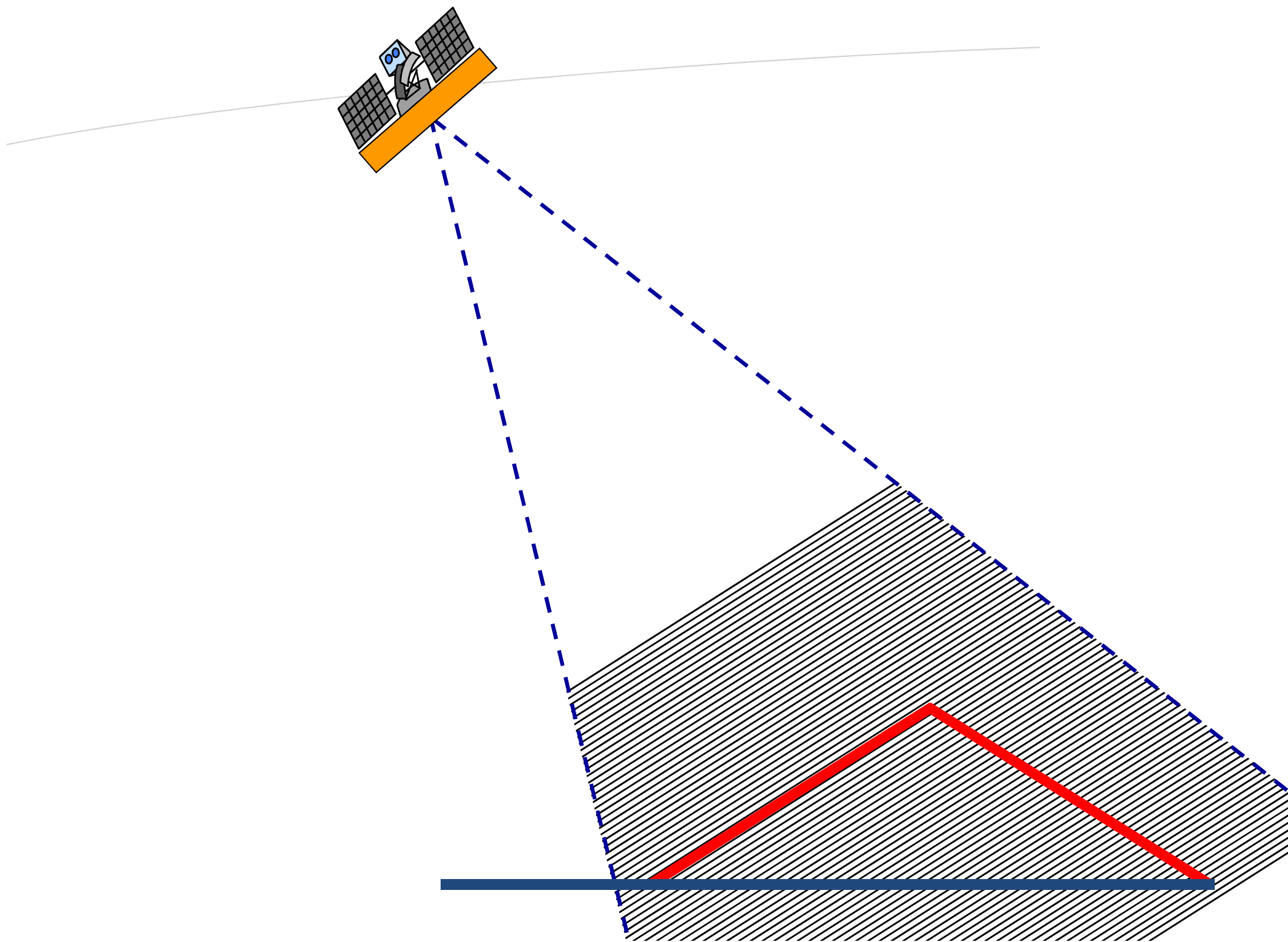
Phase: $\varphi = \arg(i_1 i_2^*) = 2 \frac{2\pi}{\lambda} \Delta R$

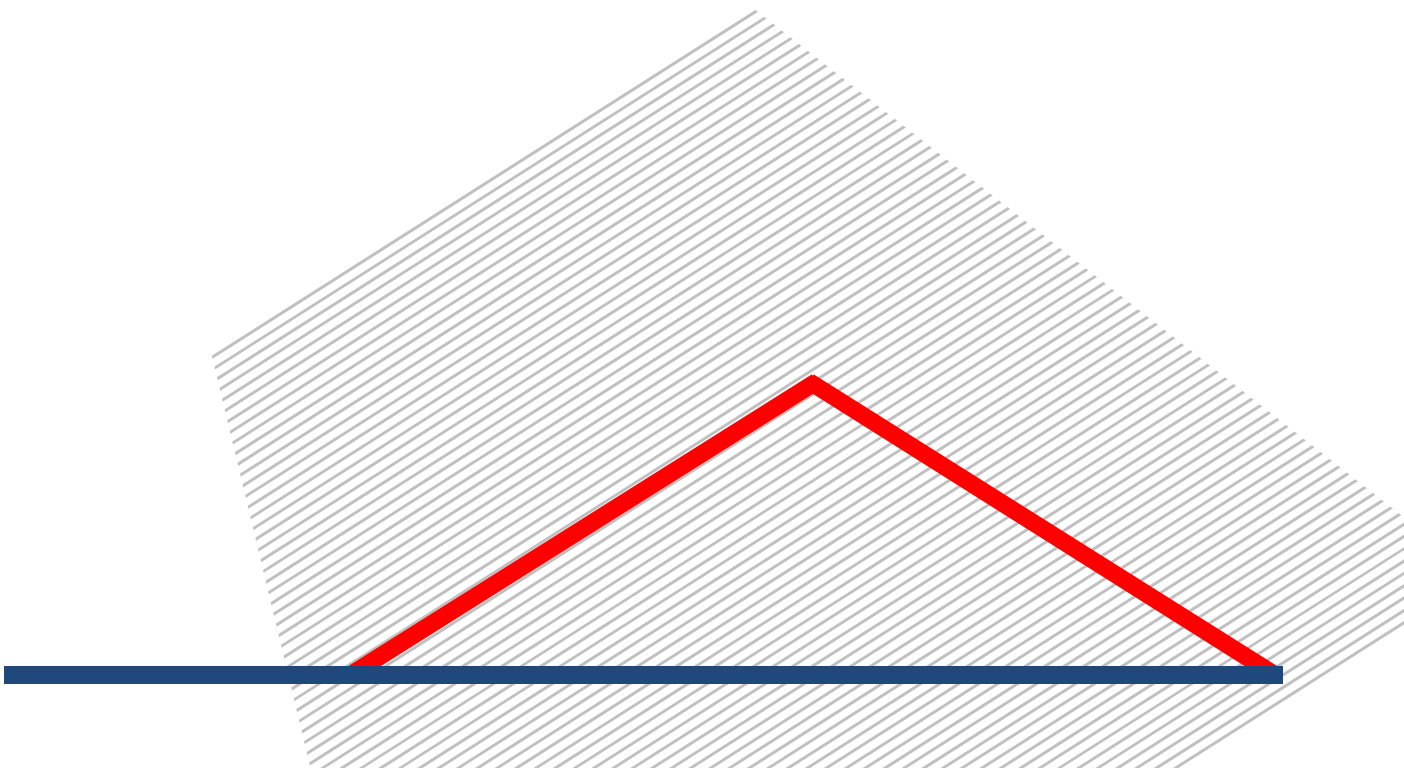
When the two images are acquired from the same location but at different times, i.e. with zero spatial & non-zero temporal baseline, the **interferometric phase is proportional to the change in the slant range distance** occurring in the time between the two acquisitions.

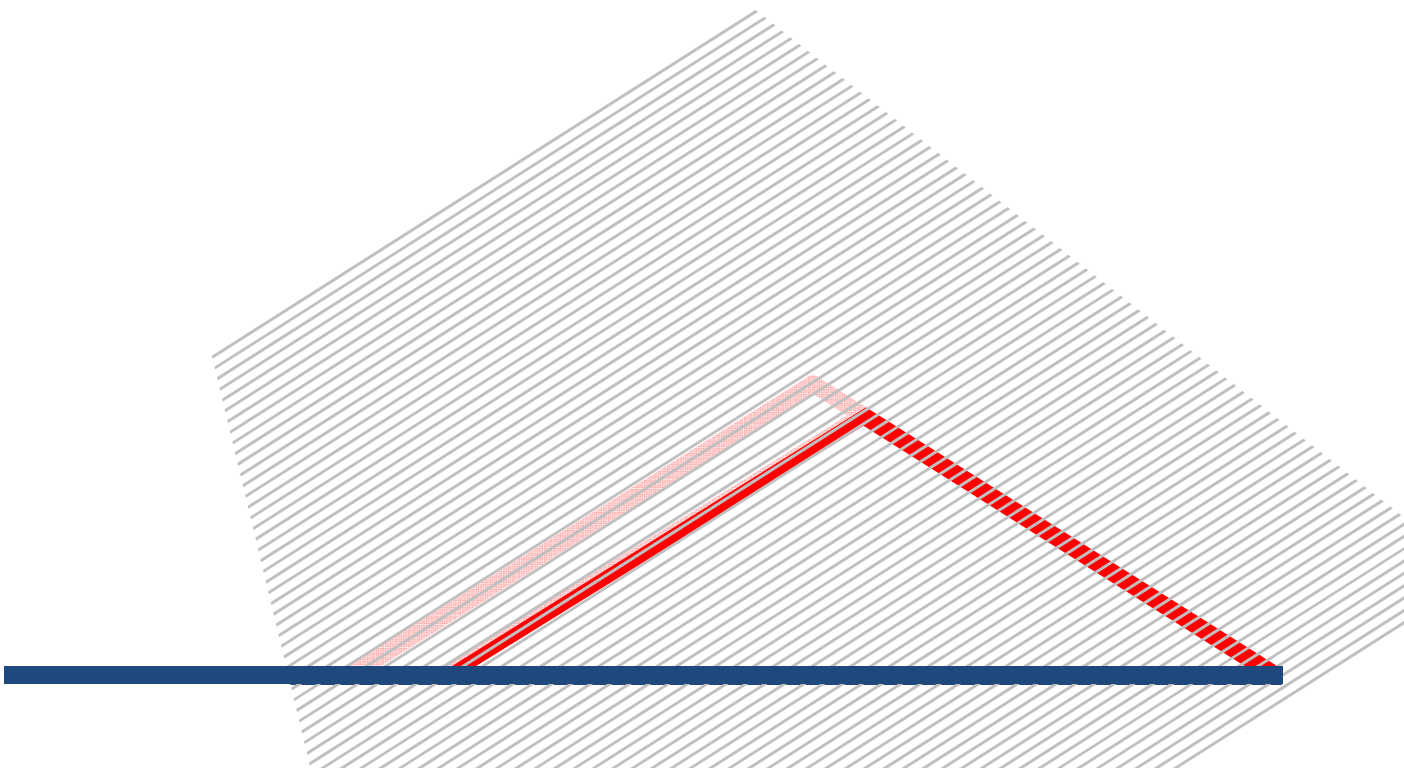


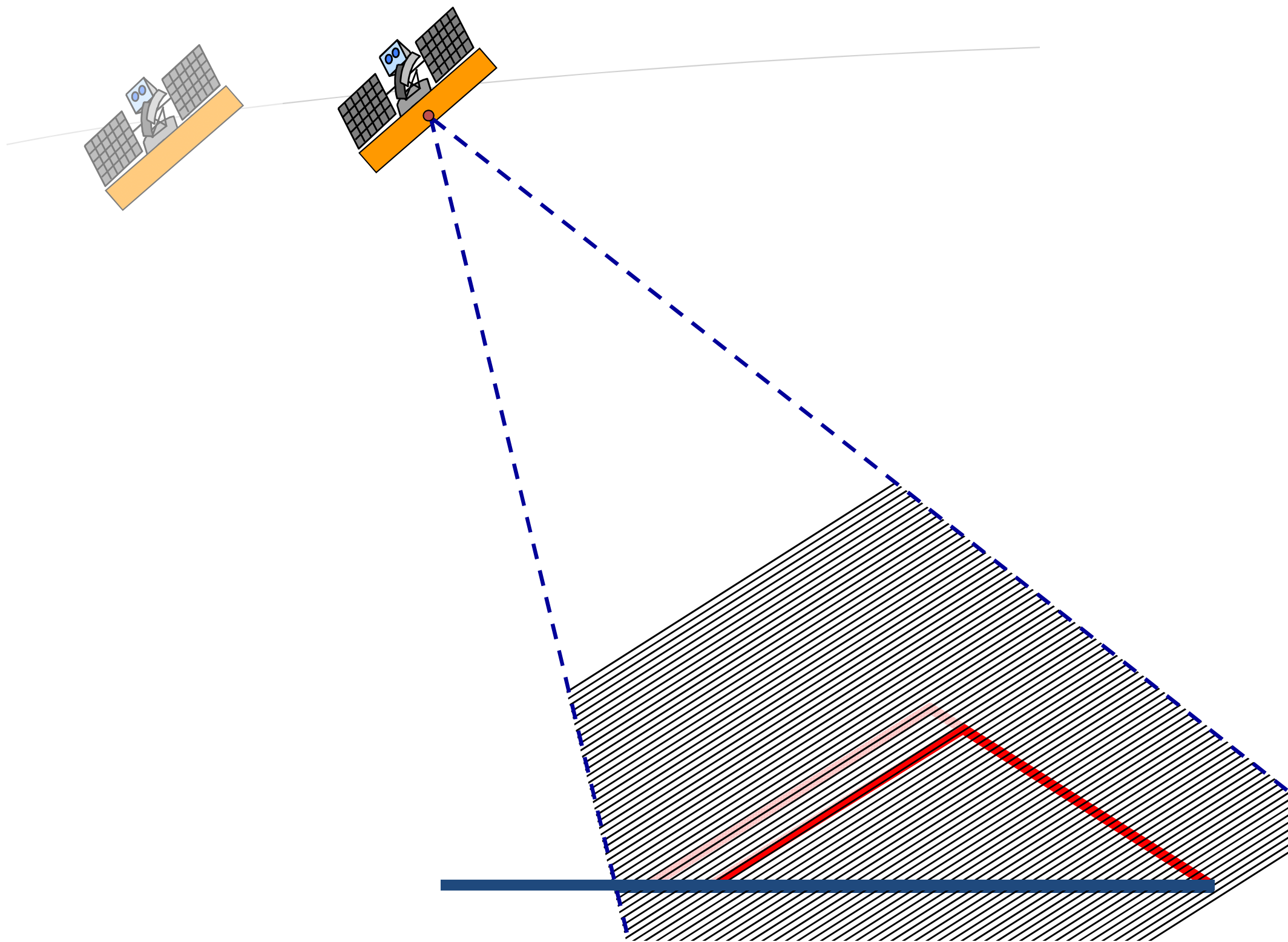
Differential SAR Interferometry

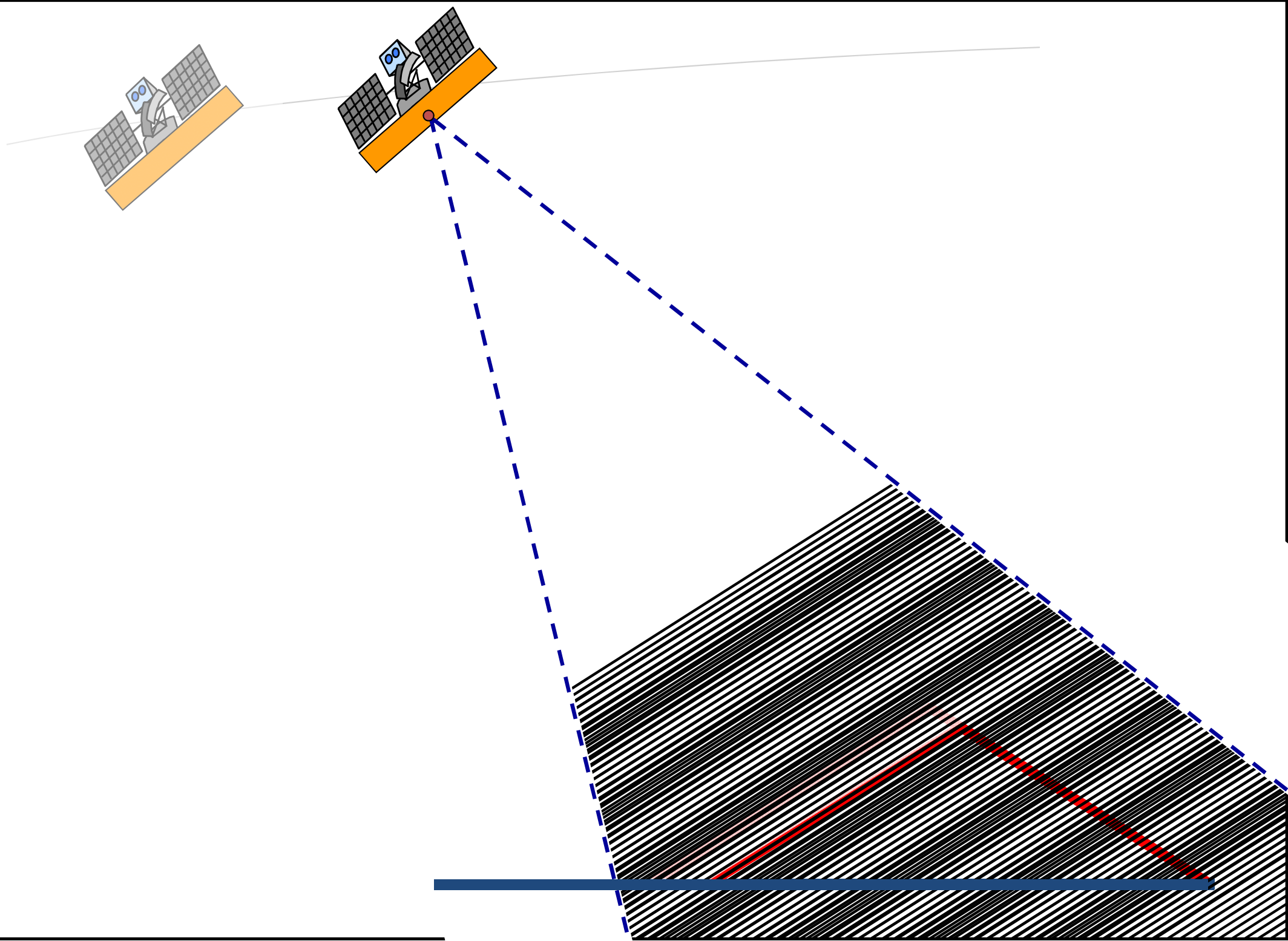




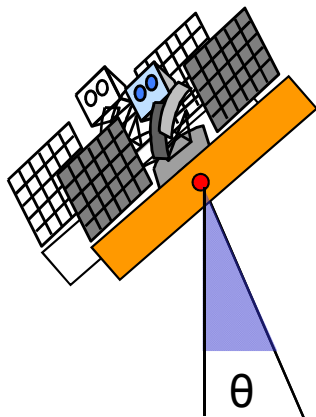








D-InSAR Phase: Height Sensitivity

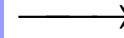


Interferometric Phase: $\varphi = 2\frac{2\pi}{\lambda}\Delta R + 2\pi N$ where $N = 0, \pm 1, \pm 2$

P_1 & P_2 : Two points at different slant range distance:

Phase-to-Slant-Range Distance Sensitivity:

$$\frac{\partial \varphi}{\partial R} := \frac{4\pi}{\lambda}$$

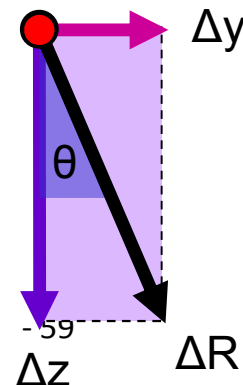


$$\sigma_R = \frac{\lambda}{4\pi} \sigma_\varphi$$

height error σ_R

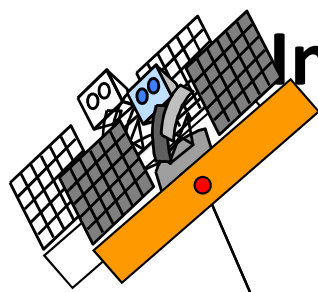
- ▶ independent on the acquisition geometry
- ▶ depends only on the system wavelength

Ground range (hor.-) & Height (ver.- displacement):

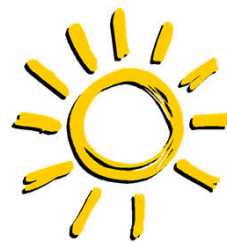
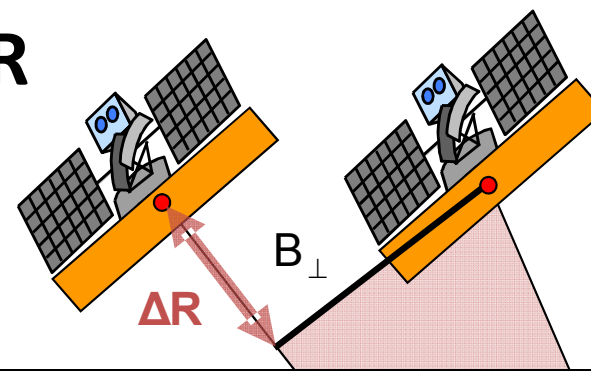


$$\Delta R = \Delta y \sin(\theta) + \Delta z \cos(\theta)$$





InSAR vs D-InSAR



Example ERS: Space-borne C-band ($\lambda=0.056\text{m}$) interferometer with incidence $\theta=23^\circ$ at range $R=870\text{km}$
 1 (2π) phase cycle (i.e. 1 fringe) corresponds to:

D-InSAR

$$\sigma_R = \frac{\lambda}{4\pi} \sigma_\phi = \frac{\lambda}{4\pi} 2\pi = 0.028 \text{ m} \quad (\text{in LOS})$$

$$\sigma_z = \frac{1}{\cos(\theta)} \sigma_R = 0.030 \text{ m} \quad (\text{vertical})$$

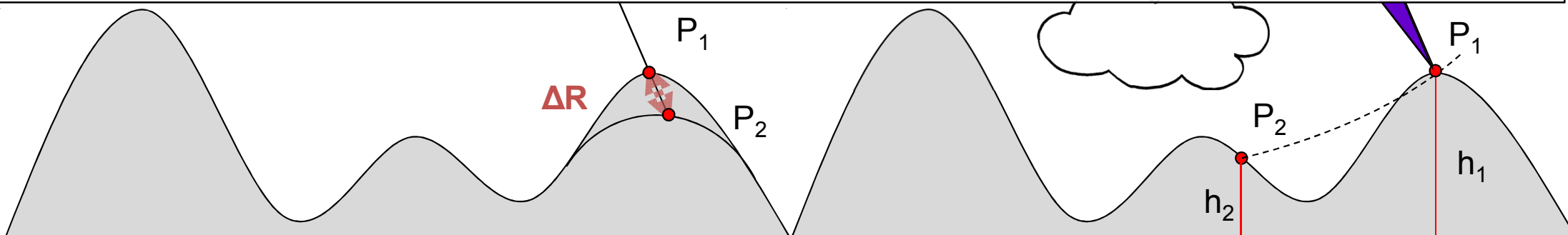
$$\sigma_y = \frac{1}{\sin(\theta)} \sigma_R = 0.072 \text{ m} \quad (\text{horizontal})$$

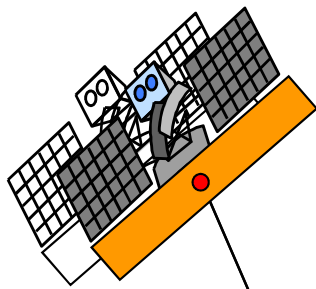
InSAR

$$\sigma_z = \frac{\lambda}{4\pi} \frac{R \sin(\theta)}{B_\perp} \sigma_\phi = \frac{\lambda}{4\pi} \frac{R \sin(\theta)}{B_\perp} \frac{10}{360} 2\pi$$

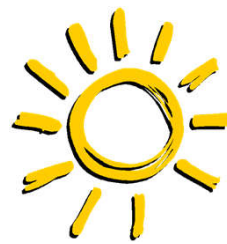
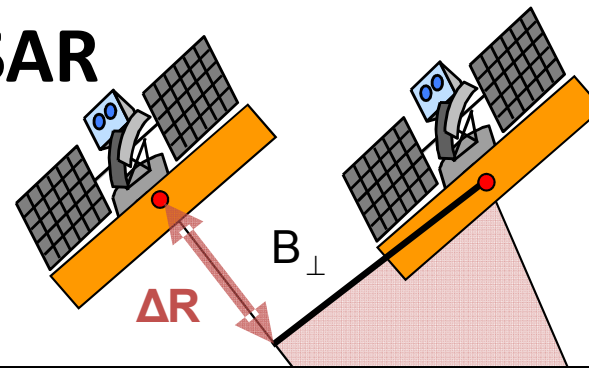
At perp. baseline $B_\perp=100\text{m}$: $\sigma_z=100\text{m}$ terrain elevation

At perp. baseline $B_\perp=200\text{m}$: $\sigma_z= 50\text{m}$ terrain elevation





InSAR vs D-InSAR



Example ERS: Space-borne C-band ($\lambda=0.056\text{m}$) interferometer with incidence $\theta=23^\circ$ at range $R=870\text{Km}$

Assuming the ability to measure the interferometric phase with an accuracy of 20° :

D-InSAR

$$\sigma_R = \frac{\lambda}{4\pi} \sigma_\phi = \frac{\lambda}{4\pi} \frac{20}{360} 2\pi \approx 1.5 \text{ mm} \quad (\text{in LOS})$$

$$\sigma_z = \frac{1}{\cos(\theta)} \sigma_R = 1.6 \text{ mm} \quad (\text{vertical})$$

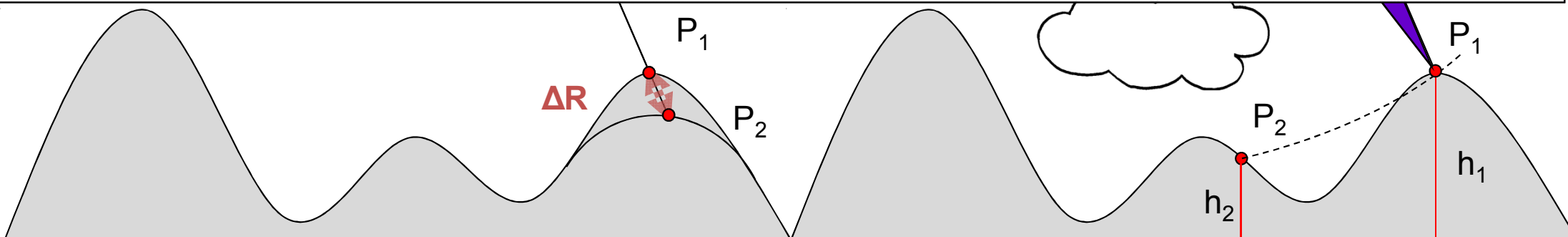
$$\sigma_y = \frac{1}{\sin(\theta)} \sigma_R = 4.0 \text{ mm} \quad (\text{horizontal})$$

InSAR

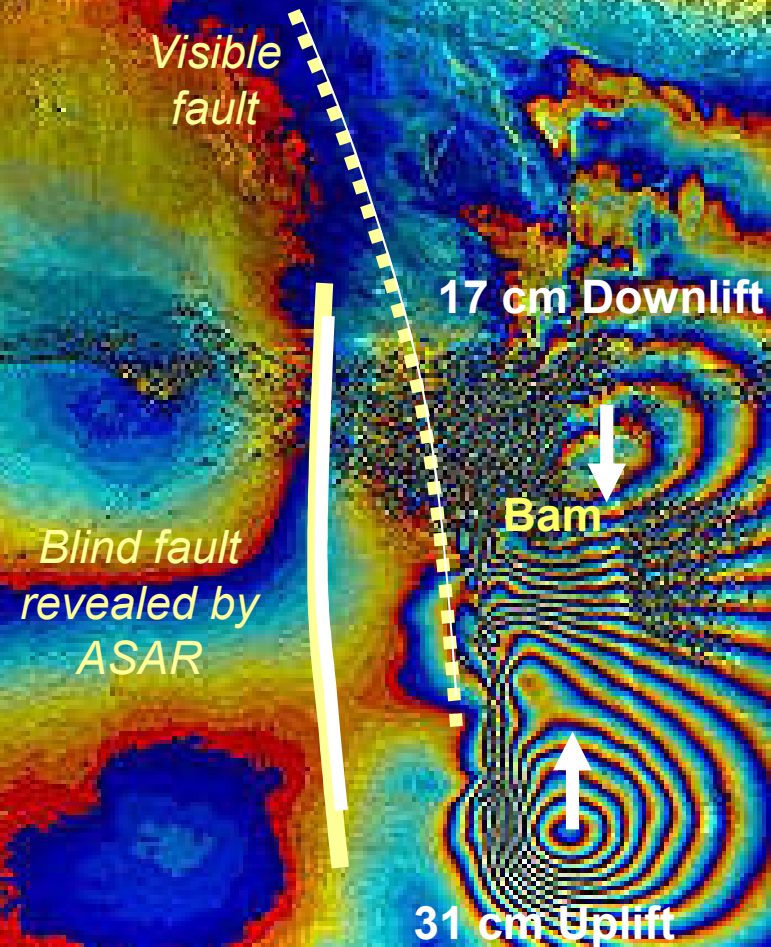
$$\sigma_z = \frac{\lambda}{4\pi} \frac{R \sin(\theta)}{B_\perp} \sigma_\phi = \frac{\lambda}{4\pi} \frac{R \sin(\theta)}{B_\perp} \frac{20}{360} 2\pi$$

At perp. baseline $B_\perp=100\text{m}$: $\sigma_z = 5.50\text{m}$ terrain error

At perp. baseline $B_\perp=200\text{m}$: $\sigma_z = 2.75\text{m}$ terrain error



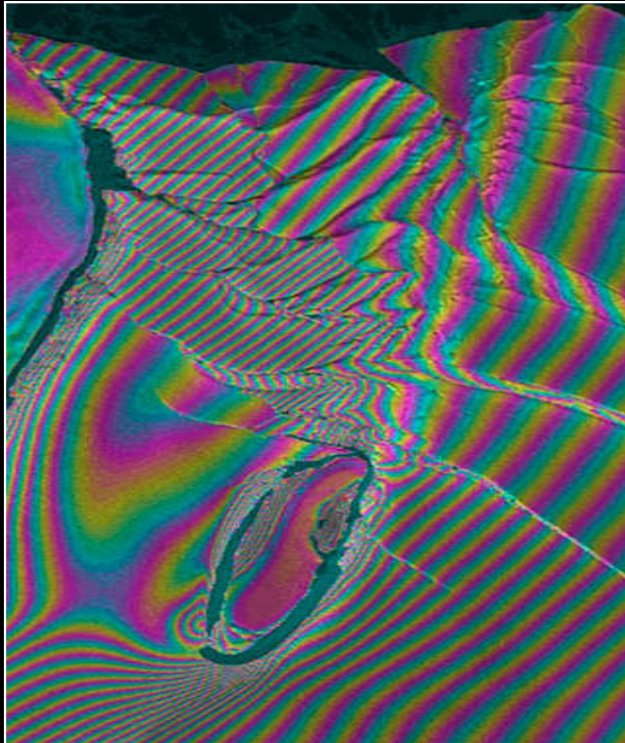
Seismic Faults: The Bam Earthquake by Envisat ASAR



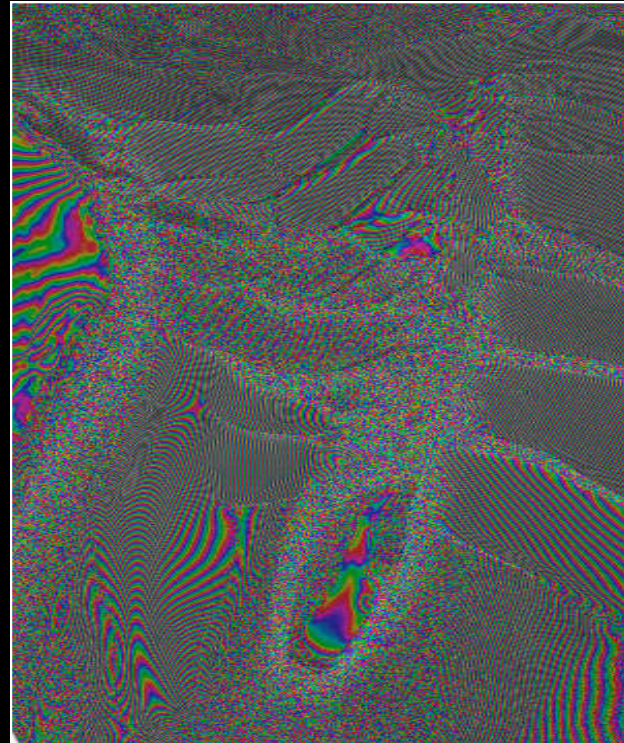
Ground motion associated with the 26 December 2003 earthquake in Bam, Iran. The "fringes" show contours of the ground deformation caused by the quake. Each contour represents 28 millimeters of motion in LOS. Image credit: ESA

Ice motion of fast moving glaciers

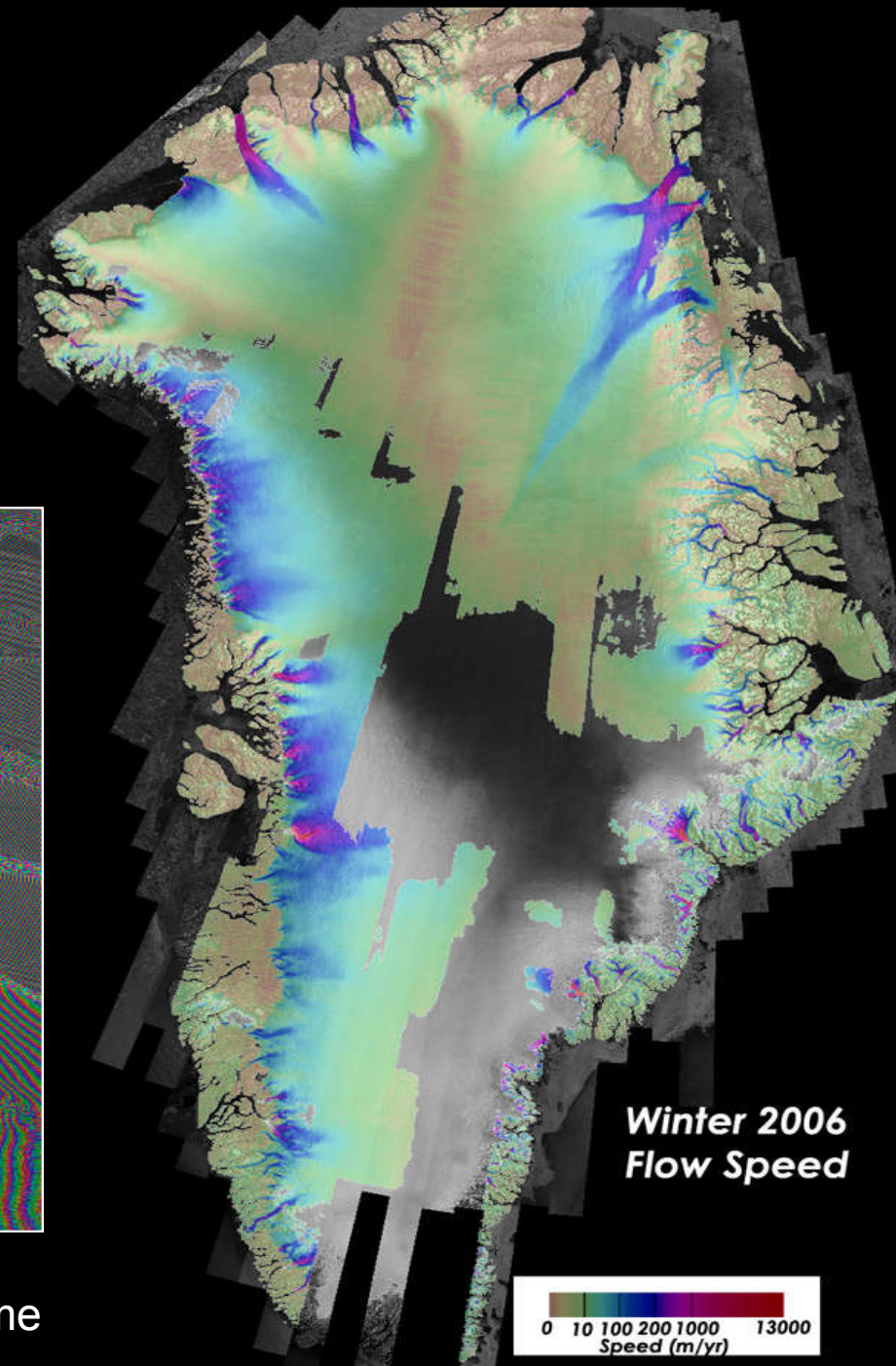
The combination of **short repeat pass times** and a **systematic acquisition scenario** and a low SAR frequency (**L-band**) is optimum for fast ice motion.



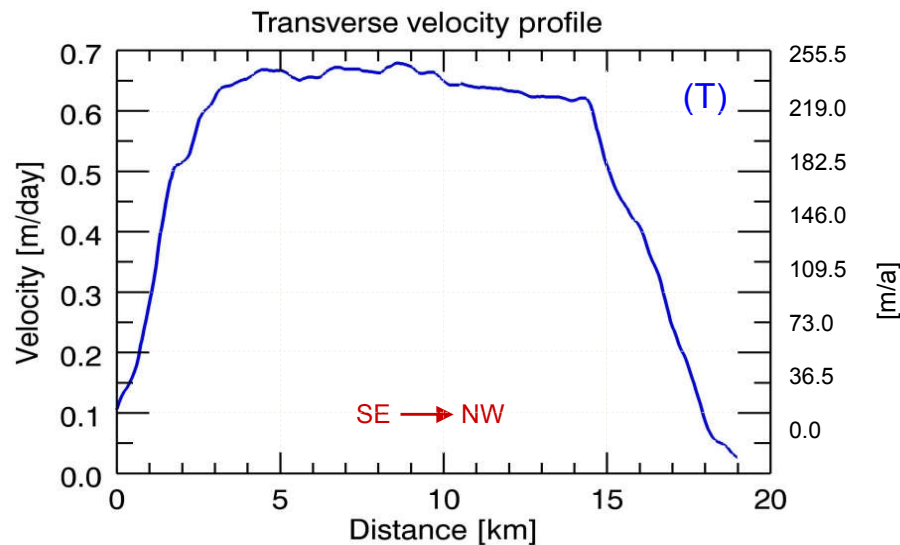
ERS Tandem 1-Day RP Time



RADARSAT 24-Days RP Time



Ice Surface Velocity from TerraSAR-X: Nimrod Glacier



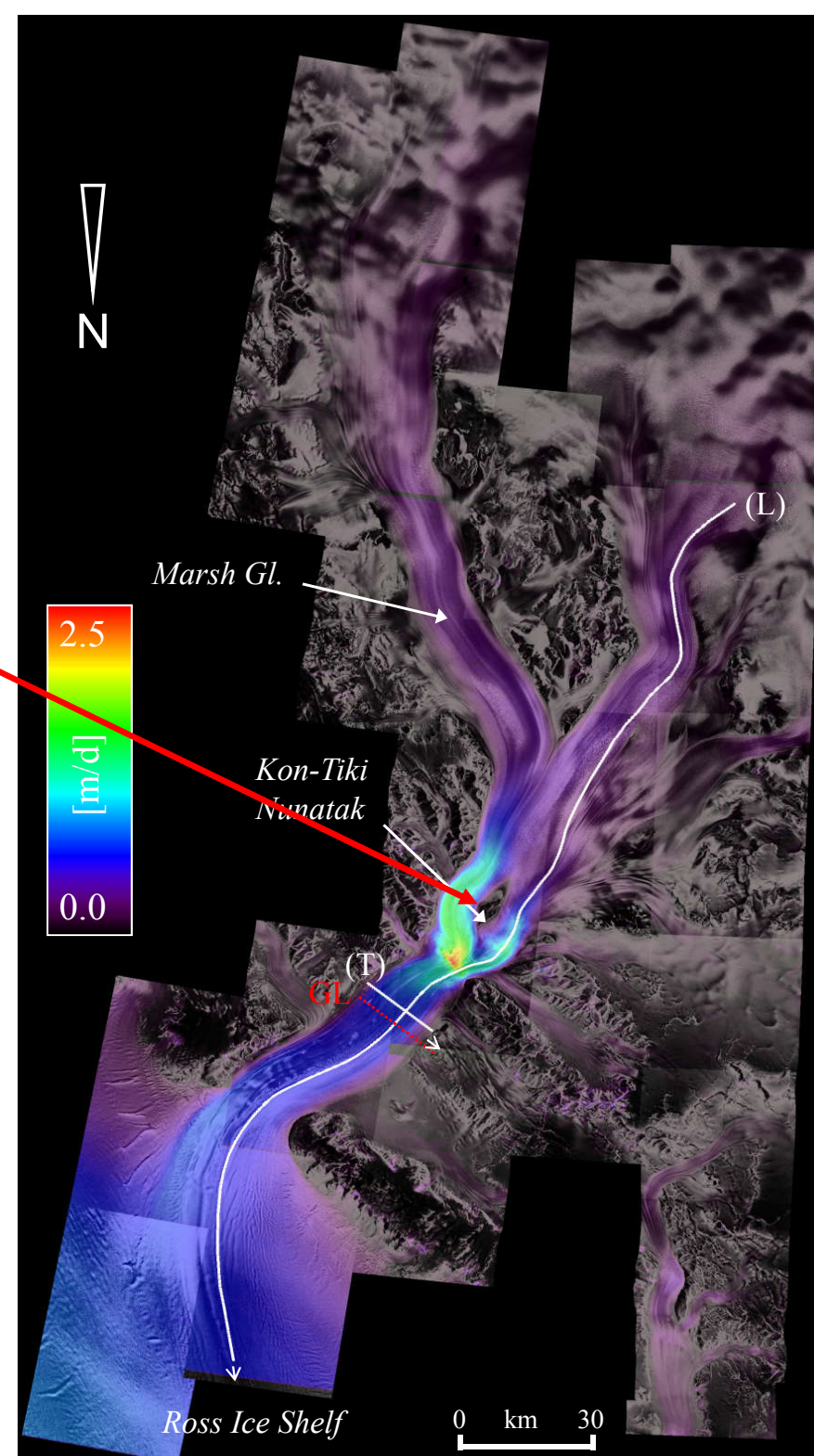
→
Plug-like
shape:
strong side
drag



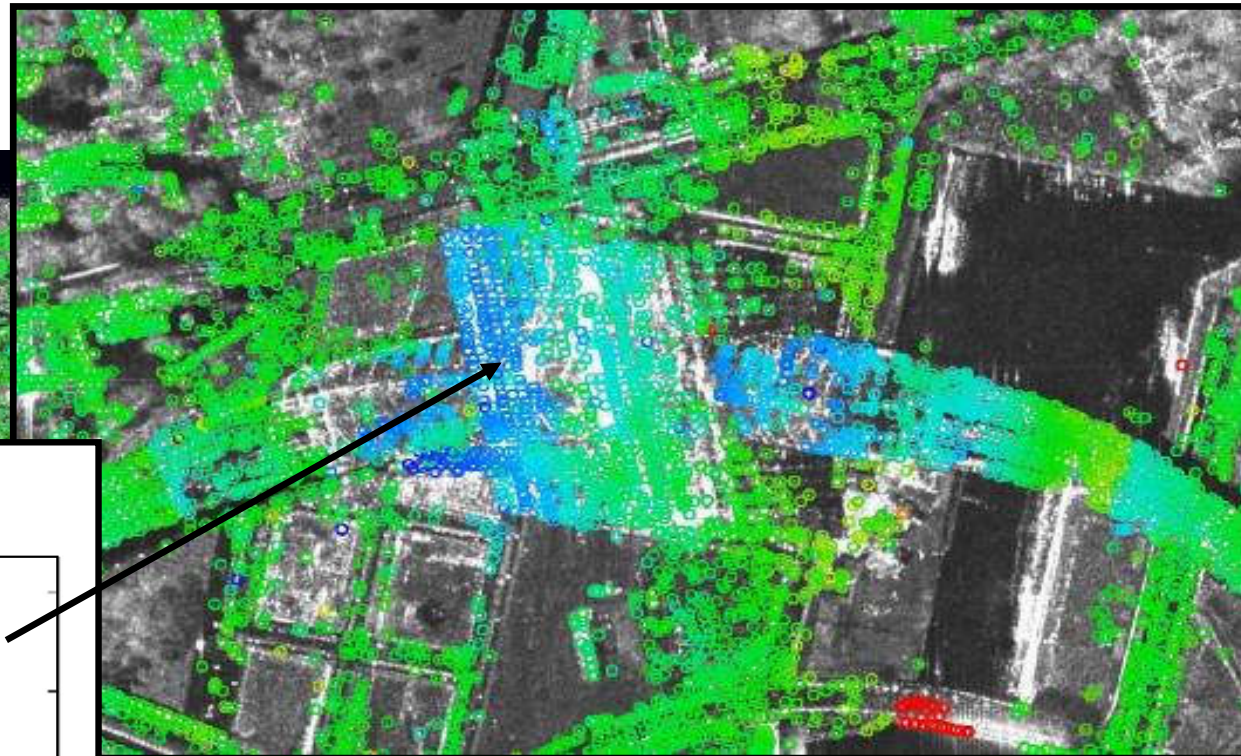
Earth Observation and
Remote Sensing

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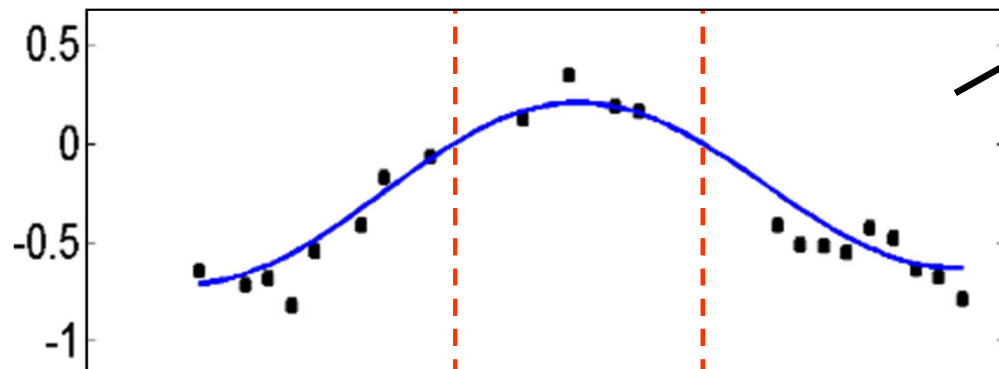
- 64



Thermal Dilation: Berlin Main Train Station

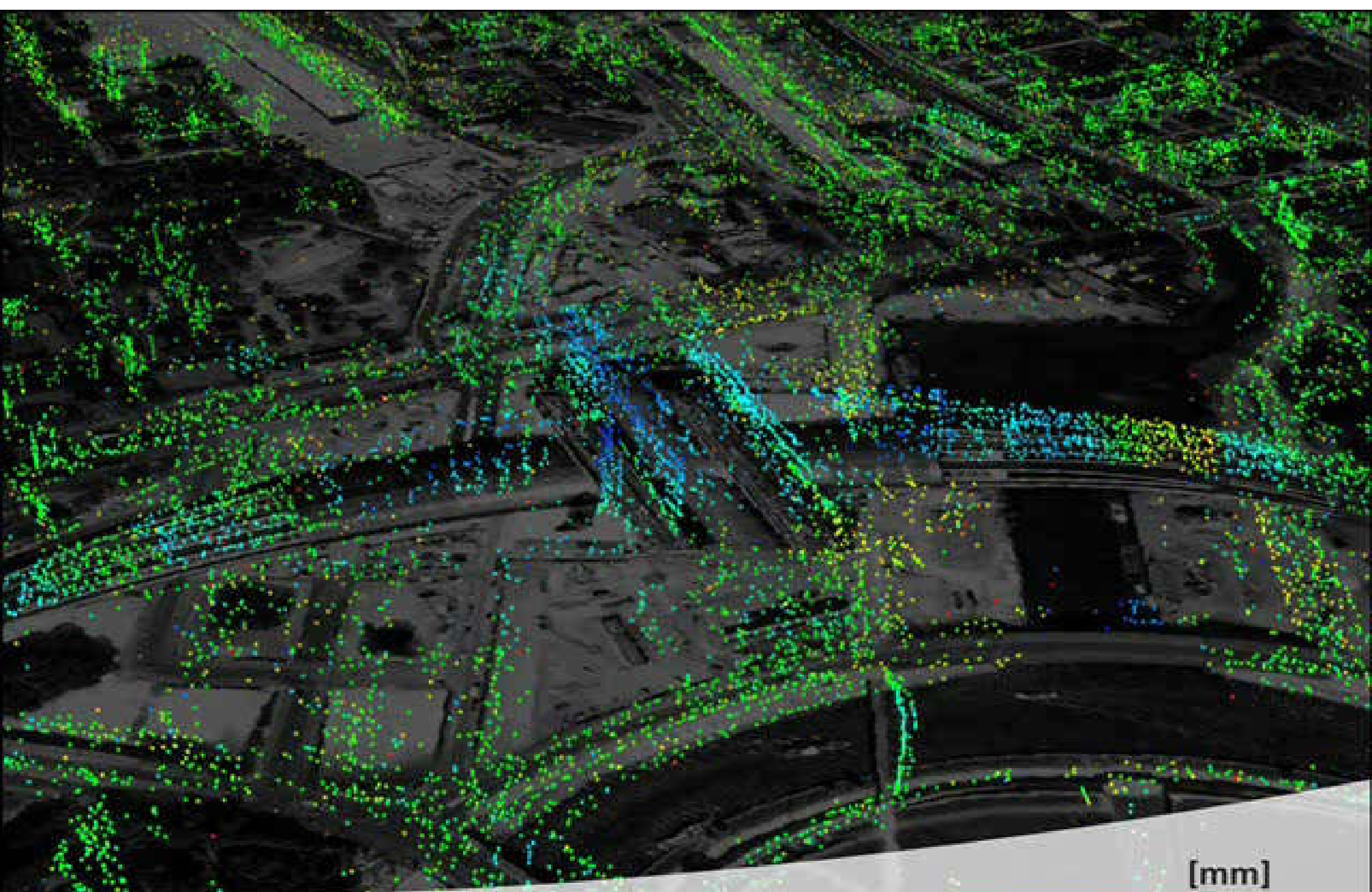


deformation [cm]



June - Sept.





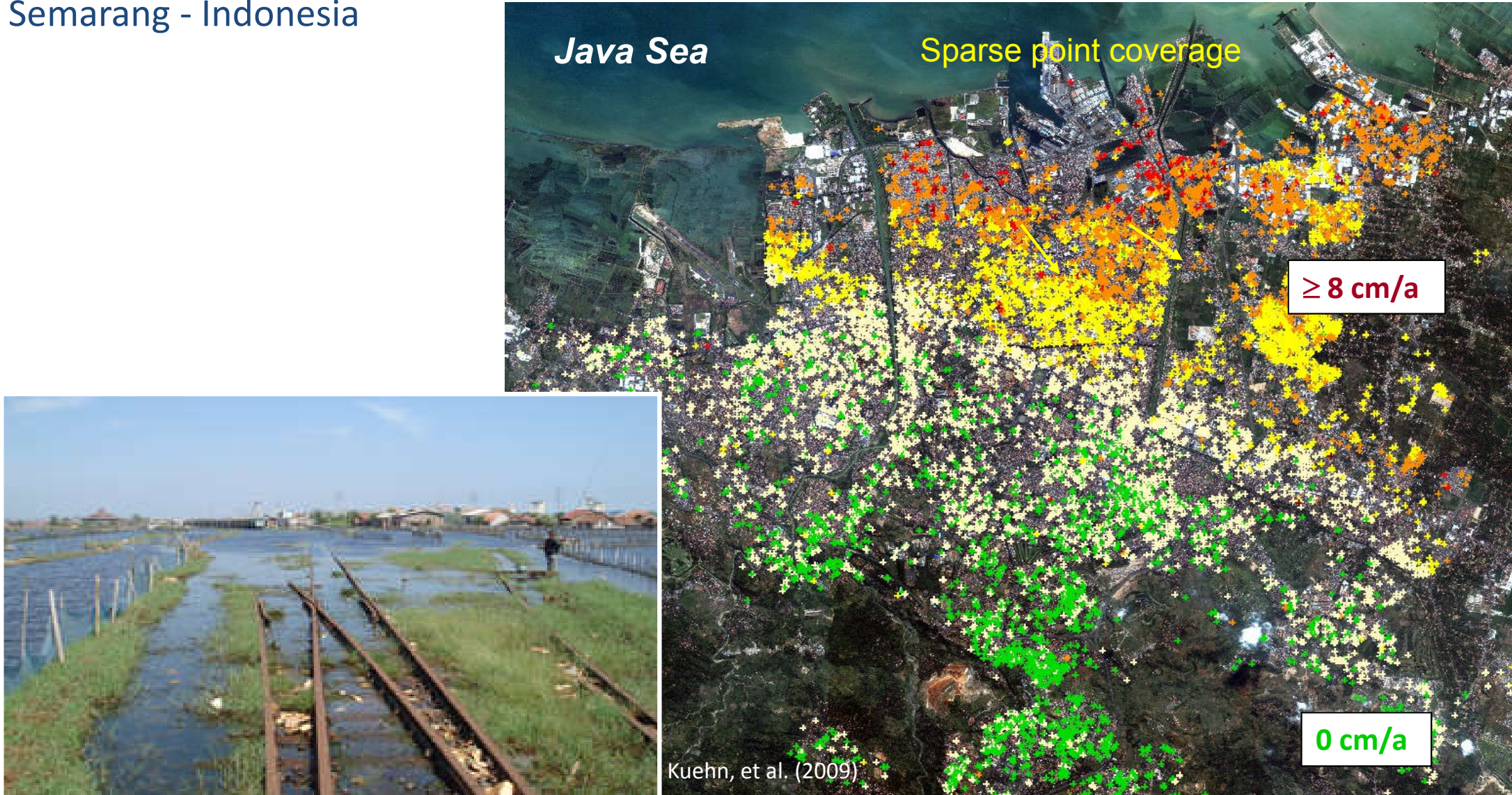
Seasonal Thermal Dilation

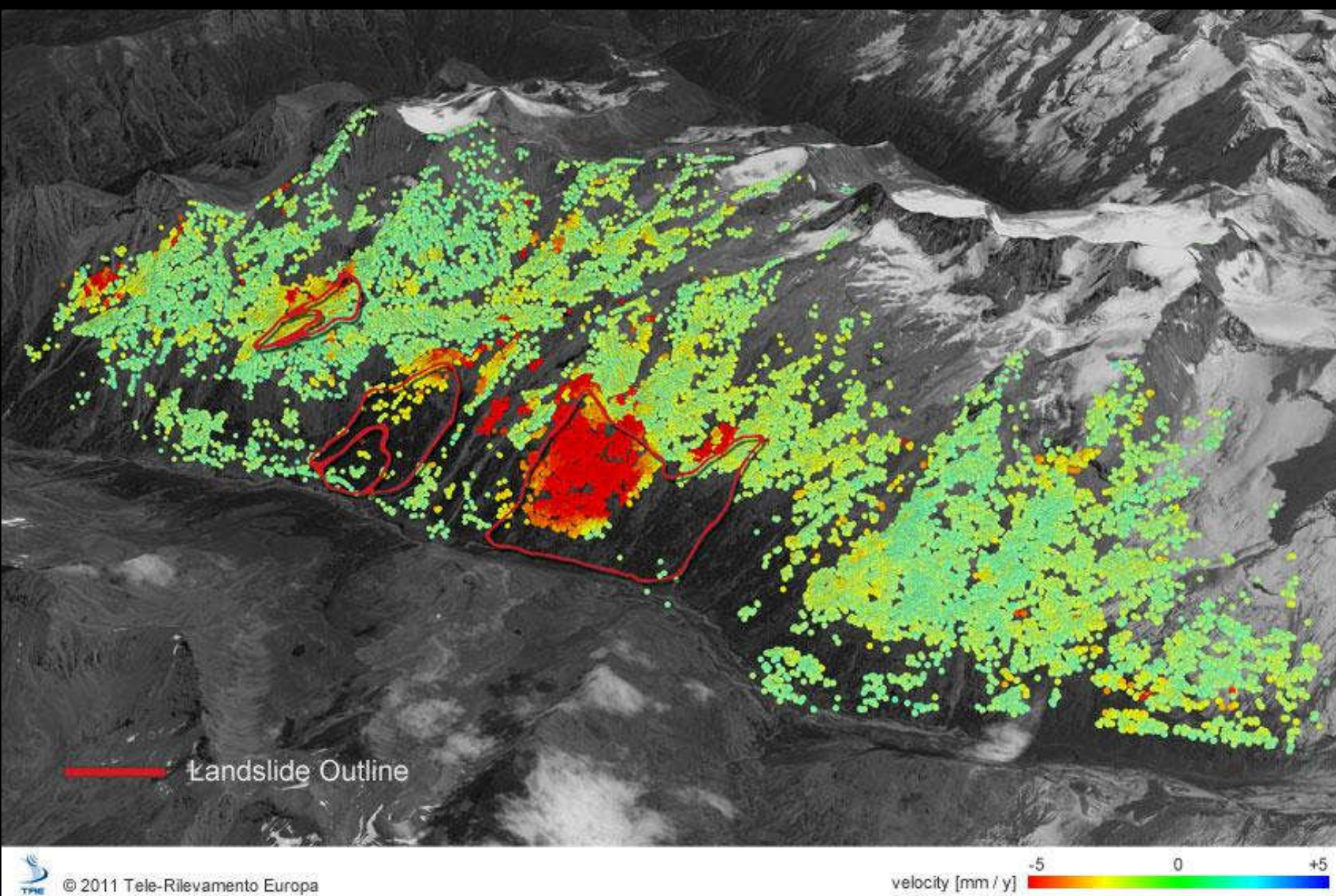


PSI Land Subsidence Monitoring

Semarang - Indonesia

27/12/02 to 23/08/06





Active landslide in Valsavarenche, Italy. For each ground point identified a time-series of its deformation can be reconstructed to show its movement over the time period analyzed. Image credit: Treuropa / Sensor: Radarsat