

# WOC 3D Ocean currents retrieval

Bruno Buongiorno Nardelli, Daniele Ciani



WorldOceanCirculation



**Improve our knowledge of the 3D transport and environmental conditions and that are known to potentially affect key biological and ecological processes in the upper ocean**

**Develop new products** to explore of the potential impact of long term oceanic variability on the population dynamics of different fish species.

The main interest is to:

- investigate the role of frontal meanders and eddies in the and dispersal of larvae of selected species (keeping in mind the possibility of diel vertical migrations from the surface down to few hundreds meters)
- assess the vertical exchanges at the base of the euphotic layer and their potential impact on primary productivity



**Improve our knowledge of the 3D transport and environmental conditions and that are known to potentially affect key biological and ecological processes in the upper ocean**

**Develop new products** to explore of the potential impact of long term oceanic variability on the population dynamics of different fish species.

The main interest is to:

- investigate the role of frontal meanders and eddies in the and dispersal of larvae of selected species (keeping in mind the possibility of diel vertical migrations from the surface down to few hundreds meters)
- assess the vertical exchanges at the base of the euphotic layer and their potential impact on primary productivity

→ New product to be tested by intermediate users active in fishery advisory bodies (e.g. ICCAT, ICES) working groups and projects to achieve maximum impact in support of sustainable fishery.

SOCIB	Diego Alvarez	Spain	<a href="http://www.socib.eu/">http://www.socib.eu/</a>
DTU Aqua	Patrizio Mariani	Denmark	<a href="https://www.aqua.dtu.dk/english">https://www.aqua.dtu.dk/english</a>

Technical  
University of  
Denmark



**Theme 2 session tomorrow**



**Improve our knowledge of the 3D transport and environmental conditions and that are known to potentially affect key biological and ecological processes in the upper ocean**

**Develop new products** to explore of the potential impact of long term oceanic variability on the population dynamics of different fish species.

**WOC-NATL3D: 3D quasi-geostrophic ocean currents (u,v,w) reconstruction covering the upper layer (0-1500 m)**



**Improve our knowledge of the 3D transport and environmental conditions and that are known to potentially affect key biological and ecological processes in the upper ocean**

**Develop new products** to explore of the potential impact of long term oceanic variability on the population dynamics of different fish species.

**WOC-NATL3D: 3D quasi-geostrophic ocean currents (u,v,w) reconstruction covering the upper layer (0-1500 m)**

**Copernicus-OMEGA3D:**

- mesoscale "permitting" resolution
- reduced accuracy at the surface

Weekly 1/4°x1/4° (global)

3D multilinear regression (CMEMS-ARMOR3D)

surface geostrophic currents (AVISO)

Atmospheric fluxes (ERA-interim)



**WOC-NATL3D:**

- mesoscale "resolving" resolution
- more accurate surface Ekman currents

Daily, 1/10°x1/10° (regional)

3D neural network model (WOC-LSTM3D)

improved surface geostrophic currents (WOC-NATL2D)

Atmospheric fluxes (ERA5)

Empirical Ekman current shear (Copernicus)



**Improve our knowledge of the 3D transport and environmental conditions and that are known to potentially affect key biological and ecological processes in the upper ocean**

**Develop new products** to explore of the potential impact of long term oceanic variability on the population dynamics of different fish species.

**WOC-NATL3D: 3D quasi-geostrophic ocean currents (u,v,w) reconstruction covering the upper layer (0-1500 m)**

#### Copernicus-OMEGA3D:

- mesoscale "permitting" resolution
- reduced accuracy at the surface

Weekly  $1/4^{\circ} \times 1/4^{\circ}$  (global)

3D multilinear regression (CMEMS-ARMOR3D)

surface geostrophic currents (AVISO)

Atmospheric fluxes (ERA-interim)



#### WOC-NATL3D:

- mesoscale "resolving" resolution
- more accurate surface Ekman currents

Daily,  $1/10^{\circ} \times 1/10^{\circ}$  (regional)

3D neural network model (WOC-LSTM3D)

improved surface geostrophic currents (WOC-NATL2D)

Atmospheric fluxes (ERA5)

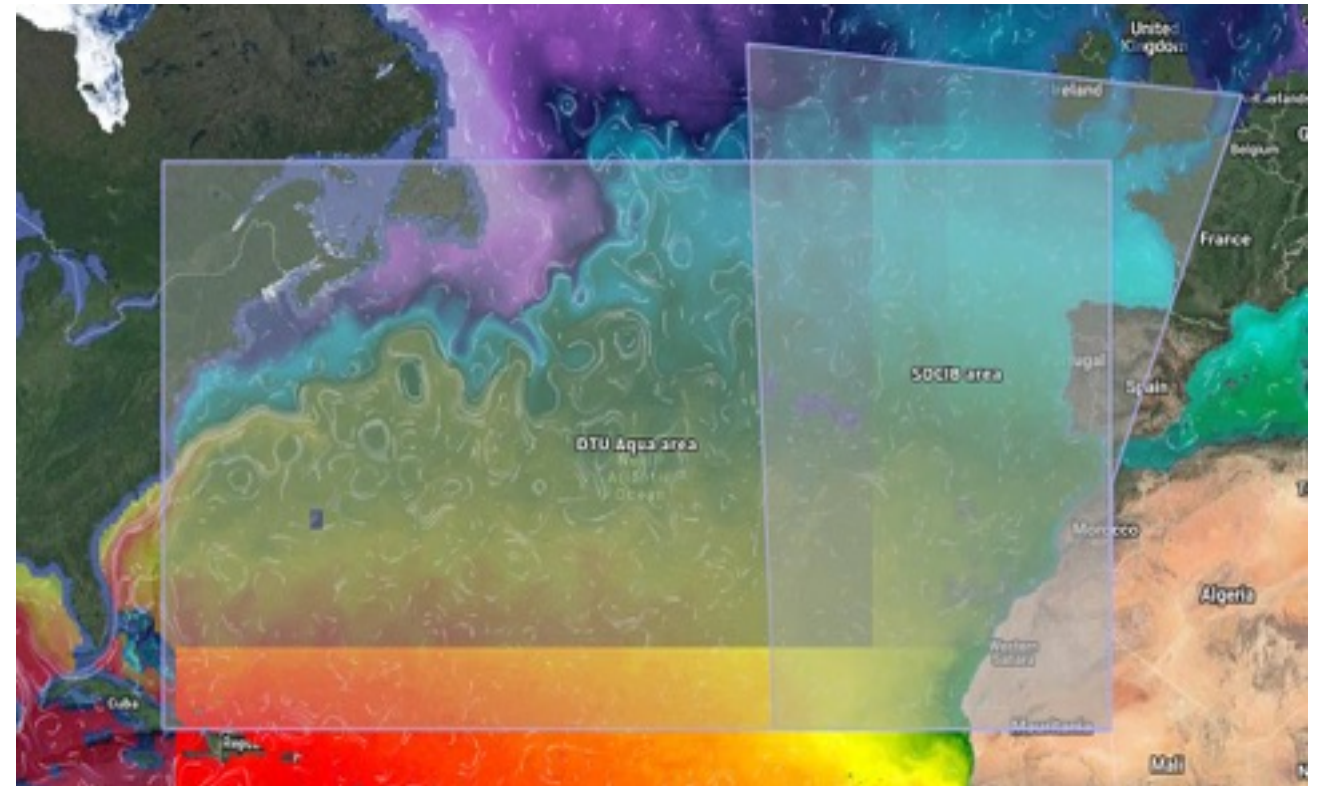
Empirical Ekman current shear (Copernicus)



## Study area

- **Sargasso Sea and Gulf Stream area** (Sargasso is the only location where the threatened European and American eels reproduce, Dekker, 2019).
- **Eastern Boundary Upwelling Systems** along the African and Iberian coasts → several species relevant for both local communities and commercial exploitation (Kämpf and Chapman, 2016)

The entire domain is ground for extremely relevant fishery activities, and identified as a key area within international conventions for the conservation of fishing resources (e.g. for tuna and tuna-like fishes, within ICCAT - International Commission for the Conservation of Atlantic Tunas)



## WOC-NATL3D product development and processing steps

daily 3D (0-1500 m) quasi-geostrophic ocean currents ( $u,v,w$ ), at mesoscale-resolving spatial resolution ( $1/10^\circ \times 1/10^\circ$ ), over a wide section of the central/North Atlantic Ocean ( $20^\circ\text{N}$ - $50^\circ\text{N}$ ,  $76^\circ\text{W}$ - $6^\circ\text{W}$ ). It covers ten years (2010-2019)

### Three steps:

#### 1. Collect/develop high resolution surface data

- Sea Surface Temperature (SST)
- Sea Surface Salinity (SSS)
- Absolute Dynamic Topography (ADT)

#### 2. Retrieve ocean 3D hydrographic structure from combined surface data and in situ vertical profiles

- multivariate Empirical Orthogonal Function reconstruction
- Long-Short Term Memory Network

#### 3. Solve diabatic Quasi-Geostrophic Omega equation including surface forcings

- adapt Copernicus Marine Service OMEGA3D processing chain to NATL3D domain/resolution
- improve forcings





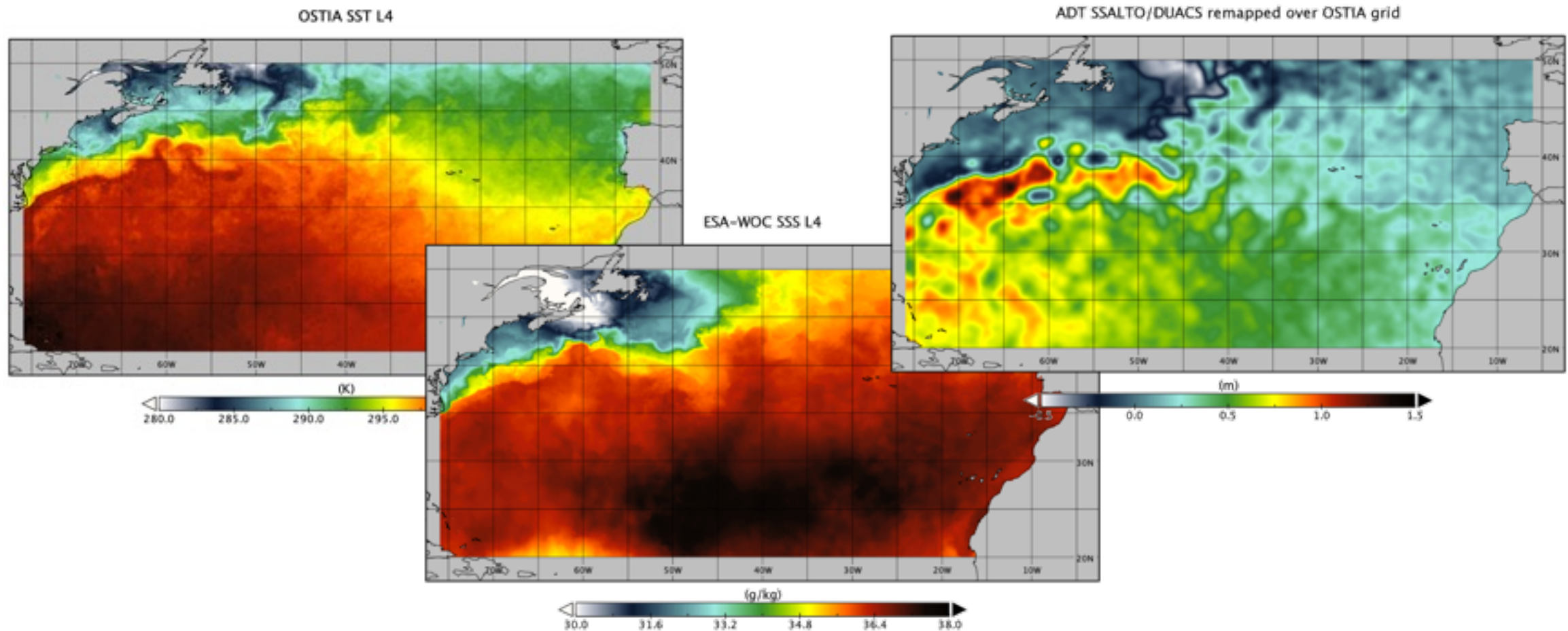
All reconstruction techniques tested here project the anomalies of **sea surface temperature (SST)**, **sea surface salinity (SSS)** and **adjusted absolute dynamic topography (ADT)** at depth based on information extracted from T, S, and steric height anomaly profiles (all anomalies are computed vs climatologies)

### High resolution surface data:

Sea Surface Temperature (SST) → OSTIA (UK Metoffice)

ESA-WOC Sea Surface Salinity (SSS) → *new ESA-WOC daily product at 1/10°*

Absolute Dynamic Topography (ADT) → *new ESA-WOC product: NATL2D*

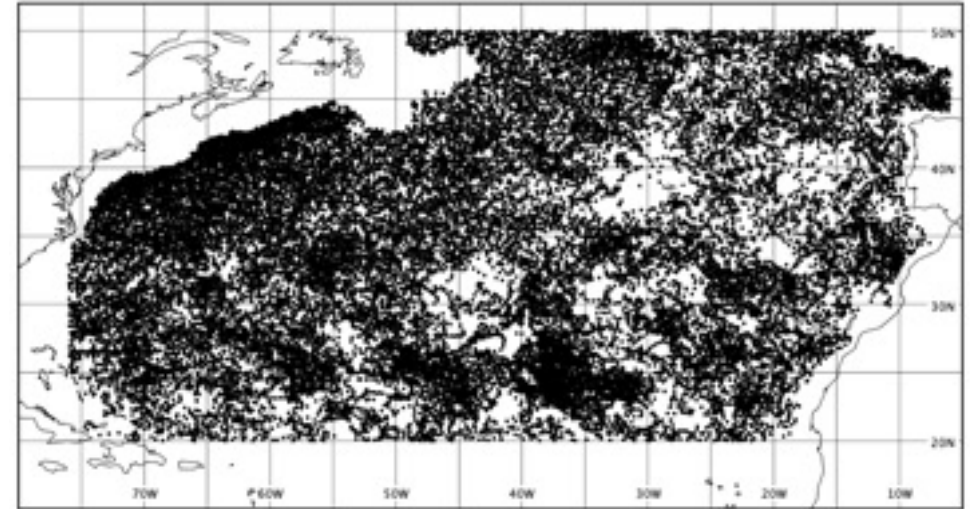


All reconstruction techniques tested here project the anomalies of sea surface temperature (SST), sea surface salinity (SSS) and adjusted absolute dynamic topography (ADT) at depth based on information extracted from **T, S, and steric height anomaly profiles** (all anomalies are computed vs climatologies)

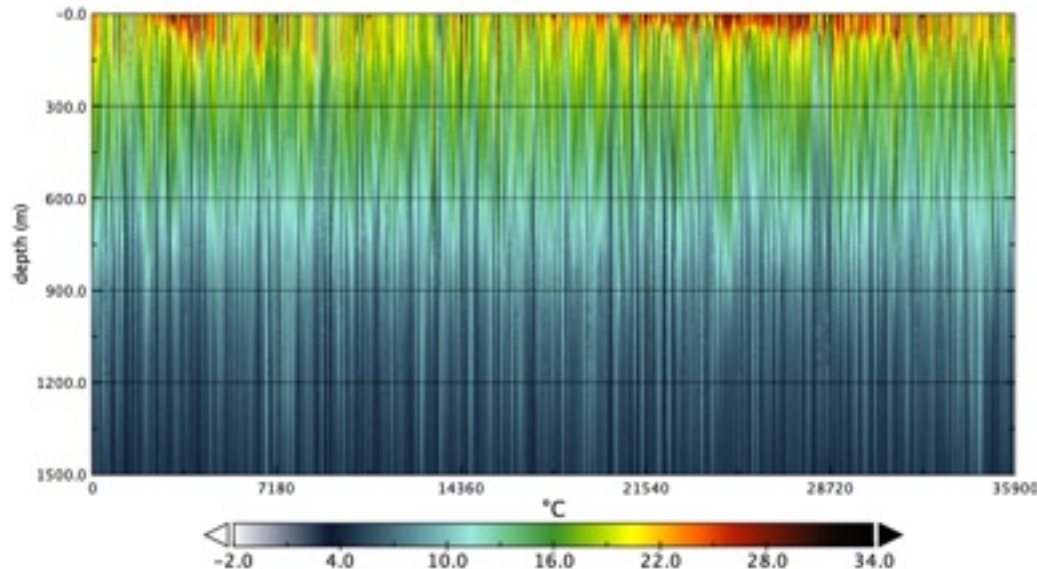
### In situ vertical profiles

- CMEMS CORA 5.2 quality controlled temperature and salinity from CTD and Argo profiles (Szekely et al., 2019)
- WORLD OCEAN ATLAS 13 monthly objectively analyzed ( $1^\circ \times 1^\circ$  grid) climatological fields of in situ temperature, salinity

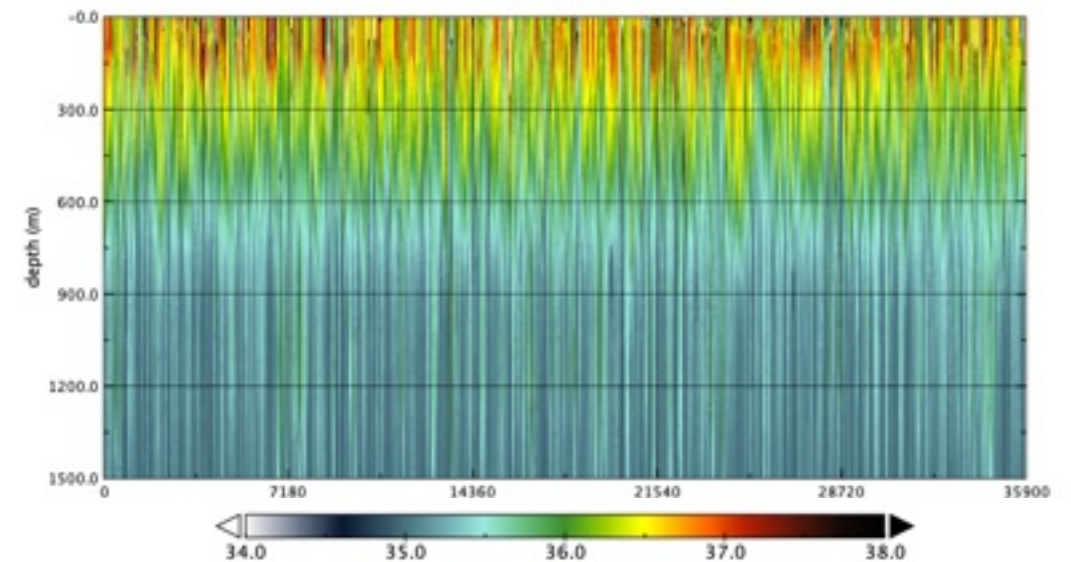
Argo profiles



temperature



salinity



All reconstruction techniques tested here project the anomalies of sea surface temperature (SST), sea surface salinity (SSS) and adjusted absolute dynamic topography (ADT) at depth based on information extracted from **T, S, and steric height anomaly profiles** (all anomalies are computed vs climatologies)

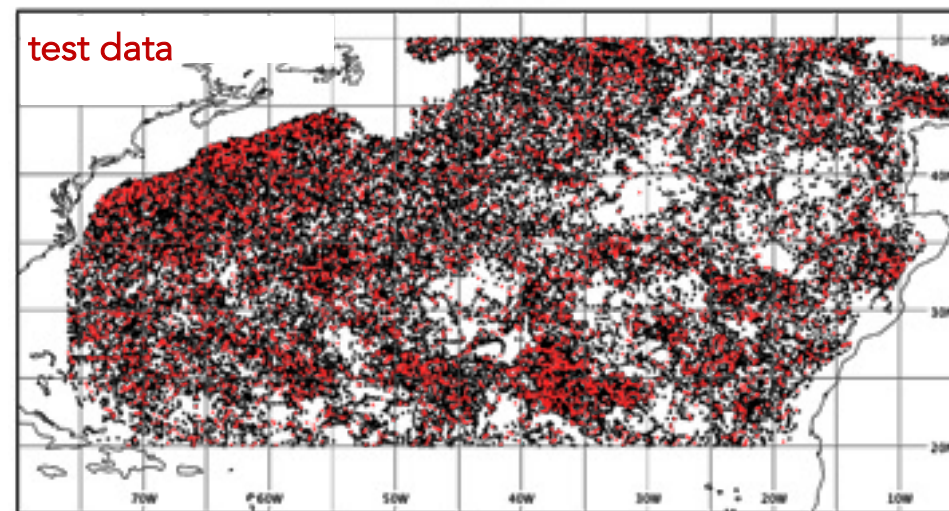
>35000 in situ vertical profiles

Assessment of reconstruction techniques requires

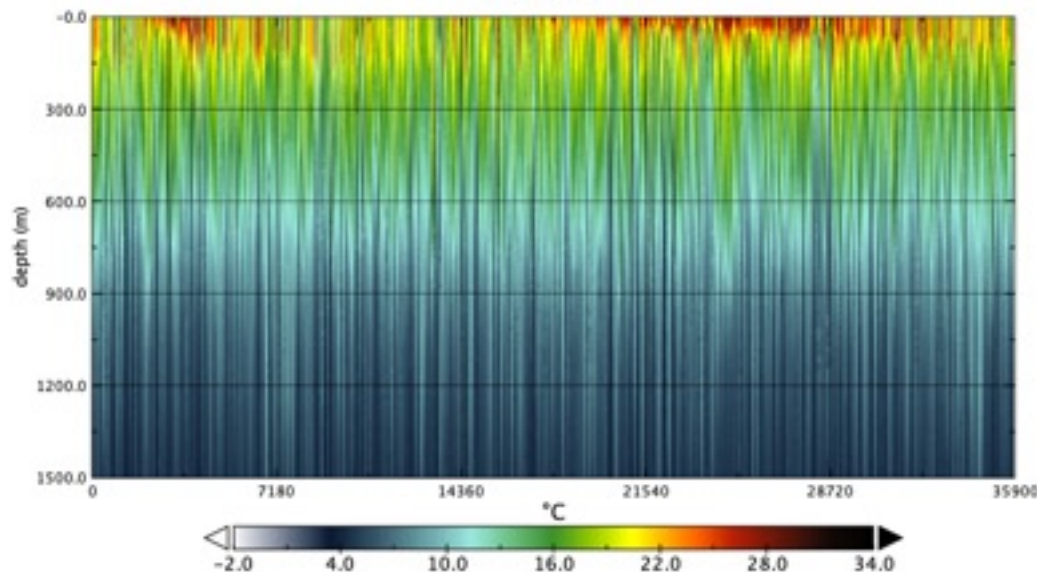
- training dataset
- test dataset (independent from training)

→ 15% of profiles kept for test (>5000)

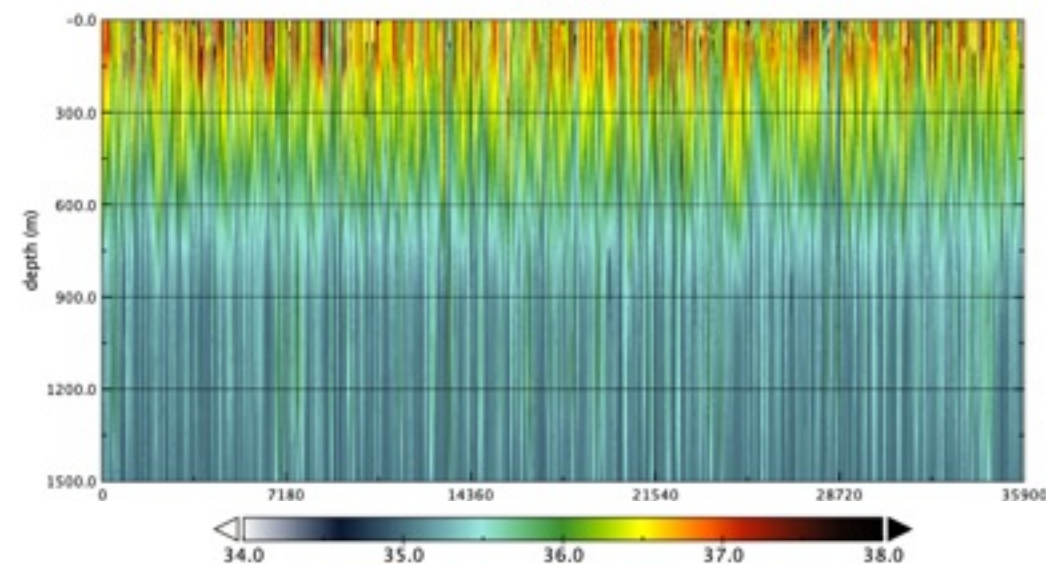
Argo profiles



temperature



salinity



The **multivariate Empirical Orthogonal Function reconstruction (mEOF-r)** is based on the EOF decomposition of a state vector that includes T,S,SH climatological anomalies from ARGO profiles

**Hypotheses:** few modes explain the most of the variability, surface values are known (SSS, SST, adjusted ADT)

- including Steric Heights favours extraction of dynamical information (but altimeter data require specific adjustment)
- anomalies computed vs WOA13 climatology

state vector =  $[T(1), T(2), \dots, T(m), S(1), S(2), \dots, S(m), SH(1), SH(2), \dots, SH(m)]$

$$T(z,t) = \sum_{k=1}^n a_k(t)L_k(z)$$

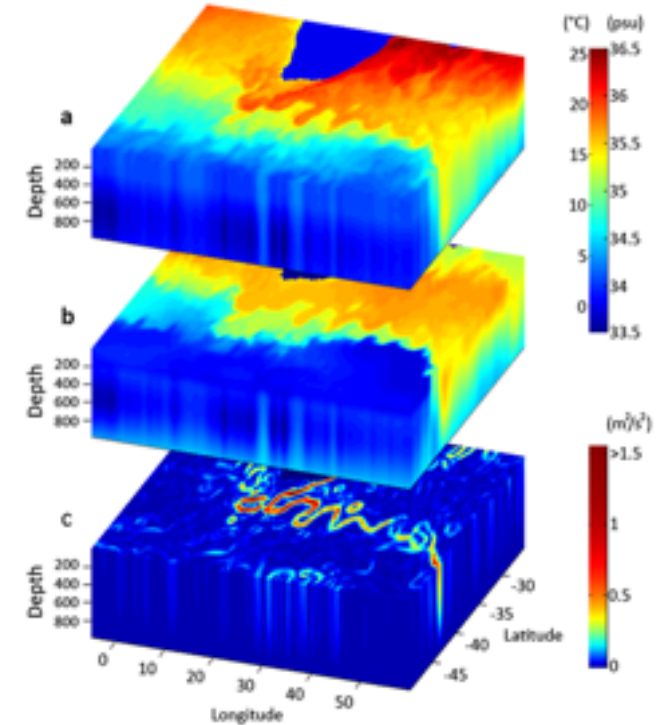
$$S(z,t) = \sum_{k=1}^n a_k(t)M_k(z)$$

$$SH(z,t) = \sum_{k=1}^n a_k(t)N_k(z)$$

**Core of mEOF-R method**

$$\begin{cases} a_1(t)L_1(0) + a_2(t)L_2(0) + a_3(t)L_3(0) = T(0,t) \\ a_1(t)M_1(0) + a_2(t)M_2(0) + a_3(t)M_3(0) = S(0,t) \\ a_1(t)N_1(0) + a_2(t)N_2(0) + a_3(t)N_3(0) = SH(0,t) \end{cases}$$

*known from surface input*



**mEOF decomposition**

k-th EOF amplitude =  $a_k(t)$

k-th EOF pattern =  $[L_k(1), L_k(2), \dots, L_k(m), M_k(1), M_k(2), \dots, M_k(m), N_k(1), N_k(2), \dots, N_k(m)]$

Buongiorno Nardelli B., Santoleri R., *J. Atmos. Ocean. Tech.* 2005  
 Buongiorno Nardelli B. et al., *J. Geophys. Res.* 2006  
 Buongiorno Nardelli B. et al., *Ocean Sci.* 2012  
 Buongiorno Nardelli, *JGR*, 2013  
 Buongiorno Nardelli et al., *JGR*, 2018a,b

solution proposed initially within ESA-WOC contract  
 → version 0 of WOC\_NATL3D (not released to the public)

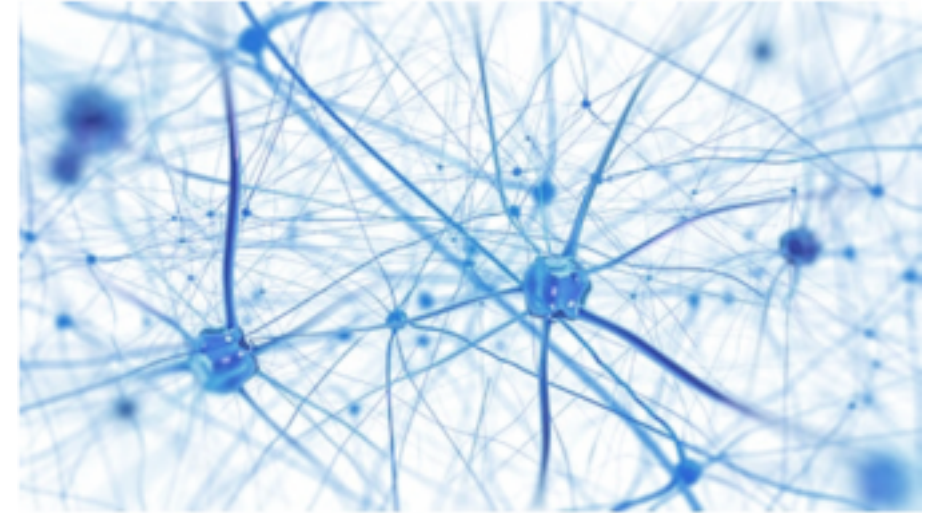
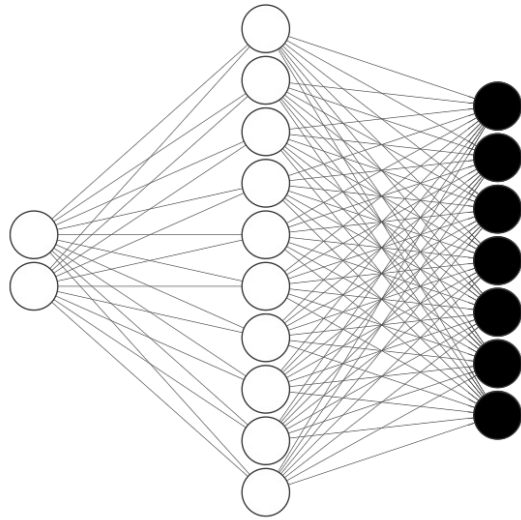


Artificial Neural Networks (ANN) are perfect candidates for regression/prediction problems

- loosely inspired by the functioning of animal brains
- built as non-linear models
- parameters estimated by "learning" from available data

input vector variable  $\mathbf{x}$  (**predictor**) related to an output vector (or scalar) variable  $\mathbf{y}$  (**target**) by nesting several non linear functions:

$$\mathbf{y} = \mathcal{M}(\mathbf{x}) = f(h(\dots(\mathbf{x})))$$



"Learning" is the process of "fitting" ANN model parameters to observed data (a.k.a. optimization). This is done by minimizing differences between model output and observed data (*loss function*).



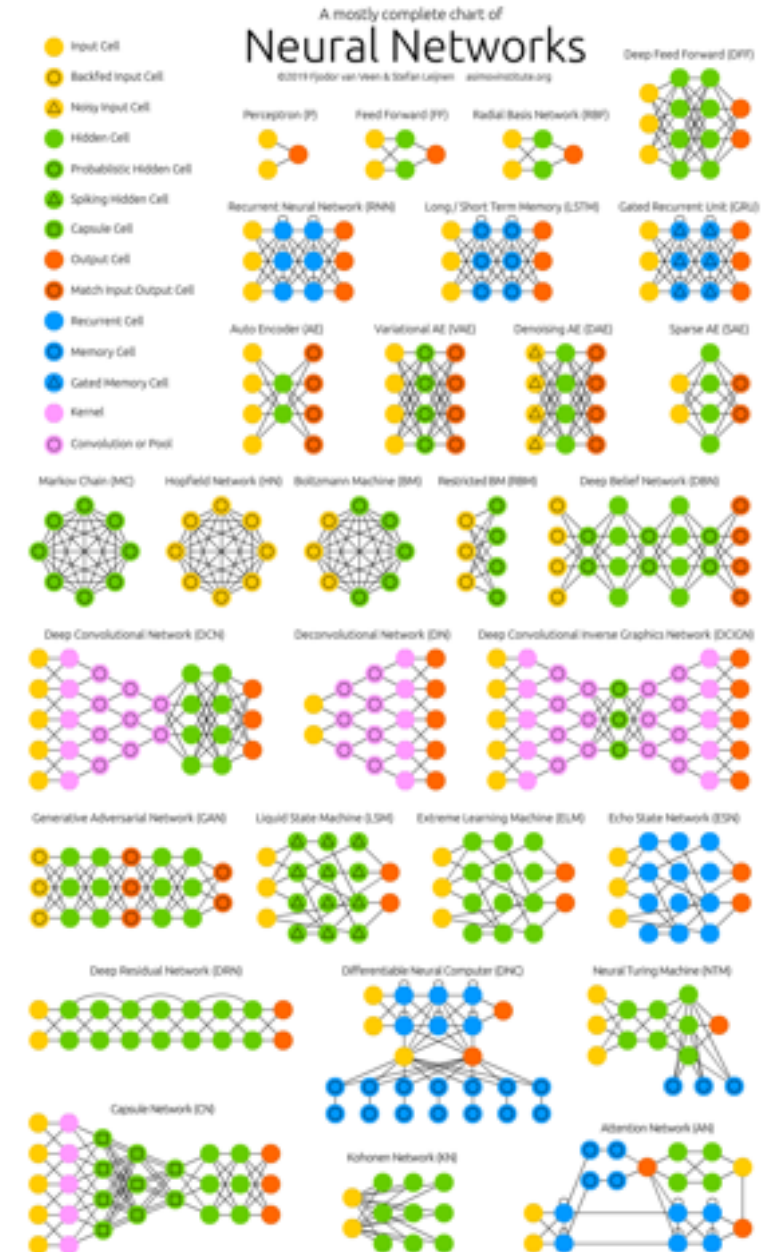
Artificial Neural Networks (ANN) are perfect candidates for regression/prediction problems

- loosely inspired by the functioning of animal brains
- built as non-linear models
- parameters estimated by "learning" from available data

input vector variable  $\mathbf{x}$  (**predictor**) related to an output vector (or scalar) variable  $\mathbf{y}$  (**target**) by nesting several non linear functions:

$$\mathbf{y} = \mathcal{M}(\mathbf{x}) = f(h(\dots(\mathbf{x})))$$

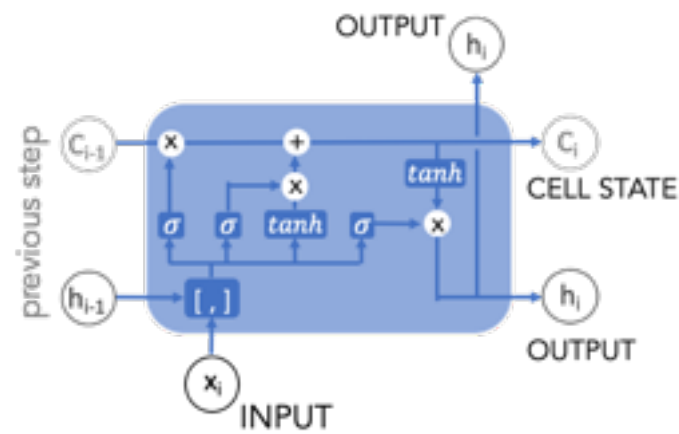
The choice of network architecture defines the "family" of solutions that can be learned from data



Long Short Term Memory network coupled to a Monte Carlo dropout method to estimate vertical profiles and associated errors

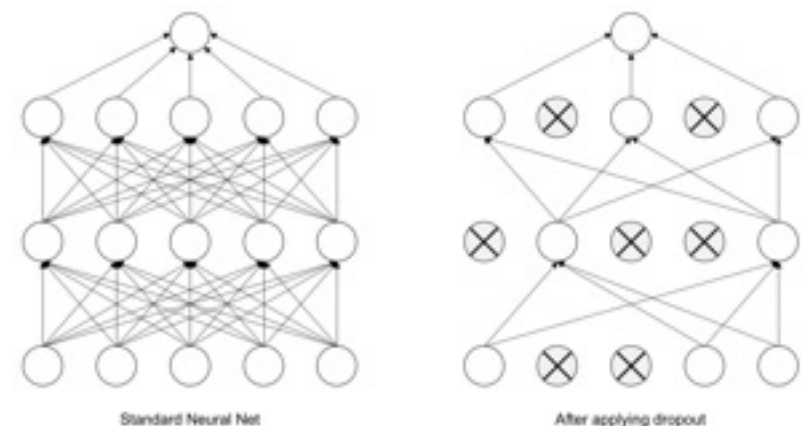
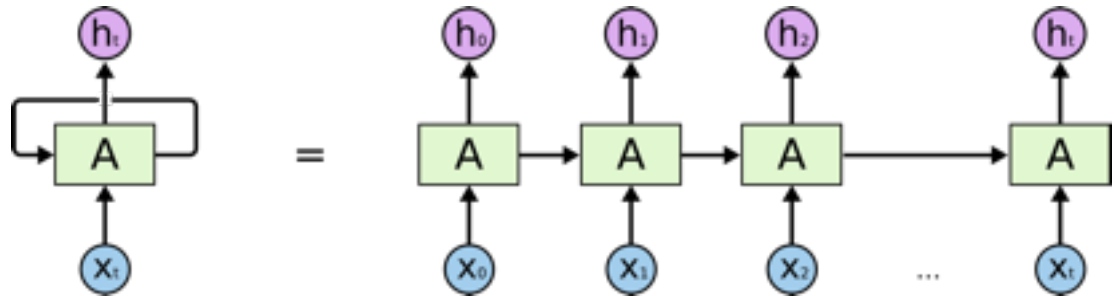
**Long Short Time Memory (LSTM)**

Networks are efficient in exploiting the information present in sequences of data. They do this by iteratively processing input sequences through cells that combine input data and information from the previous step... the core information is included in the cell state that is directly transmitted to the next cell (acting as a network "memory")



- LSTM CELL**
- $\otimes$  pointwise product
  - $+$  pointwise addition
  - $\sigma$  sigmoid activation
  - $\tanh$  hyperbolic tangent activation
  - $[ \cdot ]$  vector concatenation

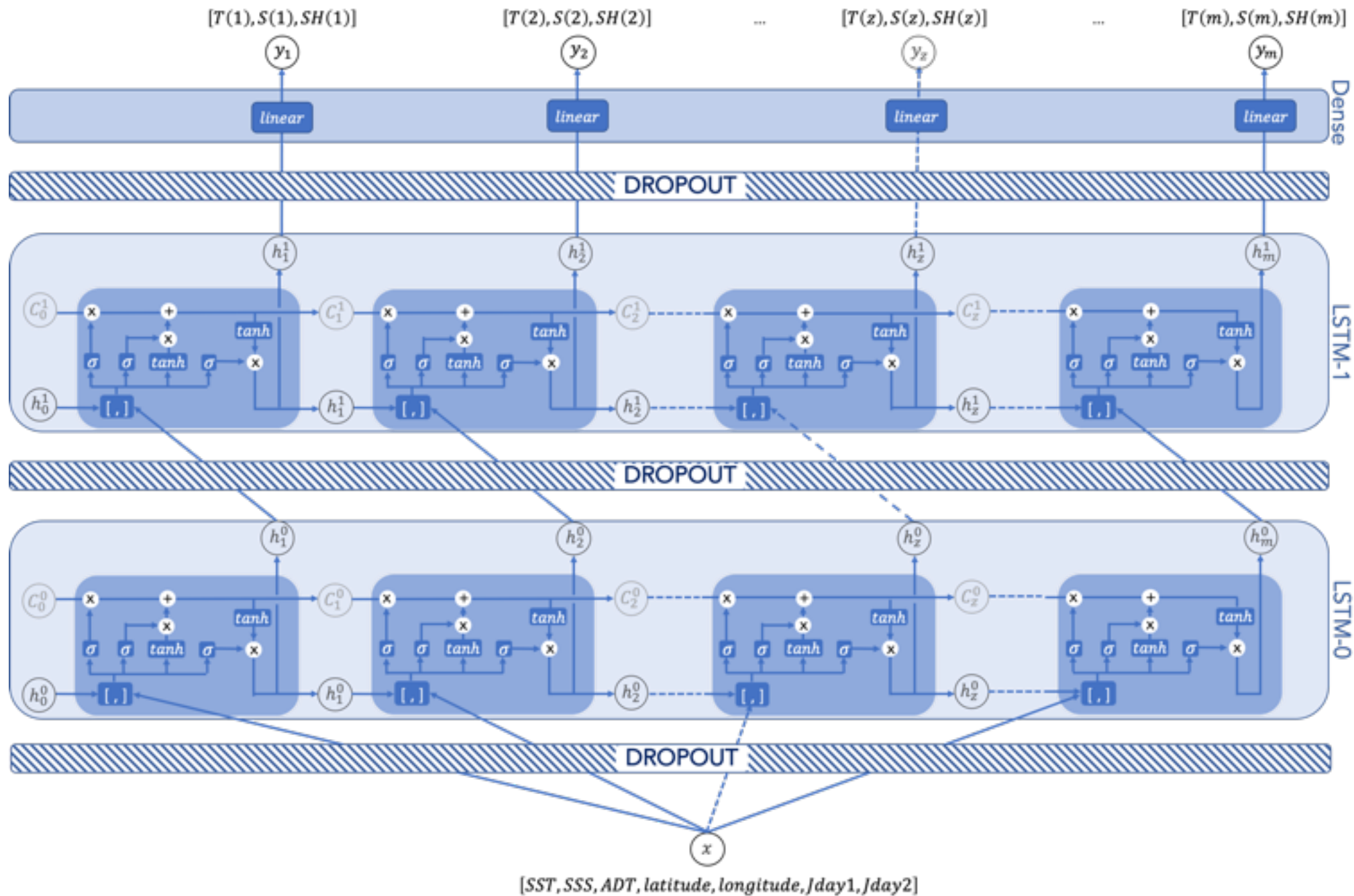
GENERIC RECURRENT NETWORK ARCHITECTURE



**Dropout:** Running a neural network regression several times with dropout during testing generates different output for the same input. These output are equivalent to Monte-Carlo sampling (Srivastava, et al. 2014). Thus, ensemble mean and variance provide the network's output values and related uncertainty, respectively.



WOC-NATL3D stacked Long Short Term Memory network

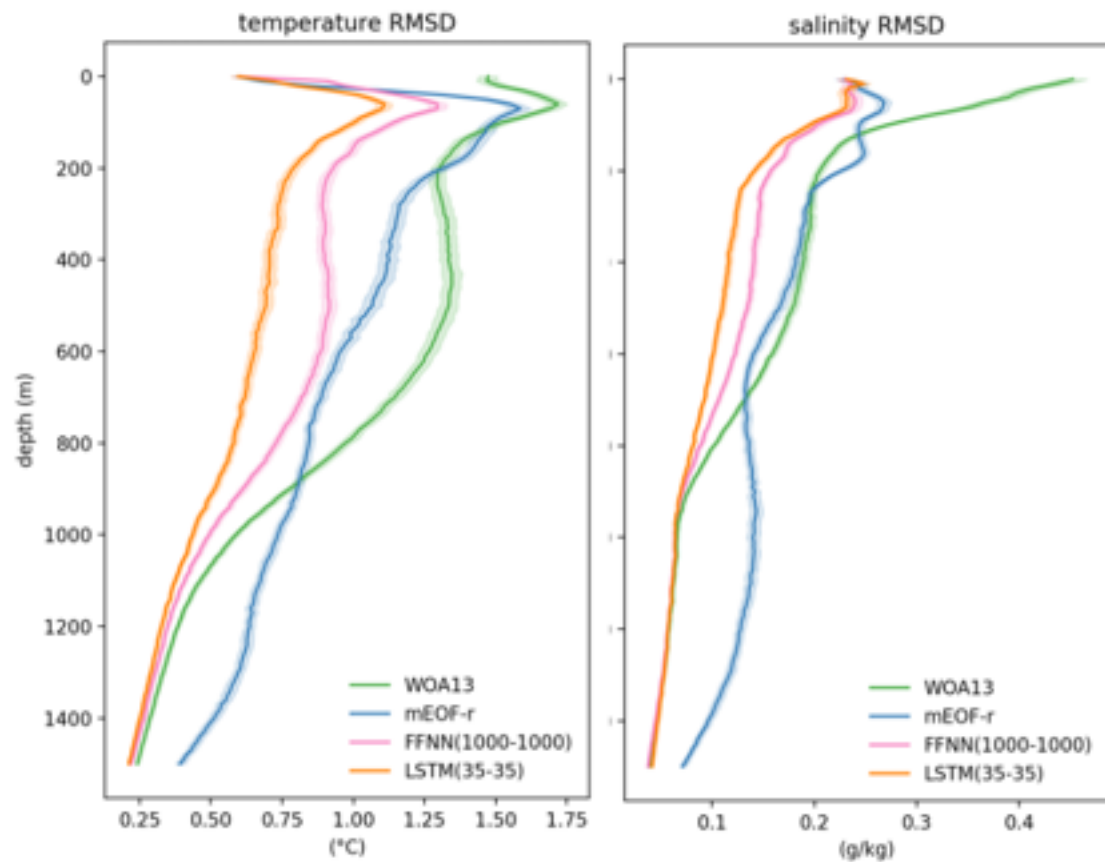




## Accuracy

→ RMSD between observed and reconstructed vertical profiles (independent test dataset) compared to RMSD between observed profiles and:

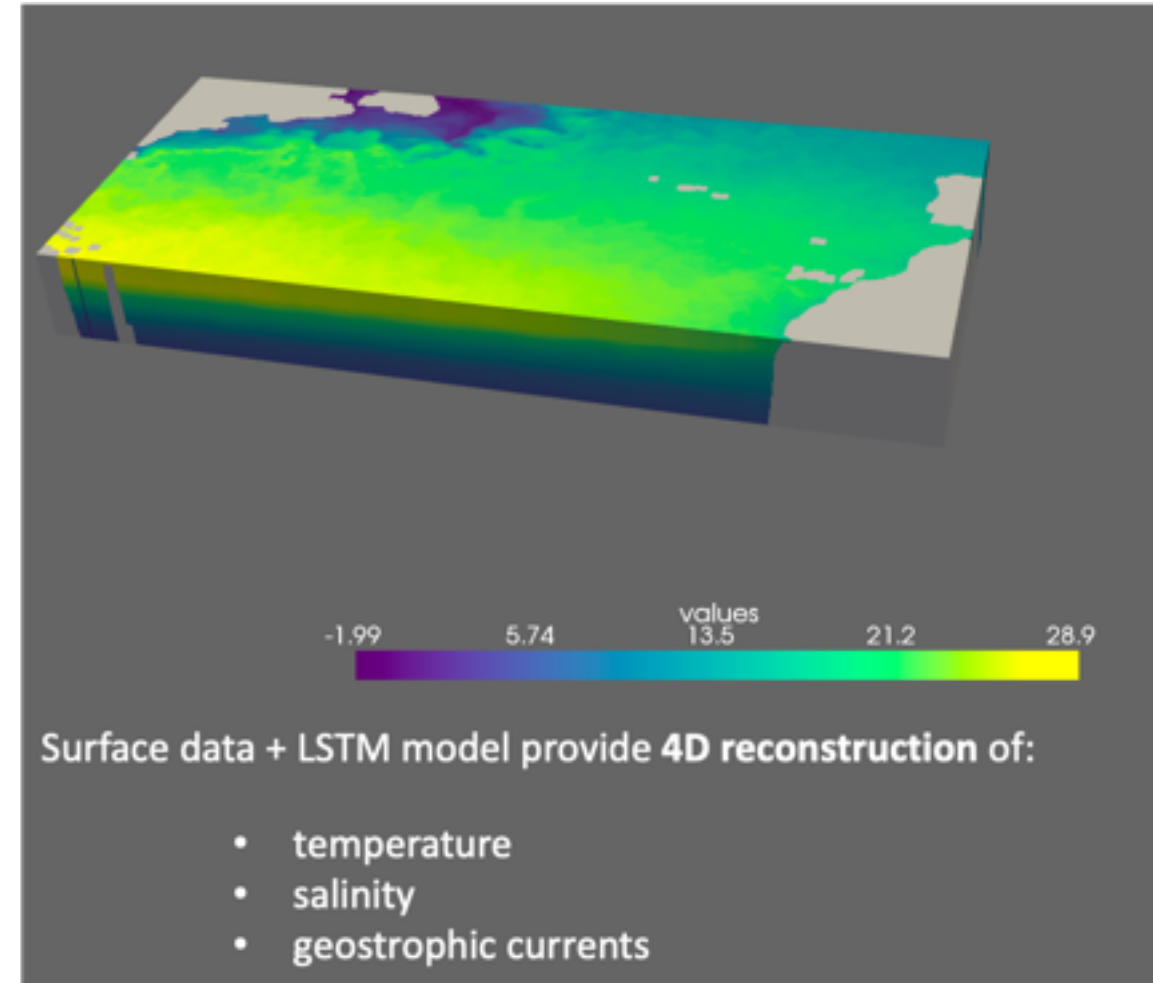
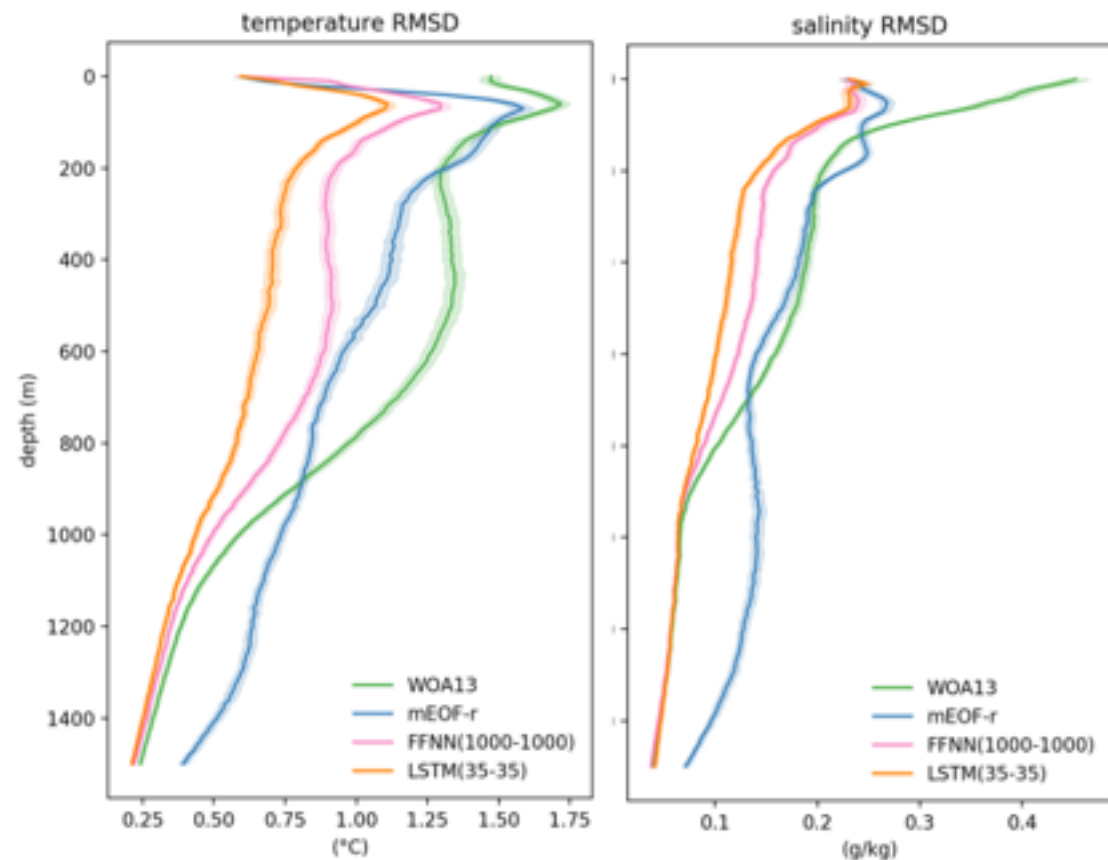
- standard feed-forward neural network (FFNN)
- multivariate EOF reconstruction (mEOF)
- climatology (WOA13)



## Accuracy

→ RMSD between observed and reconstructed vertical profiles (independent test dataset) compared to RMSD between observed profiles and:

- standard feed-forward neural network (FFNN)
- multivariate EOF reconstruction (mEOF)
- climatology (WOA13)



Q-vector formulation of the quasi-geostrophic Omega equation solved to get the vertical velocity fields

$$\nabla_h^2(N^2 w) + f^2 \frac{\partial^2 w}{\partial z^2} = \nabla_h \cdot \mathbf{Q} \quad \mathbf{Q} = 2\mathbf{Q}_{twg} + \mathbf{Q}_{th} + \mathbf{Q}_{dm}$$

kinematic deformation

$$\mathbf{Q}_{twg} = \frac{g}{\rho_0} \left( \frac{\partial u_g}{\partial x} \frac{\partial \rho}{\partial x} + \frac{\partial v_g}{\partial x} \frac{\partial \rho}{\partial y}, \frac{\partial u_g}{\partial y} \frac{\partial \rho}{\partial x} + \frac{\partial v_g}{\partial y} \frac{\partial \rho}{\partial y} \right)$$

turbulent momentum

$$\mathbf{Q}_{dm\_COP} = \frac{f}{\rho_0} \left( \frac{\partial^2}{\partial z^2} \left[ \rho \mathbf{K}_m \left( \frac{\partial v_g}{\partial z} - \gamma_v \right) \right], -\frac{\partial^2}{\partial z^2} \left[ \rho \mathbf{K}_m \left( \frac{\partial u_g}{\partial z} - \gamma_v \right) \right] \right)$$

turbulent buoyancy

$$\mathbf{Q}_{th} = -\frac{g}{\rho_0} \nabla_h \left( \frac{\partial}{\partial z} \left[ K_\rho \left( \frac{\partial \rho}{\partial z} - \gamma_\rho \right) \right] \right) = \nabla_h \left( \frac{\partial}{\partial z} \left[ K_\rho \left( N^2 + \frac{g}{\rho_0} \gamma_\rho \right) \right] \right)$$

→ KPP parameterization of viscosity/diffusivity ( $K_x$ ) and non-local effective gradients  $\gamma_x$ . (Smyth et al., 2001)



Q-vector formulation of the quasi-geostrophic Omega equation solved to get the vertical velocity fields

$$\nabla_h^2 (N^2 w) + f^2 \frac{\partial^2 w}{\partial z^2} = \nabla_h \cdot \mathbf{Q} \quad \mathbf{Q} = 2\mathbf{Q}_{twg} + \mathbf{Q}_{th} + \mathbf{Q}_{dm}$$

kinematic deformation

$$\mathbf{Q}_{twg} = \frac{g}{\rho_0} \left( \frac{\partial u_g}{\partial x} \frac{\partial \rho}{\partial x} + \frac{\partial v_g}{\partial x} \frac{\partial \rho}{\partial y}, \frac{\partial u_g}{\partial y} \frac{\partial \rho}{\partial x} + \frac{\partial v_g}{\partial y} \frac{\partial \rho}{\partial y} \right)$$

turbulent momentum

$$\mathbf{Q}_{dm\_woc} = \frac{f}{\rho_0} \left( \frac{\partial^2}{\partial z^2} \left[ \rho \mathbf{K}_m \left( \frac{\partial v_g}{\partial z} + \frac{\partial \mathbf{v}_{Ekman}}{\partial z} = \boldsymbol{\gamma}_v \right) \right], - \frac{\partial^2}{\partial z^2} \left[ \rho \mathbf{K}_m \left( \frac{\partial u_g}{\partial z} + \frac{\partial \mathbf{u}_{Ekman}}{\partial z} = \boldsymbol{\gamma}_u \right) \right] \right)$$

→ combination of empirical estimates and KPP for tracers ~~and momentum~~ (Smyth et al., 2001) non-local effective gradient,  $\gamma_\rho$ , and viscosity/diffusivity,  $K_x$ .

turbulent buoyancy

$$\mathbf{Q}_{th} = - \frac{g}{\rho_0} \nabla_h \left( \frac{\partial}{\partial z} \left[ K_\rho \left( \frac{\partial \rho}{\partial z} - \gamma_\rho \right) \right] \right) = \nabla_h \left( \frac{\partial}{\partial z} \left[ K_\rho \left( N^2 + \frac{g}{\rho_0} \gamma_\rho \right) \right] \right)$$

**background Ekman velocity** approximated through an analytical fit to CMEMS Ekman empirical reconstruction (MULTIOBS\_GLO\_PHY\_REP\_015\_004)

$$u_{Ekman}(z) = e^{\frac{z}{D_{amp}}} [u_0 \cos(z/D_{rot}) - v_0 \sin(z/D_{rot})]$$

$$v_{Ekman}(z) = e^{\frac{z}{D_{amp}}} [u_0 \sin(z/D_{rot}) + v_0 \cos(z/D_{rot})]$$

**viscosity in the Ekman layer** constrained by analytical profile (defined as in Nagai et al., 2006) estimated empirically (i.e. limited by local Ekman amplitude decay scale)

$$K_m(z) = K_{max} \left[ 1 + \tanh \left( \frac{z - D_{amp}}{\delta} \right) \right] \quad K_{max} = \frac{f D_{amp}^2}{2}$$



## → horizontal ageostrophic components

Once the Omega equation is solved for  $w$ , horizontal ageostrophic components can be estimated by integrating two expressions that are obtained during the analytical derivation of the omega equation:

$$u_a(z) = \int_{REF}^z \frac{\partial u_a}{\partial z} dz = \frac{1}{f^2} \int_{REF}^z \left( \frac{\partial}{\partial x} (N^2 w) - \frac{f}{\rho_0} \frac{\partial}{\partial z} \left( \frac{\partial \tau_{yz}}{\partial z} \right) - 2 \frac{g}{\rho_0} \left( \frac{\partial u_g}{\partial x} \frac{\partial \rho}{\partial x} + \frac{\partial v_g}{\partial x} \frac{\partial \rho}{\partial y} \right) - \frac{g}{\rho_0} \frac{\partial}{\partial x} \left( \frac{\partial F_{\rho z}}{\partial z} \right) \right) dz$$

$$v_a(z) = \int_{REF}^z \frac{\partial v_a}{\partial z} dz = \frac{1}{f^2} \int_{REF}^z \left( \frac{\partial}{\partial y} (N^2 w) + \frac{f}{\rho_0} \frac{\partial}{\partial z} \left( \frac{\partial \tau_{xz}}{\partial z} \right) - 2 \frac{g}{\rho_0} \left( \frac{\partial u_g}{\partial y} \frac{\partial \rho}{\partial x} + \frac{\partial v_g}{\partial y} \frac{\partial \rho}{\partial y} \right) - \frac{g}{\rho_0} \frac{\partial}{\partial y} \left( \frac{\partial F_{\rho z}}{\partial z} \right) \right) dz$$

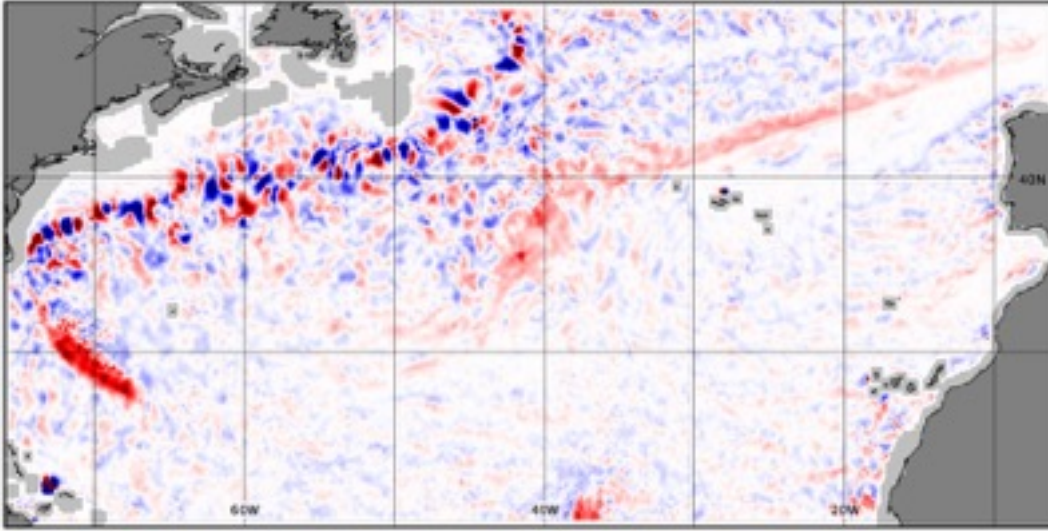
where we have defined:

$$\begin{aligned} \tau_{xz} &= \rho K_m \left( \frac{\partial u}{\partial z} \right) \\ \tau_{yz} &= \rho K_m \left( \frac{\partial v}{\partial z} \right) \\ F_{\rho z} &= K_\rho \left( \frac{\partial \rho}{\partial z} - \gamma_\rho \right) \end{aligned}$$

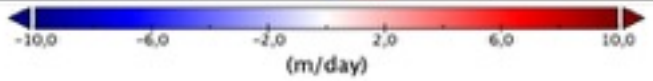
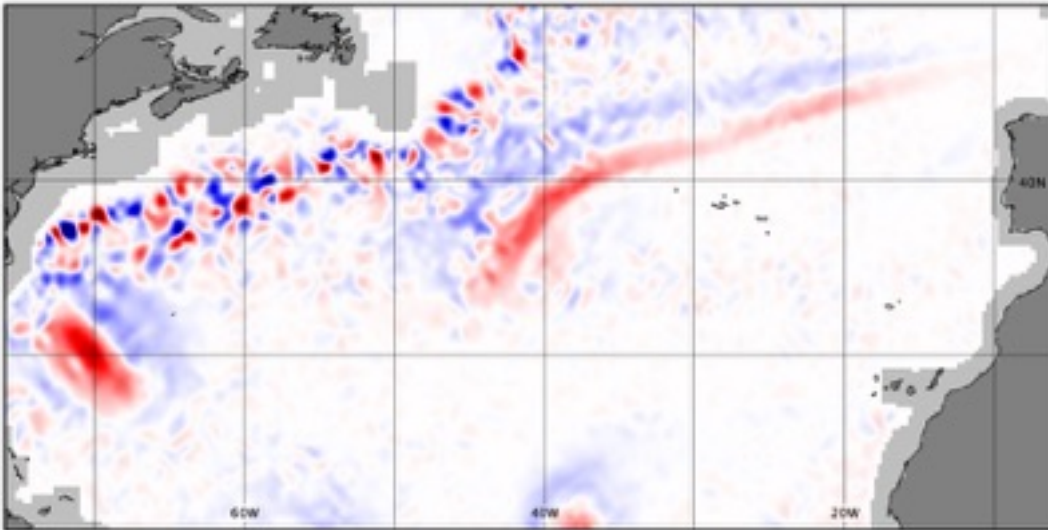
and assumed that the ageostrophic velocities can be neglected at the reference layer considered in the integral (here taken as the deepest level).



NATL3D vertical velocity at 50 m



OMEGA3D vertical velocity at 50 m

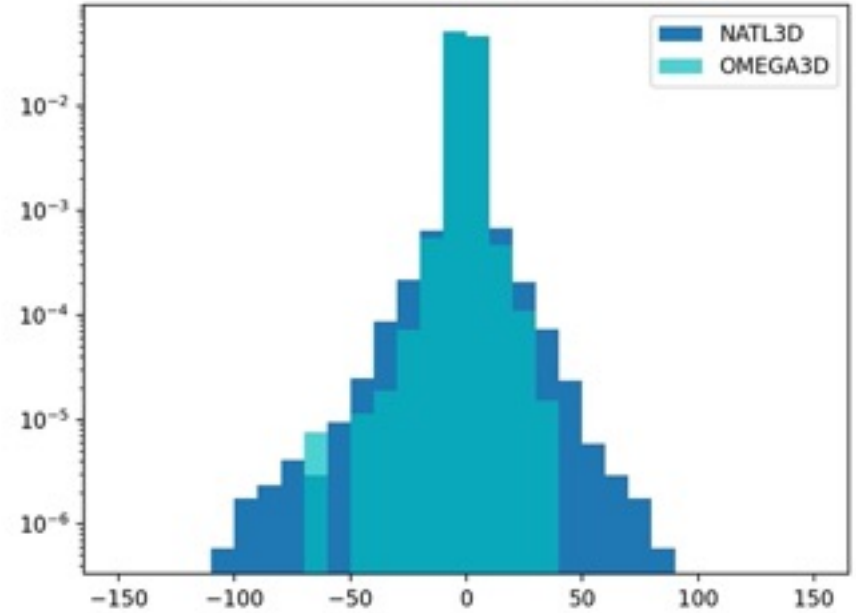


### Qualitative comparison

NATL3D vertical velocity and OMEGA3D vertical velocity at 50 m on 2018-09-12

Histogram of the differences between NATL3D and OMEGA3D vertical velocities at 100 m depth on 2018-09-12

Normlized distribution of w values at 100 m

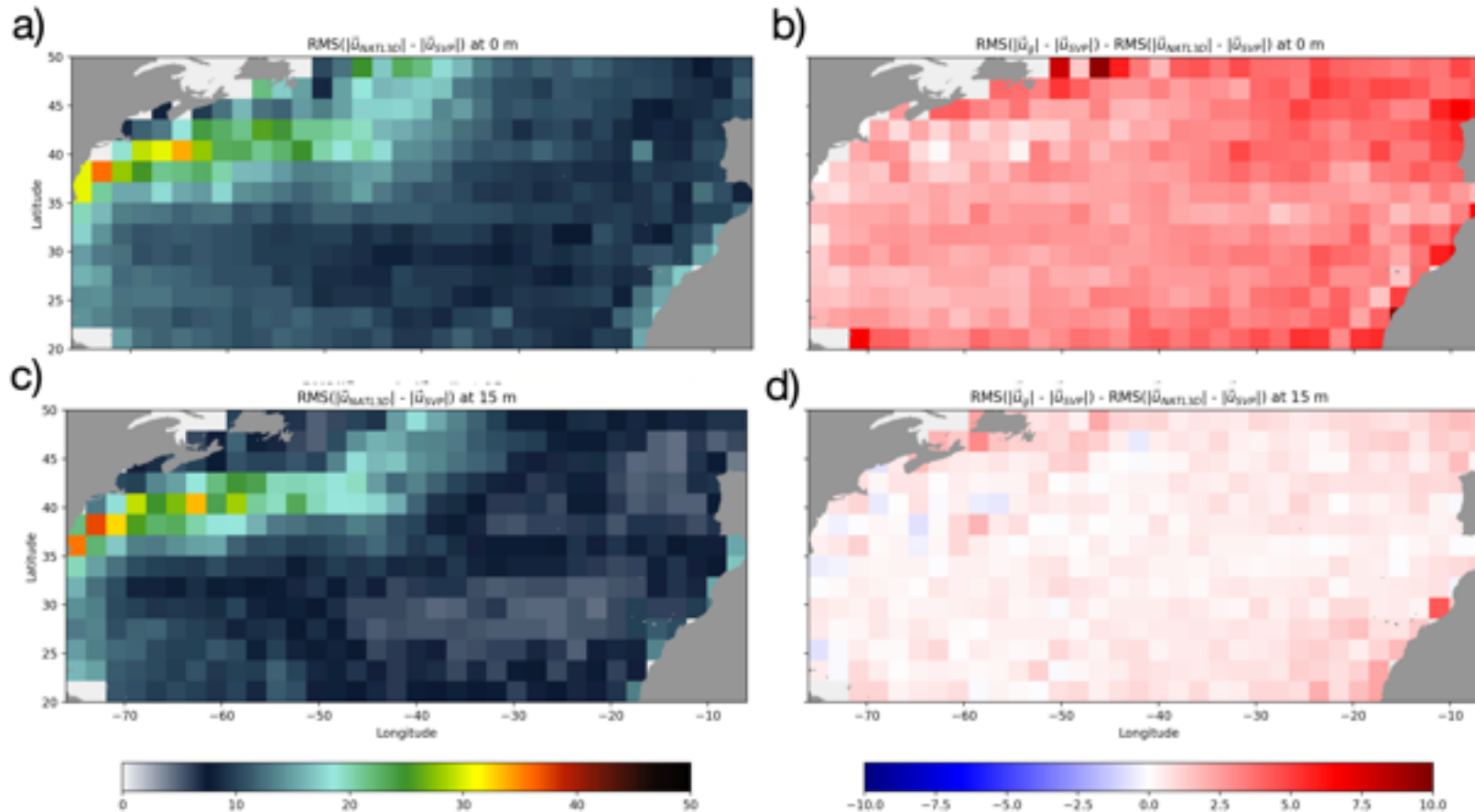


Total horizontal and geostrophic components have been compared with independent estimates of the ocean currents retrieved from SVP drifting buoys over the **entire timeseries** (2010-2019).

**Total horizontal velocities RMSD:** **0.119±0.001** m/s at 0 m and **0.113±0.001** m/s at 15 m

**Geostrophic velocities RMSD:** **0.145±0.001** m/s at 0 m and **0.117±0.001** m/s at 15 m

# matchups used to compute the statistics: 311735 for undrogued SVP velocities (at 0) m and 243742 for drogued SVP data (at 15 m). Confidence intervals are estimated with bootstrapping ( $1\sigma$ ).



Positive values indicate an improvement with respect to geostrophy

WOC-NATL3D algorithm includes several improvements with respect to Copernicus, involving all processing steps.

**Planned future research:**

- test different parameterizations of vertical mixing
- test impact of improved surface stress estimates
- test new surface Ekman current estimates

Present **roadmap for further improvements** includes:

- **New algorithms/set-up for surface input data retrieval**
  - SSS based on in situ+SMOS+SMAP data
  - test of super-resolution deep convolutional neural network algorithms for ADT and joint SST/ADT retrieval (also though physically-informed approach)
- test of **new/refined 3D reconstruction** deep learning algorithms
- development of **3D Omega solvers** based on deep learning

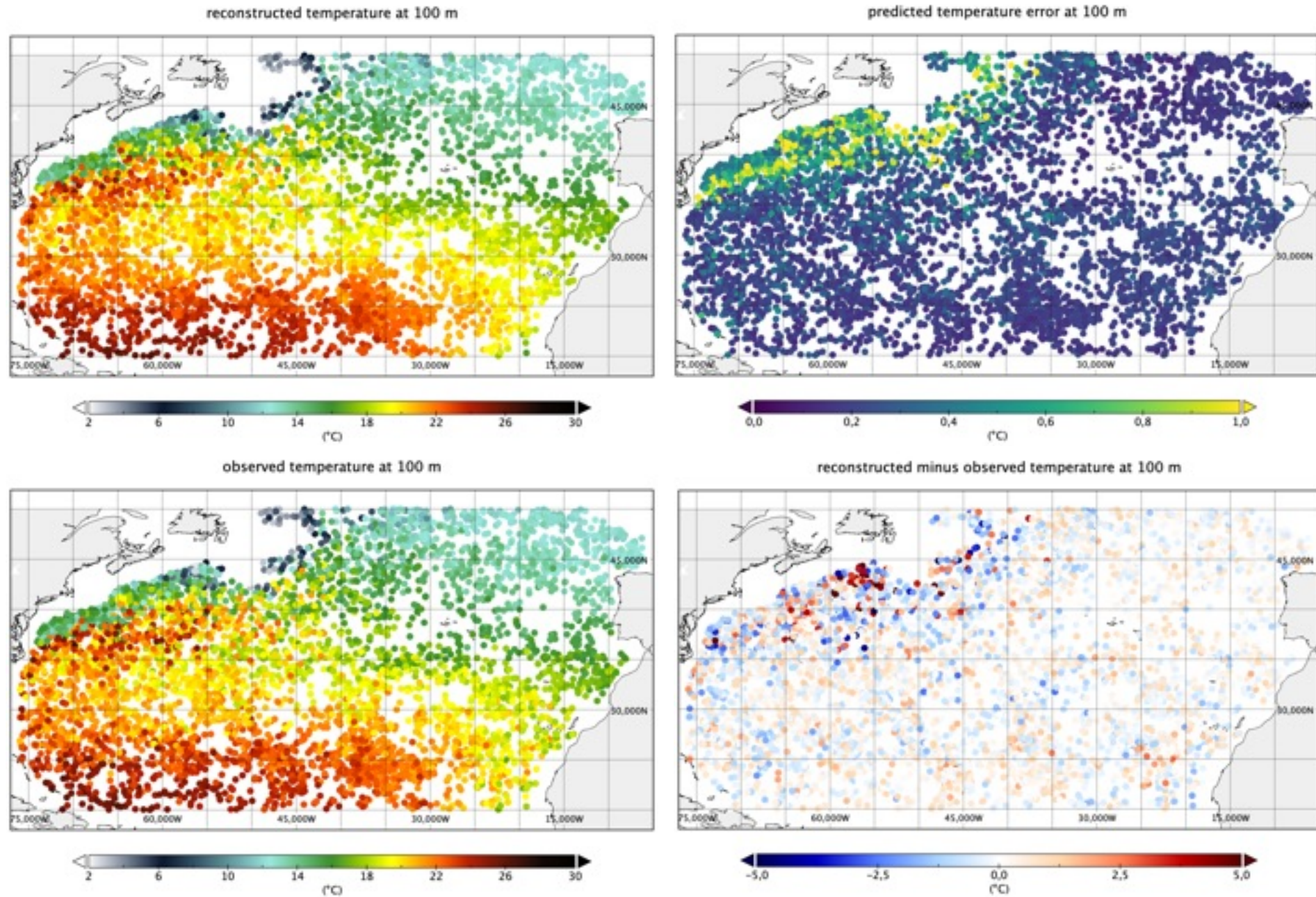




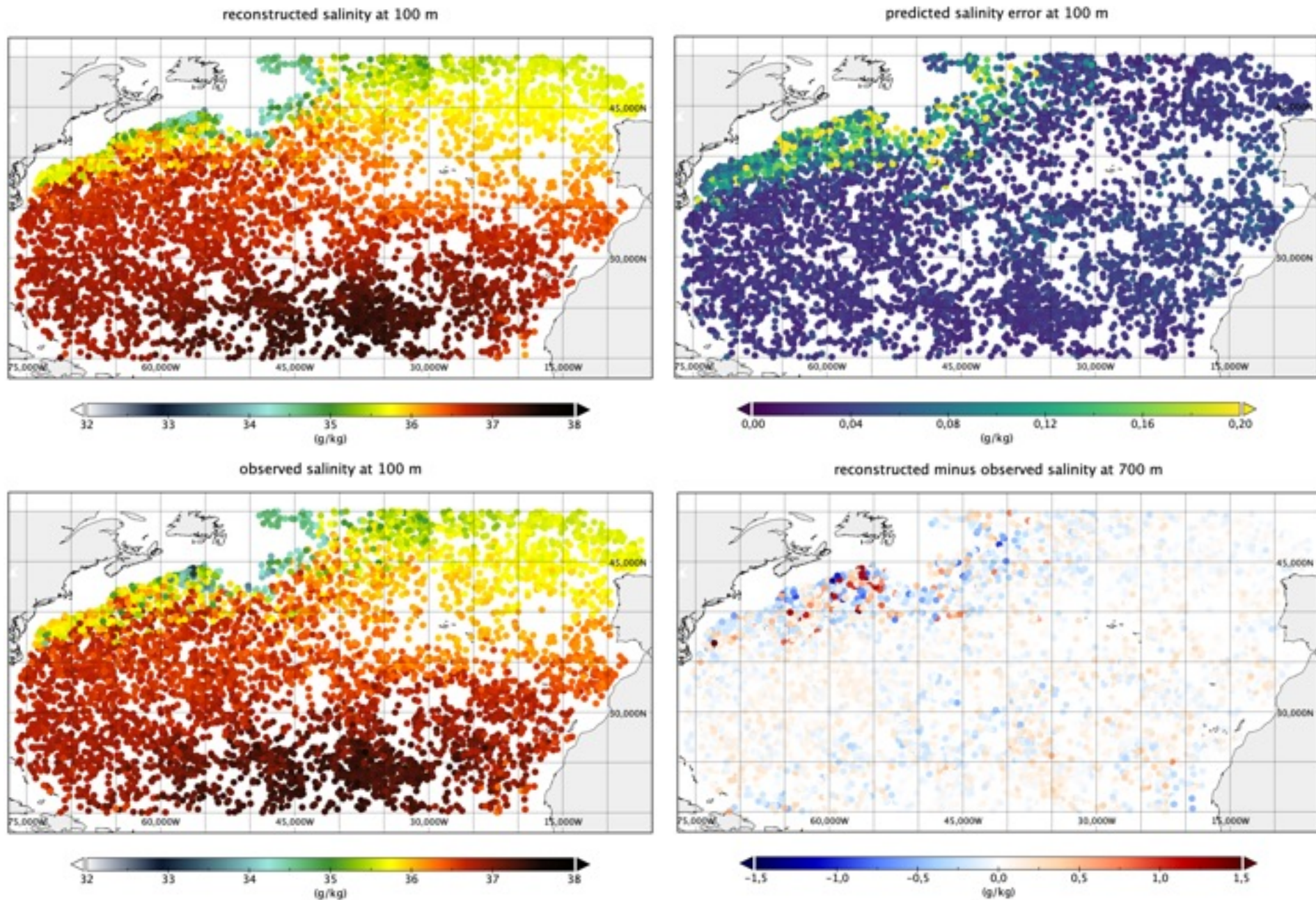
**Additional slides**



## 1-Stacked LSTM to project surface information at depth: temperature reconstruction uncertainties



## 1-Stacked LSTM to project surface information at depth: salinity reconstruction uncertainties





Letter

# A Deep Learning Network to Retrieve Ocean Hydrographic Profiles from Combined Satellite and In Situ Measurements

Bruno Buongiorno Nardelli

Consiglio Nazionale delle Ricerche, Istituto di Scienze Marine (CNR-ISMAR), 80133 Naples, Italy;  
bruno.buongiornoardelli@cnr.it

Received: 5 September 2020; Accepted: 24 September 2020; Published: 25 September 2020



bbuong / 3Drec

<> Code Issues Pull requests Actions Projects Wiki Security Insights Settings

master 1 branch 0 tags

Go to file Add file Code

File	Commit Message	Commit ID	Date	Commits
LICENSE	Initial commit	7941d76	on 25 Sep	13 commits
README.md	Update README.md			2 months ago
WOC_FFNN3D_model_github.py	Add files via upload			2 months ago
WOC_LSTM3D_model_github.py	Add files via upload			2 months ago

README.md

## 3Drec

Made with Python

3Drec provides the implementation of two deep learning networks designed to reconstruct the 3D ocean structure from 2D satellite data: one based on a deep feed-forward network (FFNN3D) and one based on a stacked Long-Short Term Memory network (LSTM3D).

Search Upload Communities

July 14, 2020

Dataset Open Access

ESA-WOC North Atlantic Sea Surface Salinity maps from a multivariate combination of satellite and in situ surface measurements (2010-2018)

Buongiorno Nardelli, Bruno

Search Upload Communities

September 21, 2020

Dataset Open Access

Developing a deep Learning network to retrieve ocean hydrographic profiles in the North Atlantic from combined satellite and in situ measurements: training datasets

Buongiorno Nardelli, Bruno



## CMEMS Algorithm

→ issues in the surface layer

In depth analysis of OMEGA3D data revealed **low performance wind-driven surface currents** retrieval at the surface

Data Type	Eastward error	Northward error	Norm error	Field speed	percentage
015_004	0.1109	0.1080	0.1105	0.2180	38.7053
001_024_d	0.1333	0.1254	0.1274	0.2072	44.3085
015_002	0.1301	0.1091	0.1201	0.1784	45.9299
015_007	0.2047	0.2331	0.2357	0.3752	52.0173



## Primitive Equation Omega

$$\nabla_h^2 (N^2 w) + f^2 \frac{\partial^2 w}{\partial z^2} = \nabla_h \cdot \mathbf{Q}$$

$$\mathbf{Q} = 2\mathbf{Q}_{twg} + \mathbf{Q}_{th} + \mathbf{Q}_{dm} + \mathbf{Q}_{dag} + \mathbf{Q}_{dr}$$

Likely due to dynamical inconsistency related to more than one factor:

- Diabatic forcing term estimated from **geostrophic shear** and KPP does not include iterative adjustment  
→ computationally not feasible
- **Thermal Wind Inbalance forcing terms ( $\mathbf{Q}_{dr}, \mathbf{Q}_{dag}$ )** not negligible if too far from Ekman balance (not stationary)

$$\mathbf{Q}_{dm} = \frac{f}{\rho_0} \left( \frac{\partial^2}{\partial z^2} \left[ \rho K_m \left( \frac{\partial v_g}{\partial z} + \frac{\partial v_a}{\partial z} - \gamma_v \right) \right], - \frac{\partial^2}{\partial z^2} \left[ \rho K_m \left( \frac{\partial u_g}{\partial z} + \frac{\partial u_a}{\partial z} - \gamma_u \right) \right] \right)$$

$$\mathbf{Q}_{dr} = f \left( \frac{D}{Dt} \left( \frac{\partial v_a}{\partial z} \right), - \frac{D}{Dt} \left( \frac{\partial u_a}{\partial z} \right) \right)$$

$$\mathbf{Q}_{dag} = f \left( \frac{\partial v}{\partial x} \frac{\partial u_a}{\partial z} - \frac{\partial u}{\partial x} \frac{\partial v_a}{\partial z}, \frac{\partial v}{\partial y} \frac{\partial u_a}{\partial z} - \frac{\partial u}{\partial y} \frac{\partial v_a}{\partial z} \right)$$

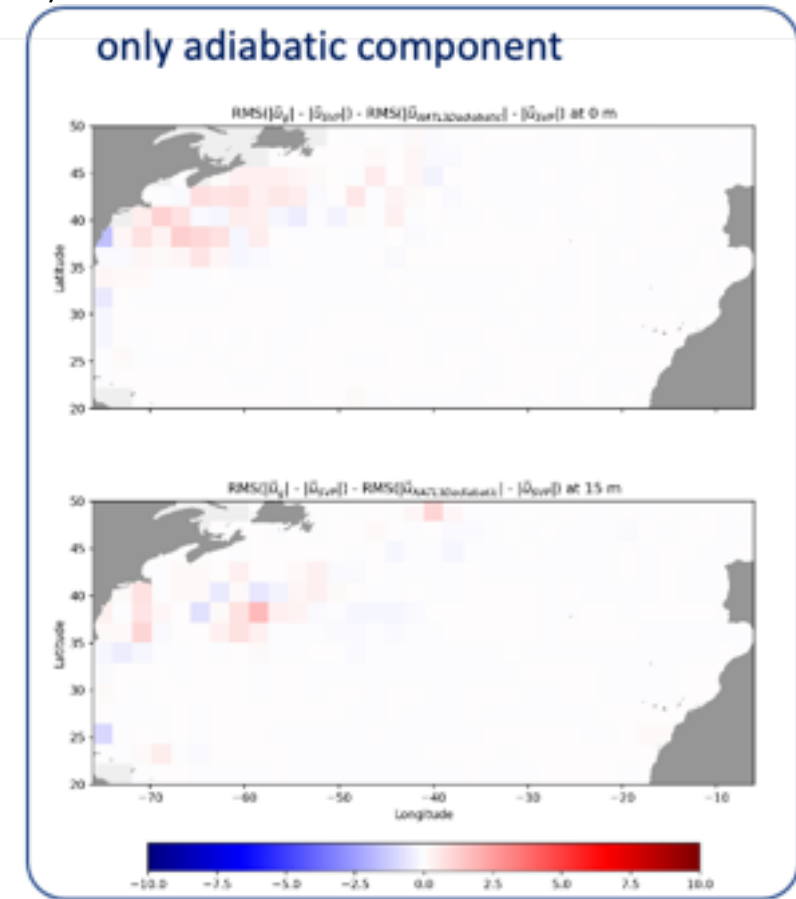
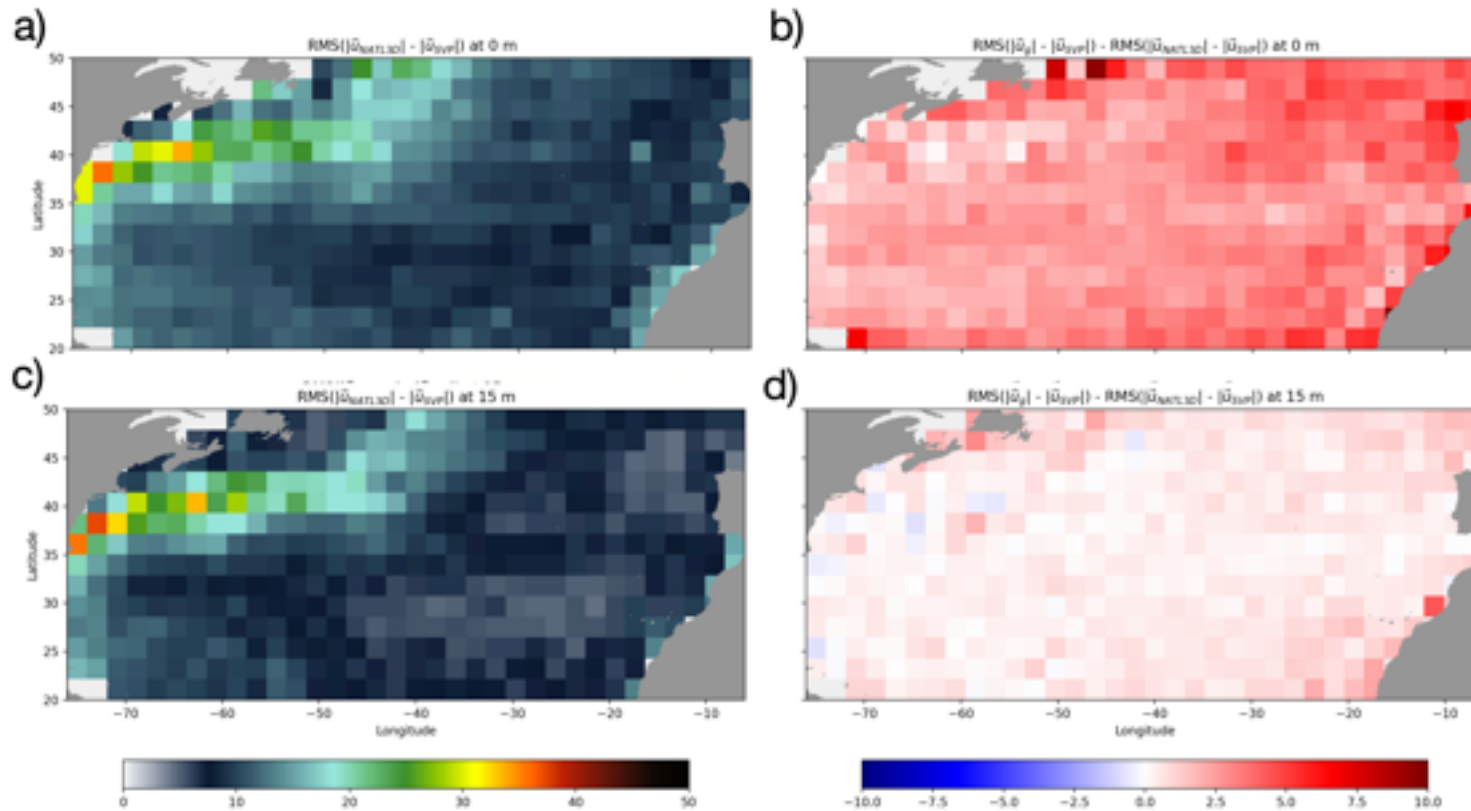


Total horizontal and geostrophic components have been compared with independent estimates of the ocean currents retrieved from SVP drifting buoys over the **entire timeseries** (2010-2019).

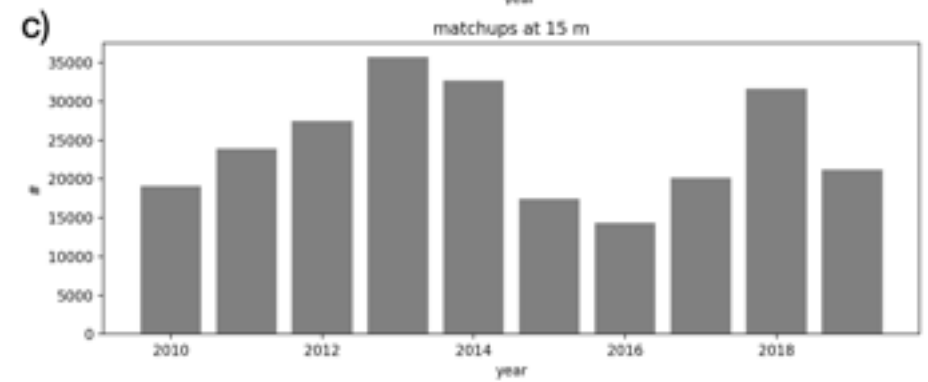
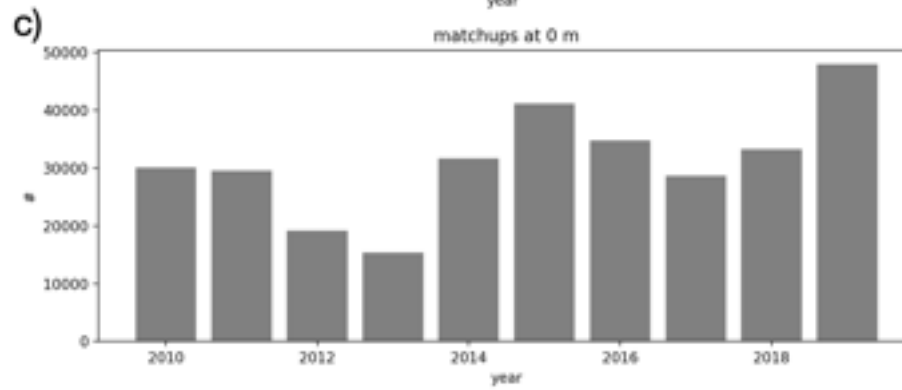
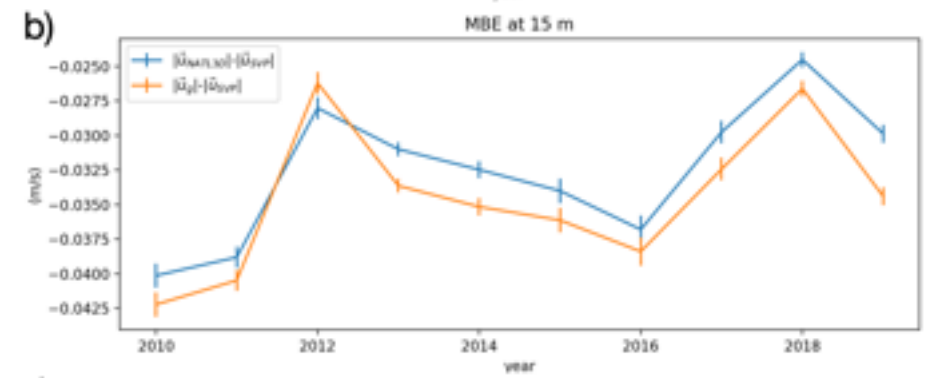
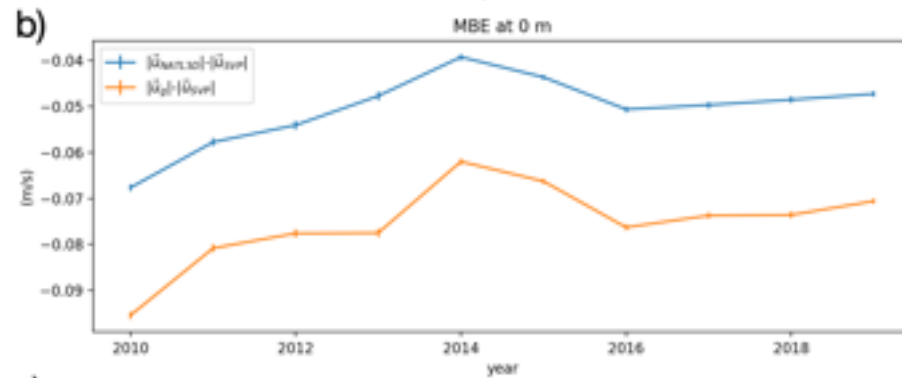
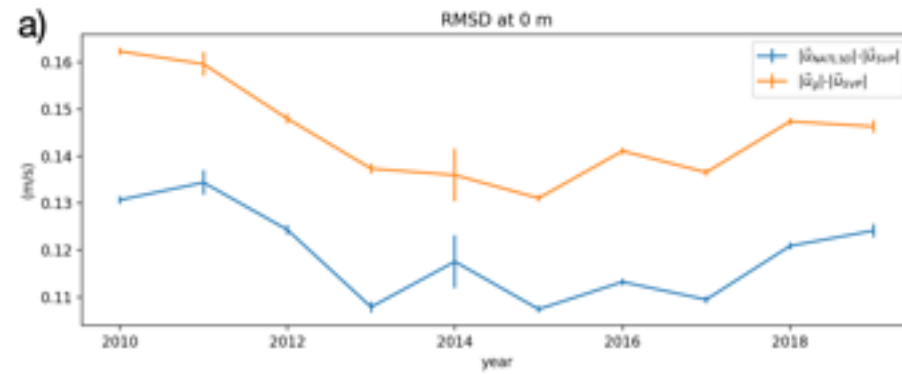
**Total horizontal velocities RMSD:**  $0.119 \pm 0.001$  m/s at 0 m and  $0.113 \pm 0.001$  m/s at 15 m

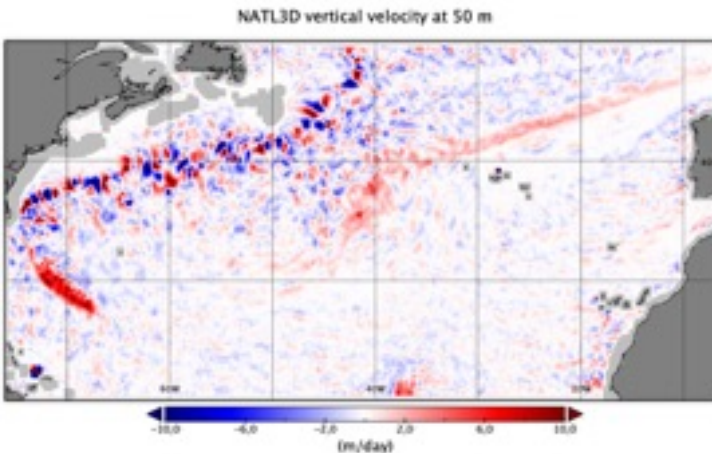
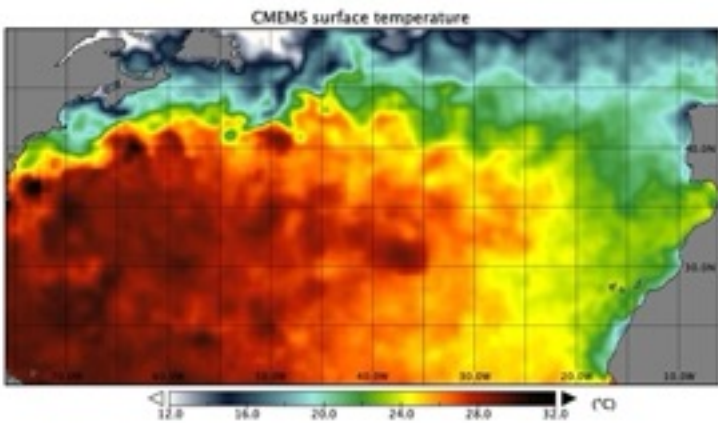
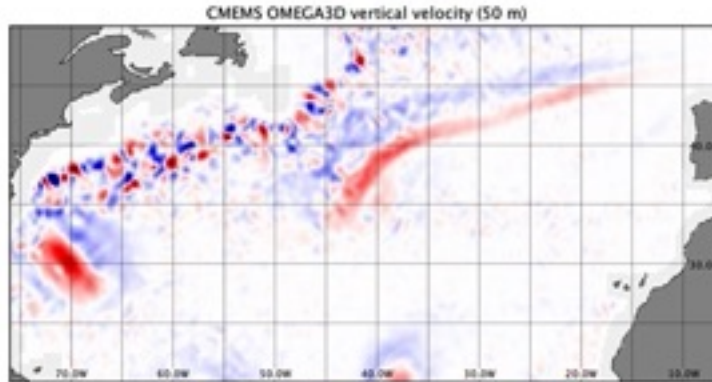
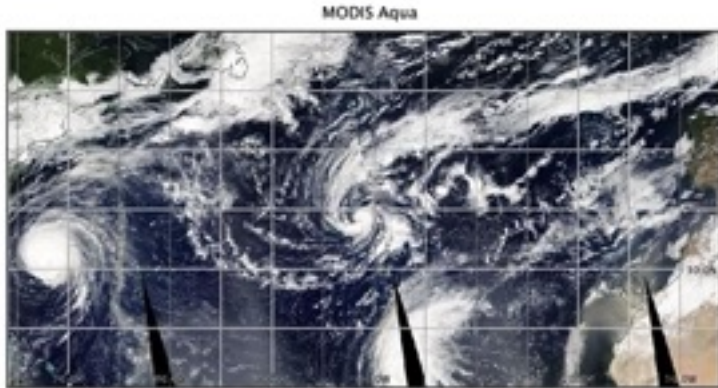
**Geostrophic velocities RMSD:**  $0.145 \pm 0.001$  m/s at 0 m and  $0.117 \pm 0.001$  m/s at 15 m

# matchups used to compute the statistics: 311735 for undrogued SVP velocities (at 0) m and 243742 for drogued SVP data (at 15 m). Confidence intervals are estimated with bootstrapping ( $1 \sigma$ ).



**Yearly validation metrics**  
indicate stable performances  
along the entire timeseries  
(2010-2019)





**CMEMS-OMEGA:**

- mesoscale "permitting" resolution
- inaccurate surface Ekman currents

Weekly  $1/4^\circ \times 1/4^\circ$  (global)  
 3D multilinear regression (CMEMS-ARMOR3D)  
 surface geostrophic currents (AVISO)  
 ERA-interim

**WOC-NATL3D:**

- mesoscale "resolving" resolution
- more accurate surface Ekman currents

Daily,  $1/10^\circ \times 1/10^\circ$  (regional)  
 3D neural network model (WOC-LSTM3D)  
 surface geostrophic currents (WOC-NATL2D)  
 ERA5  
 Empirical Ekman current shear (CMEMS)

**12 September 2018**

MODIS true colour image (top-left), CMEMS OMEGA3D vertical velocities at 50 m depth (top-right),  
 CMEMS SST (bottom-left), WOC\_NATL3D vertical velocities at 50 m depth (bottom-right).  
 Vertical velocities are modulated at different scales by hurricane Florence, visible in the left part of the domain, and by the mesoscale meanders and eddies along the Gulf Stream

