

# Multi-baseline Polarimetric SAR Interferometry: Forest Applications.

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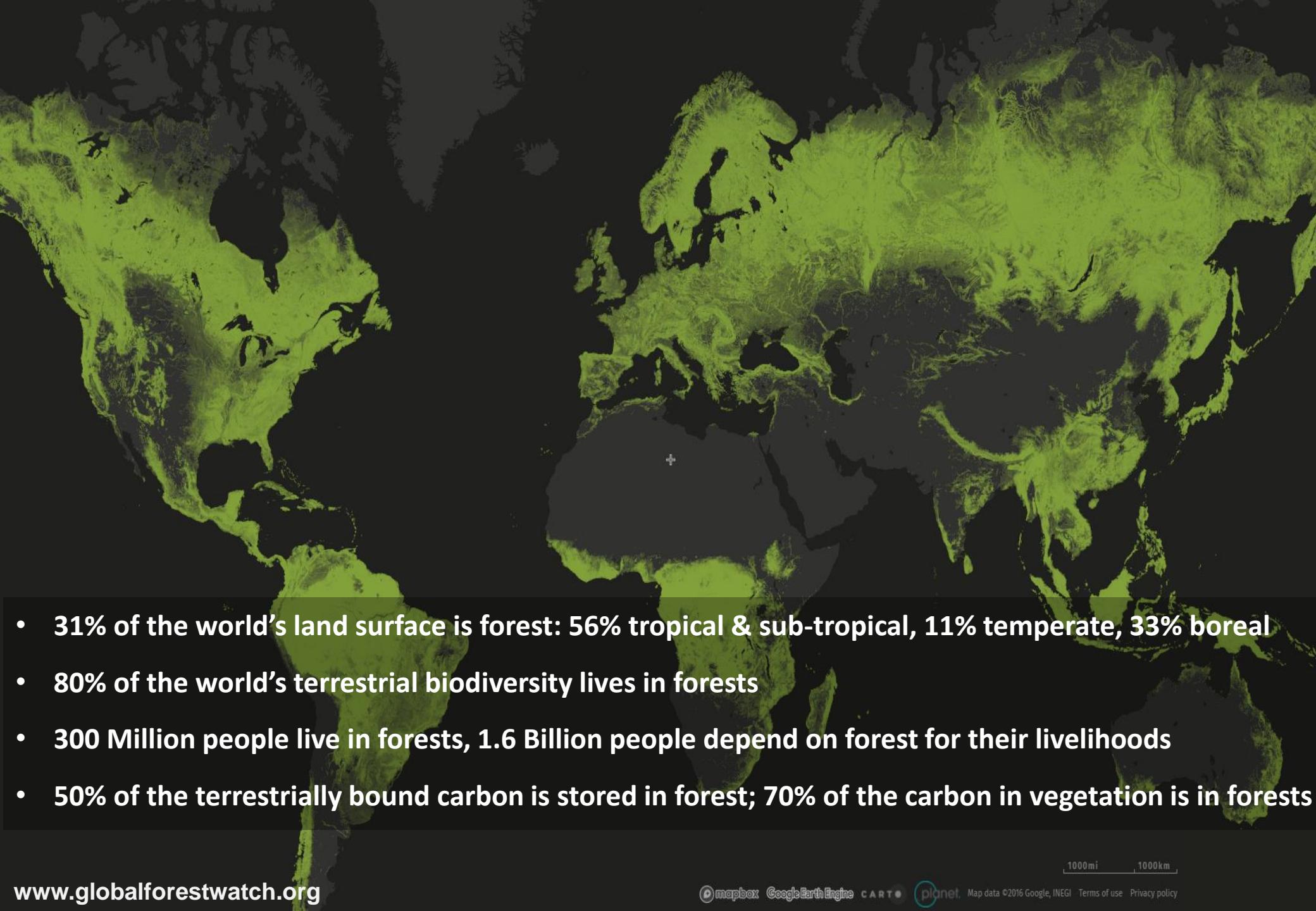
Web: <http://www.eo.ifu.ethz.ch/>

German Aerospace Center

Microwaves and Radar Institute

Department: Radar Concepts

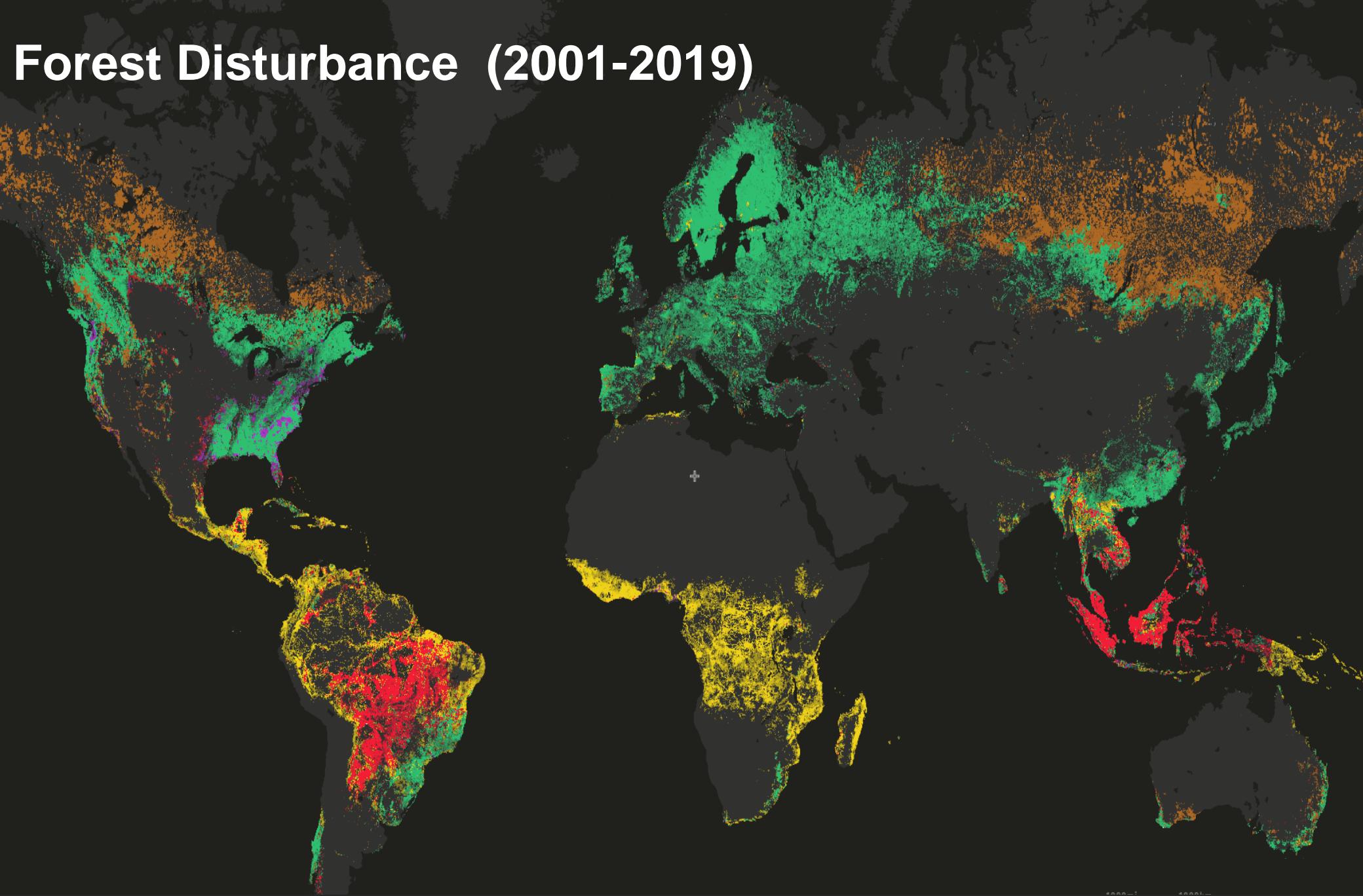
Research Group: Pol-InSAR



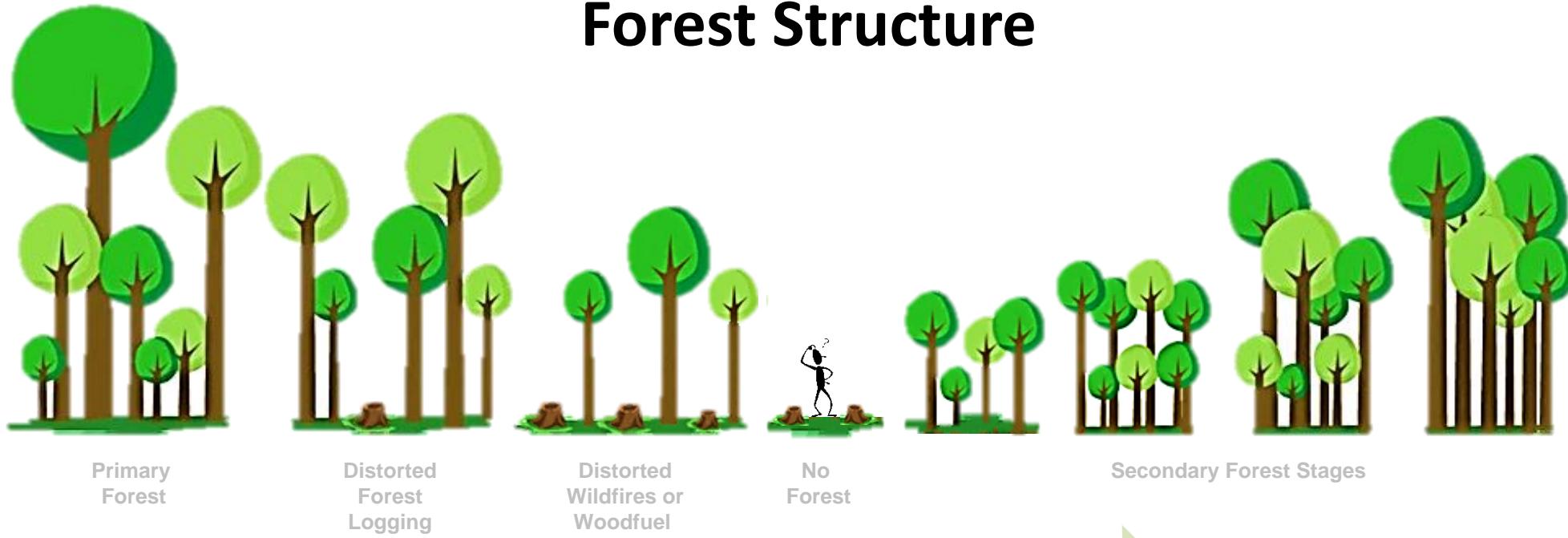
- **31% of the world's land surface is forest: 56% tropical & sub-tropical, 11% temperate, 33% boreal**
- **80% of the world's terrestrial biodiversity lives in forests**
- **300 Million people live in forests, 1.6 Billion people depend on forest for their livelihoods**
- **50% of the terrestrially bound carbon is stored in forest; 70% of the carbon in vegetation is in forests**

1000 mi 1000 km

# Forest Disturbance (2001-2019)



# Forest Structure



**Structural Degradation**

**Degraded forests:** forests which have been harvested beyond the natural growth capacity.

**Secondary Forests:** forests regenerating through a natural succession process after significant and/or total disturbance of the original forest. They show major difference in structure, species composition, and age profile compared to primary forests.

# Climate change can modify role of vegetation

Europe 2003 drought:

**30% decrease of productivity, forest transforms from C-sink 0.3 GtC to C-source: -0.5 GtC**

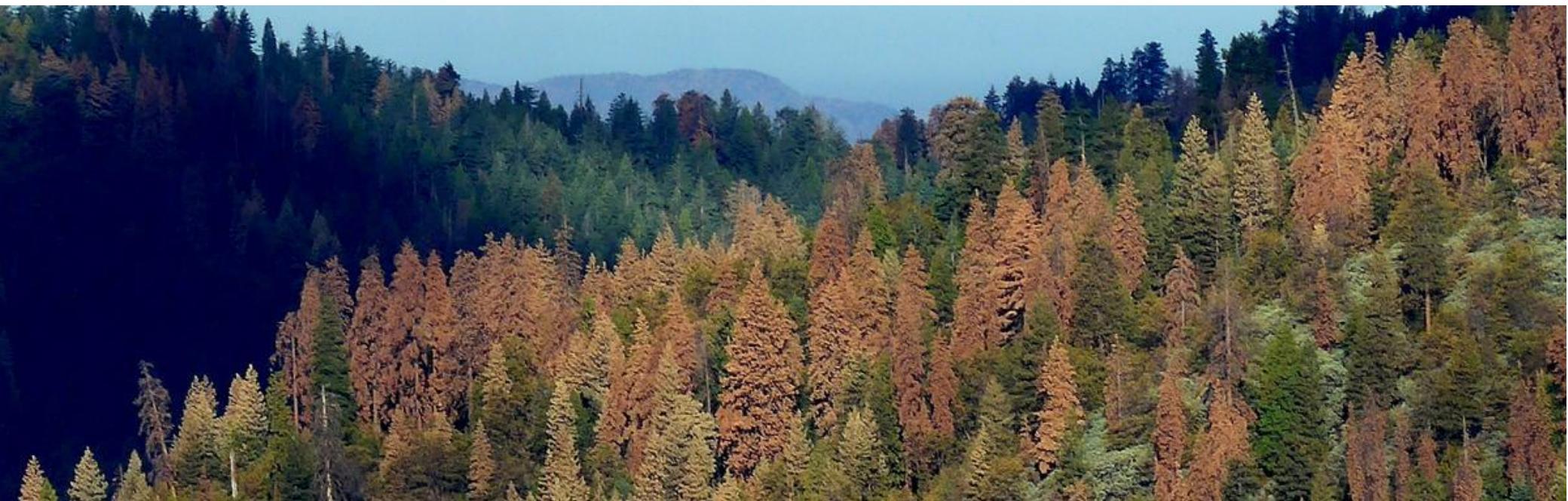
(Cias et al. 2005, Nature)

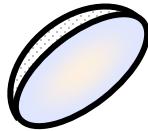
Amazon 2005 and 2010 droughts:

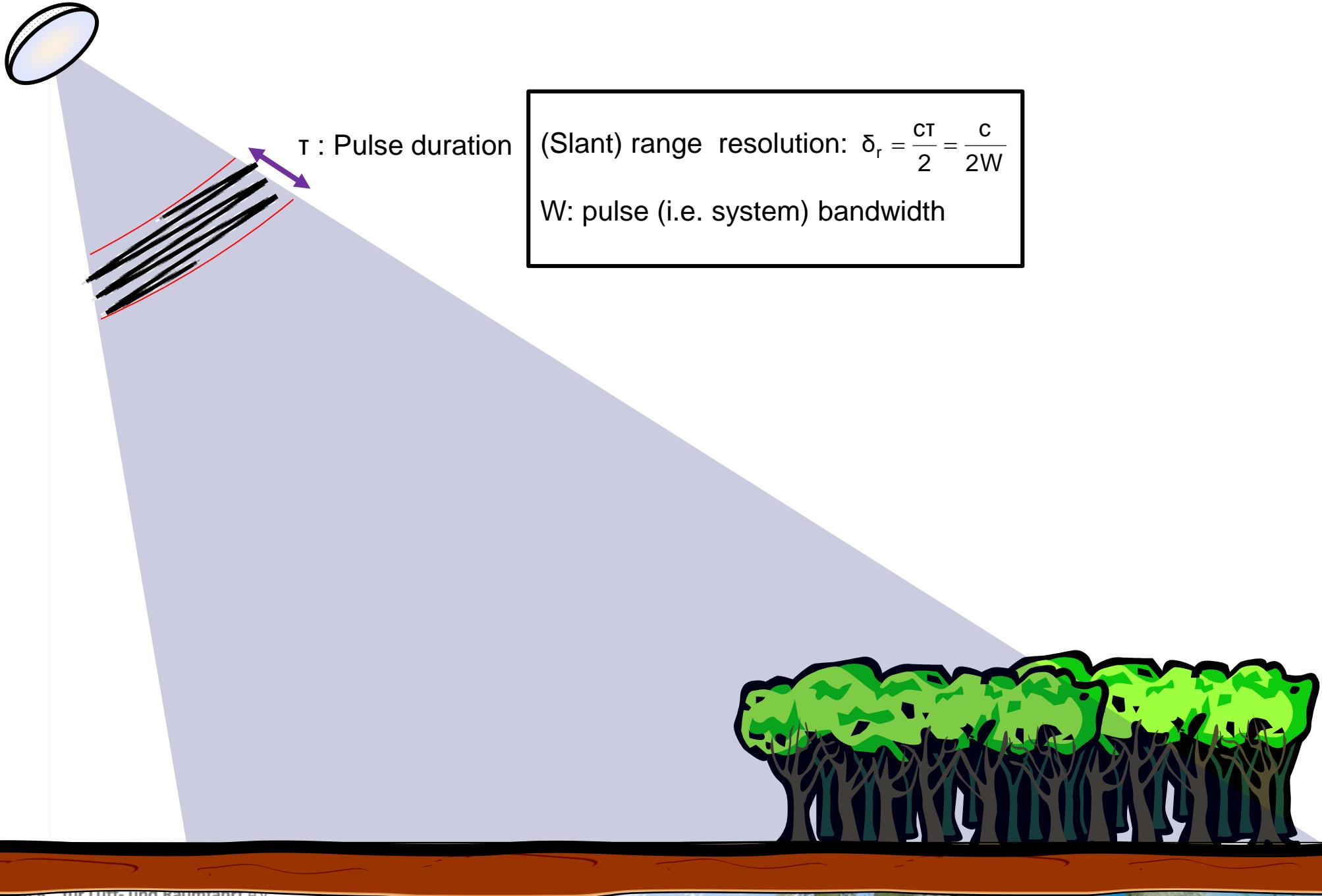
**forests transforms from C-sink 0.5 GtC to C-source -1.2 GtC**

(Phillips et al. 2009, Science, Lewis et al. 2011, Nature)

Does vegetation act as a carbon sink also in the future ?

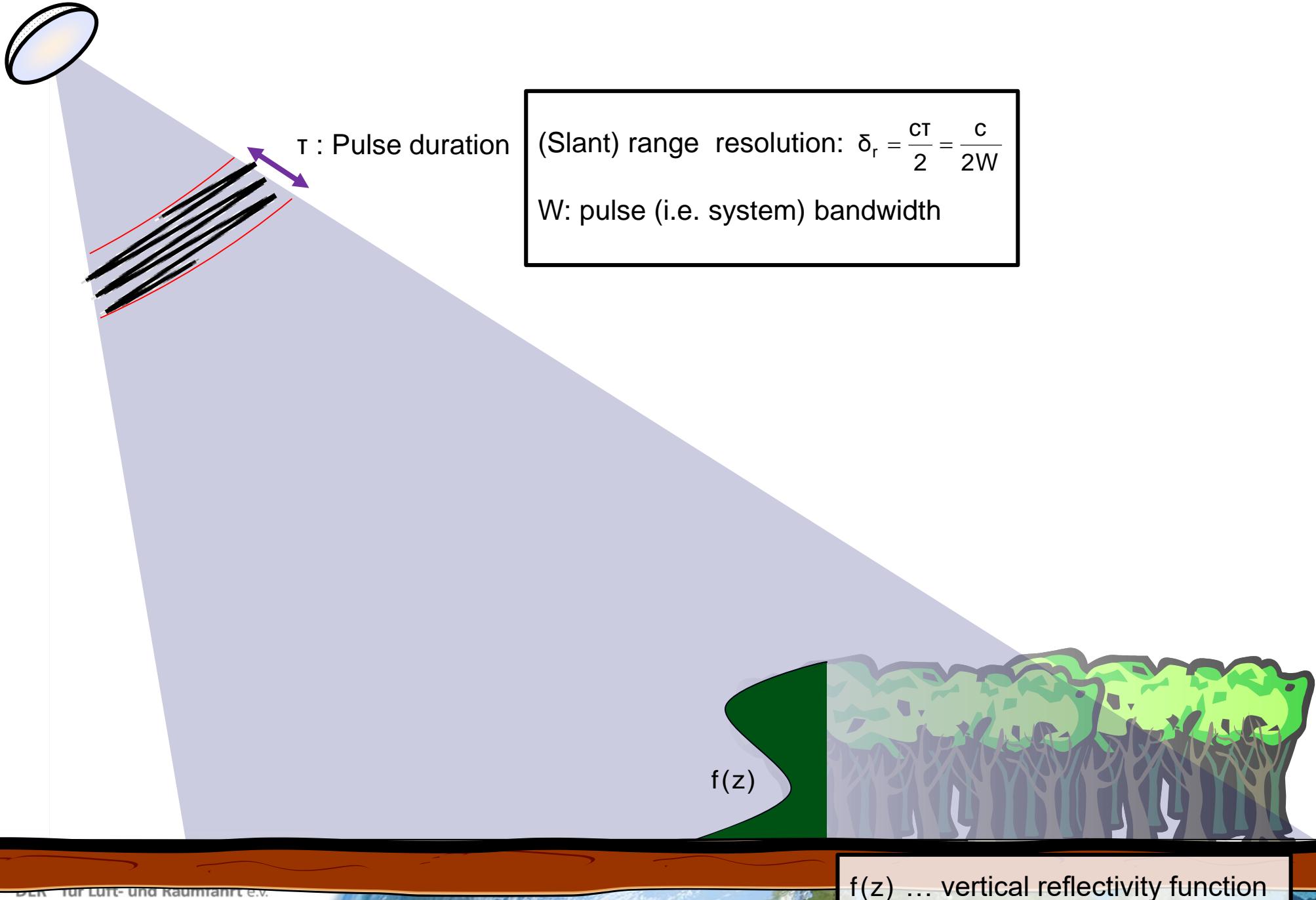


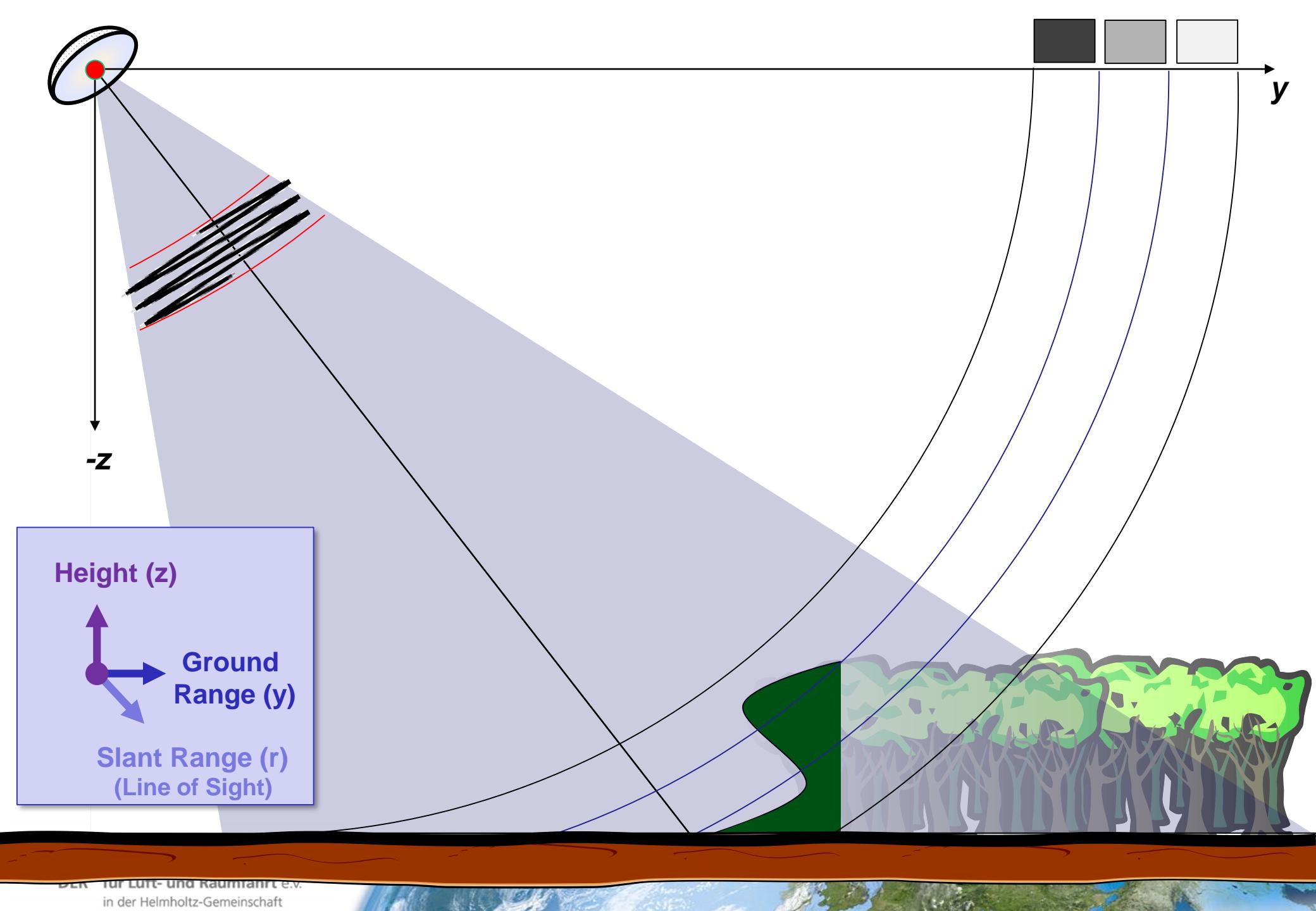




$$(\text{Slant}) \text{ range resolution: } \delta_r = \frac{c\tau}{2} = \frac{c}{2W}$$

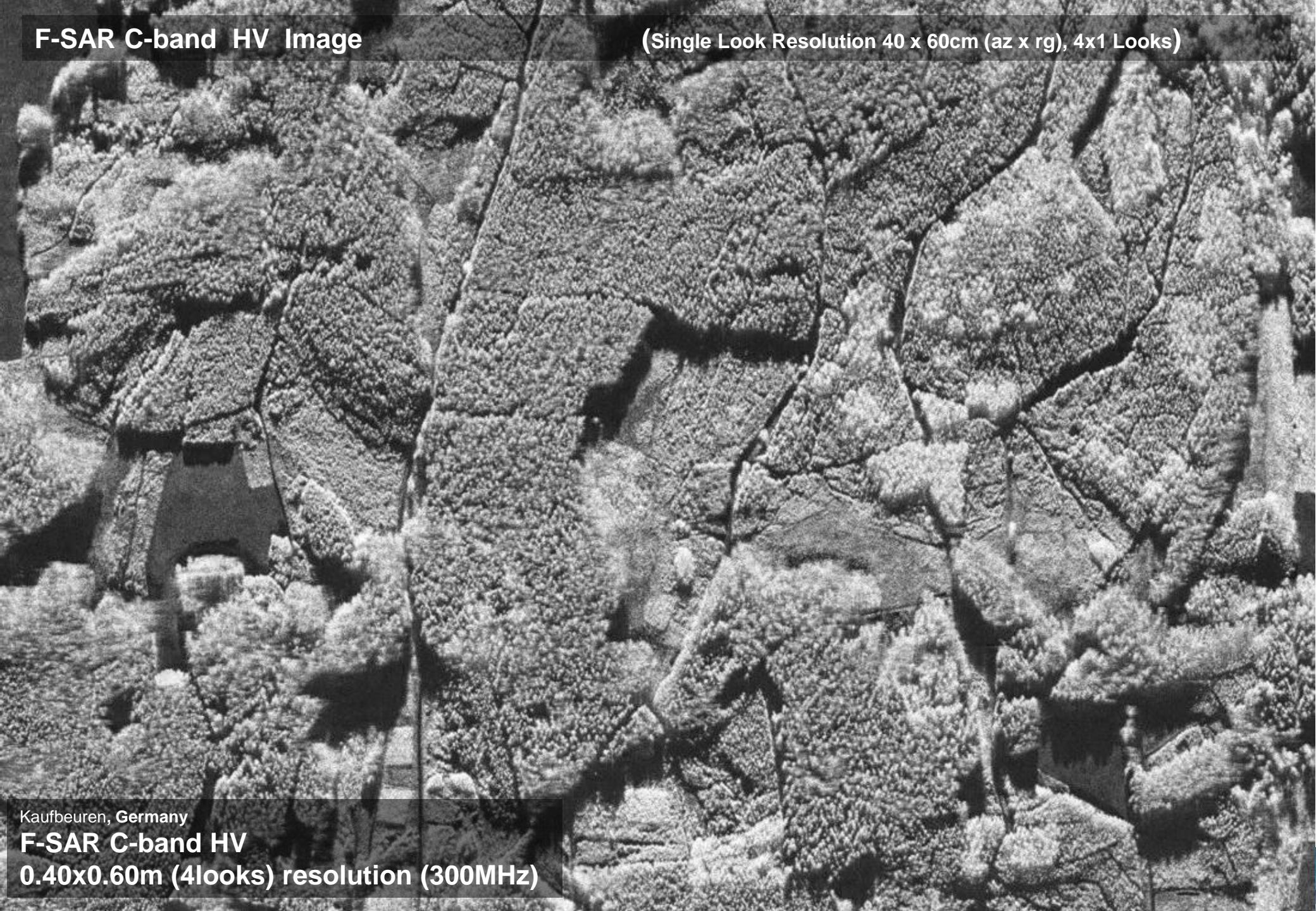
W: pulse (i.e. system) bandwidth





# F-SAR C-band HV Image

(Single Look Resolution 40 x 60cm (az x rg), 4x1 Looks)



Kaufbeuren, Germany

**F-SAR C-band HV**

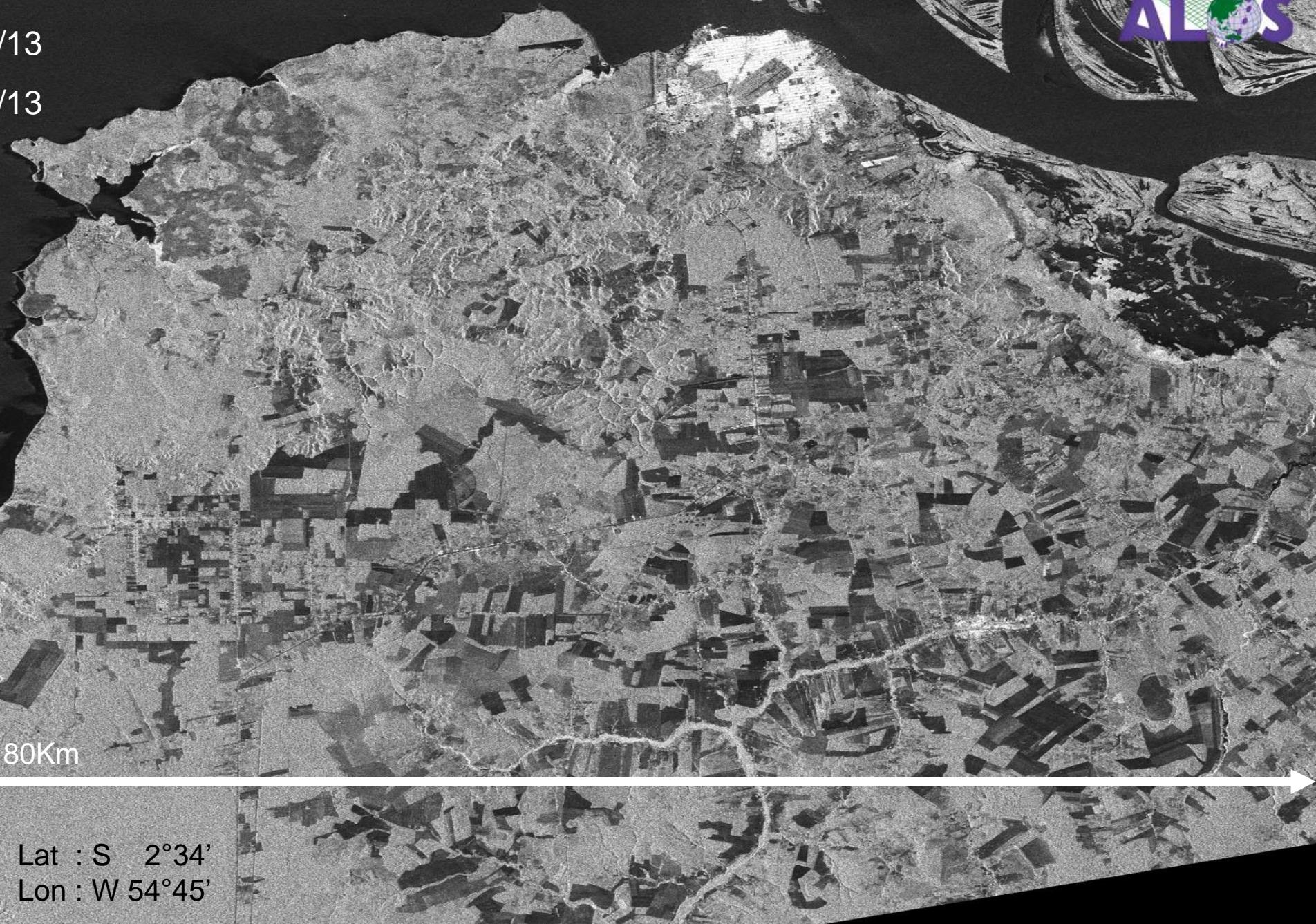
**0.40x0.60m (4looks) resolution (300MHz)**

# Amazon Deforest Watch (Santarem) ALOS Palsar



2007/6/13

2007/9/13

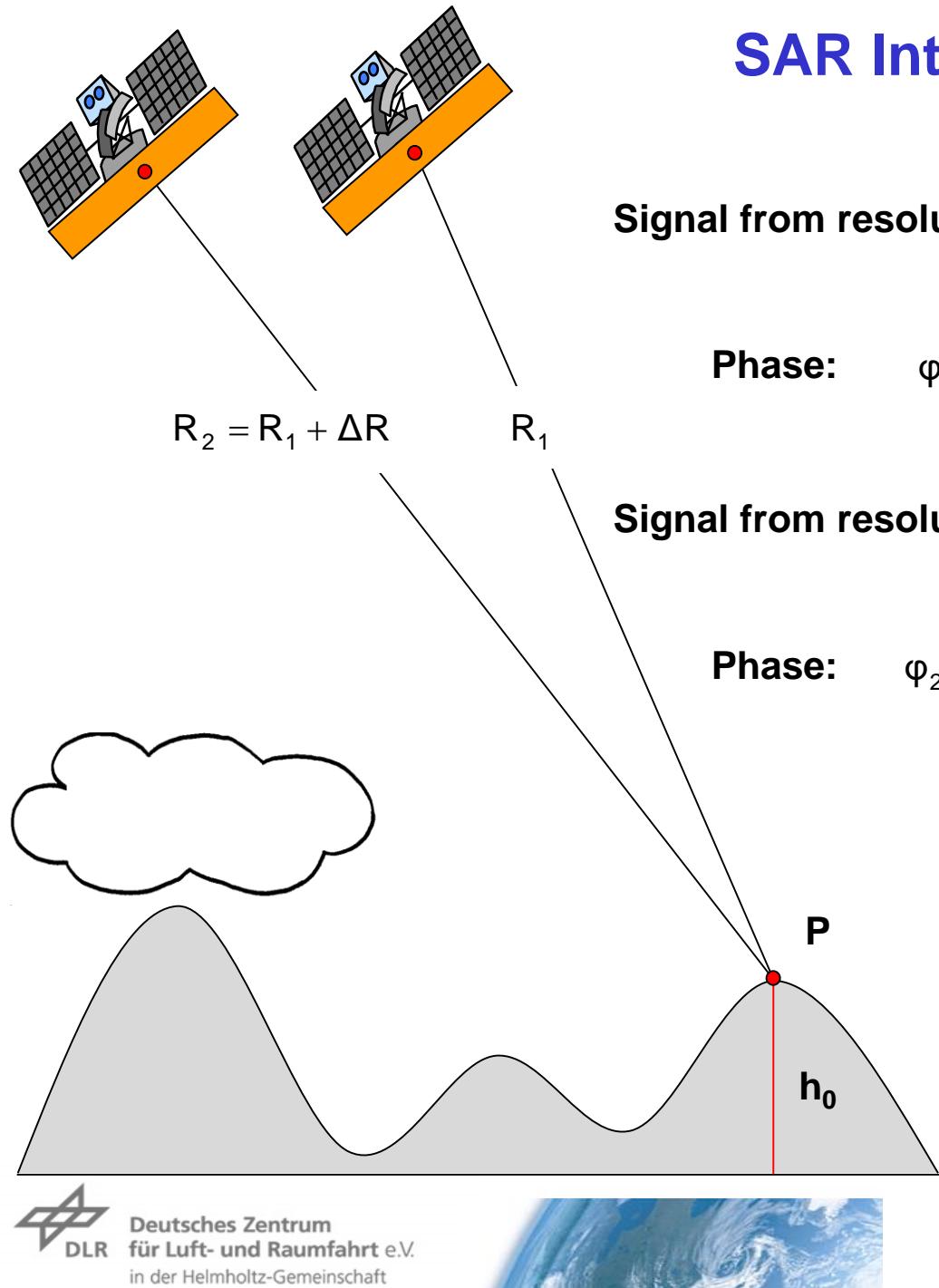


80Km

Lat : S 2°34'

Lon : W 54°45'

# SAR Interferometry



**Signal from resolution cell P in Image 1**  $i_1 = |i_1| \exp[-i(2\frac{2\pi}{\lambda}R_1) + \varphi_{s1}]$

**Phase:**  $\varphi_1 = \arg(i_1) = (2\frac{2\pi}{\lambda}R_1) + \boxed{\varphi_{s1}}$

**Signal from resolution cell P in Image 2**  $i_2 = |i_2| \exp[-i(2\frac{2\pi}{\lambda}R_2) + \varphi_{s2}]$

**Phase:**  $\varphi_2 = \arg(i_2) = (2\frac{2\pi}{\lambda}R_2) + \boxed{\varphi_{s2}}$

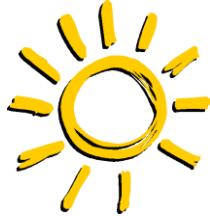


**Assuming**  $\varphi_{s1} = \varphi_{s2}$  !!!

**Interferogram:**  $i_1 i_2^* = |i_1 i_2^*| \exp[-i(2\frac{2\pi}{\lambda}\Delta R)]$

**Phase:**  $\varphi_{int} = \frac{\text{Re}\{i_1 i_2^*\}}{\text{Im}\{i_1 i_2^*\}} = \boxed{2\frac{2\pi}{\lambda}\Delta R}$

**Deterministic !!!**



# Interferometric Coherence

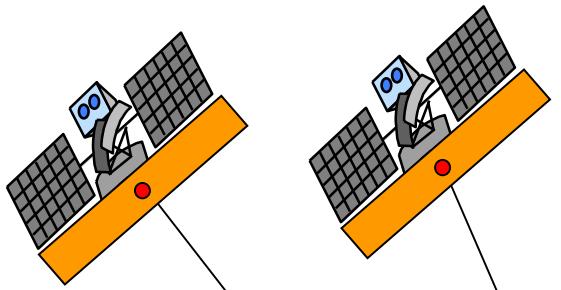


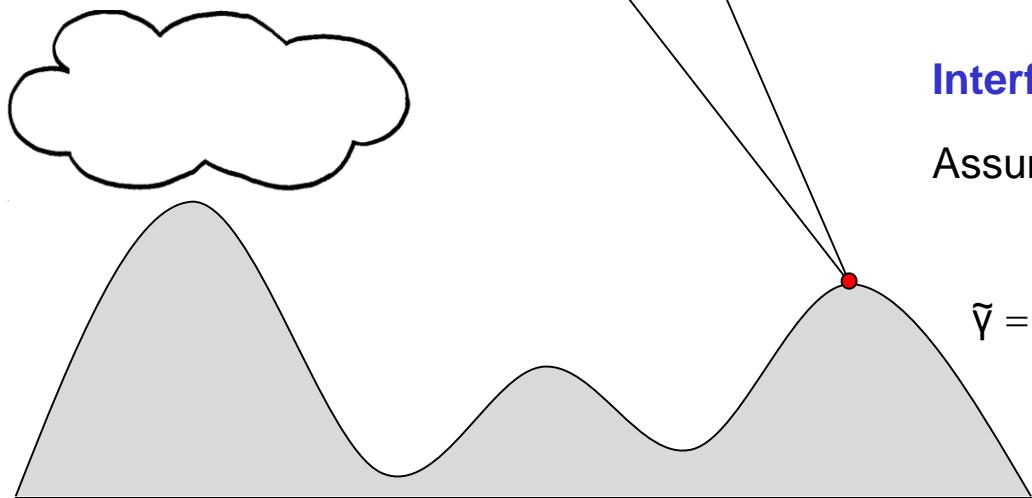
Image 1:  $i_1 = |i_1| \exp[-i(2\frac{2\pi}{\lambda}R_1) + \phi_{s1}]$

Image 2:  $i_2 = |i_2| \exp[-i(2\frac{2\pi}{\lambda}R_2) + \phi_{s2}]$

**Interferometric Coherence:** Normalised Complex Correlation Coefficient

$$\tilde{\gamma} = \frac{E\{ i_1 i_2^* \}}{\sqrt{E\{ i_1 i_1^* \} E\{ i_2 i_2^* \}}} = \frac{|E\{ i_1 i_2^* \}| \exp(i\varphi)}{\sqrt{E\{ |i_1|^2 \} E\{ |i_2|^2 \}}}$$

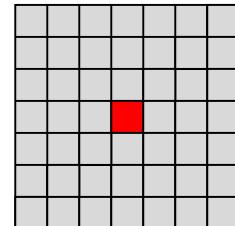
$$0 \leq |\tilde{\gamma}| \leq 1$$



**Interferometric Coherence Estimation:**

Assuming stationarity within the estimation window:

$$\tilde{\gamma} = \frac{\sum_w i_1[i, j] i_2^*[i, j]}{\sqrt{\sum_w |i_1[i, j]|^2 \sum_w |i_2[i, j]|^2}} = \frac{\langle i_1 i_2^* \rangle}{\sqrt{\langle i_1 i_1^* \rangle \langle i_2 i_2^* \rangle}}$$



Typical window size: 10 (3x3) – >100 pixels



Earth Observation and  
Remote Sensing

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Eidgenössische Technische Hochschule Zürich  
Swiss Federal Institute of Technology Zurich

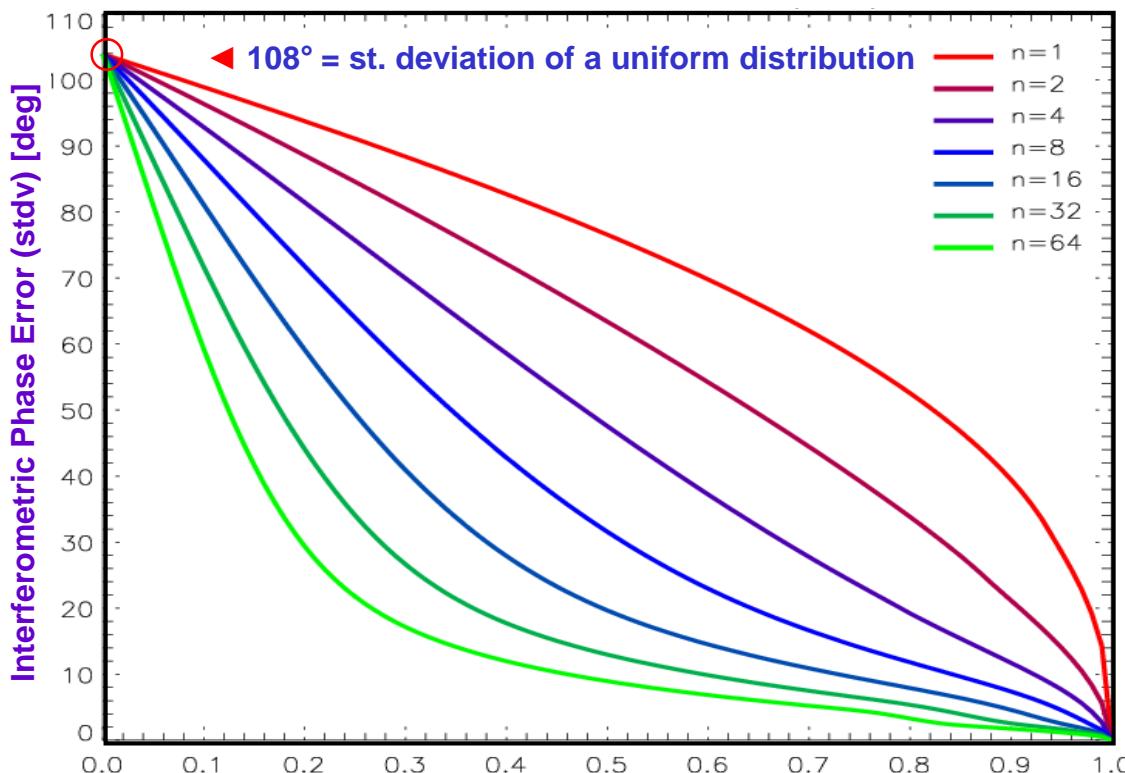
# InSAR Coherence

... is a measure of interferogram quality:

Standard Deviation of the InSAR Phase  $\phi$ :

$$\sigma_\phi = \sqrt{\int_{-\pi}^{\pi} \phi^2 \text{pdf}(\phi) \cdot d\phi}$$

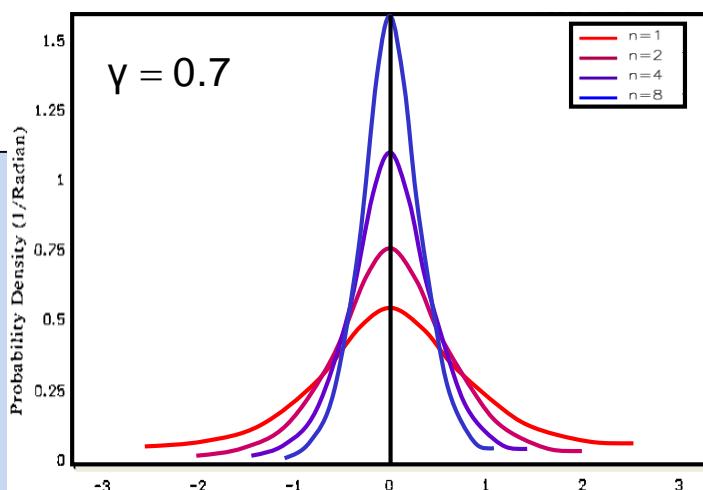
- depends on ▶ the underlying coherence &
- ▶ the number of looks N.



An increase in decorrelation (= loss in coherence) is associated with an increase in the phase variance;  
▶ Increased phase variance leads to increased height errors.

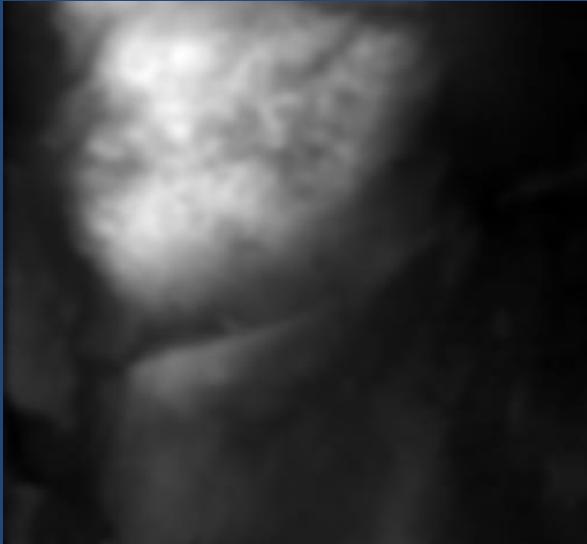
$$\text{where: } \text{pdf}(\phi, N) = \frac{\Gamma(N + 1/2)(1 - |\gamma|^2)^2 \beta}{2\sqrt{\pi} \Gamma(N) (1 - \beta^2)^{N+1/2}} + \frac{(1 - |\gamma|^2)^N}{2\pi} F(N, 1; 1/2; \beta^2)$$

- ▶ F is a Gauss hypergeometric function and  $\beta = |\gamma| \cos(\phi - \bar{\phi})$
- ▶ N is the number of Looks

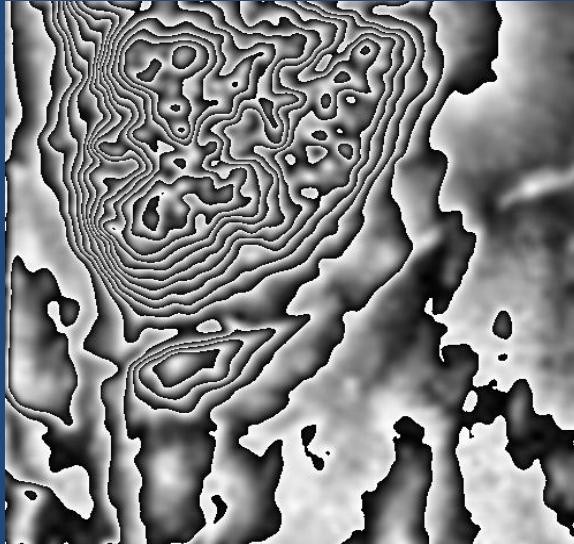


# Interferometric Phase Images

Simulation

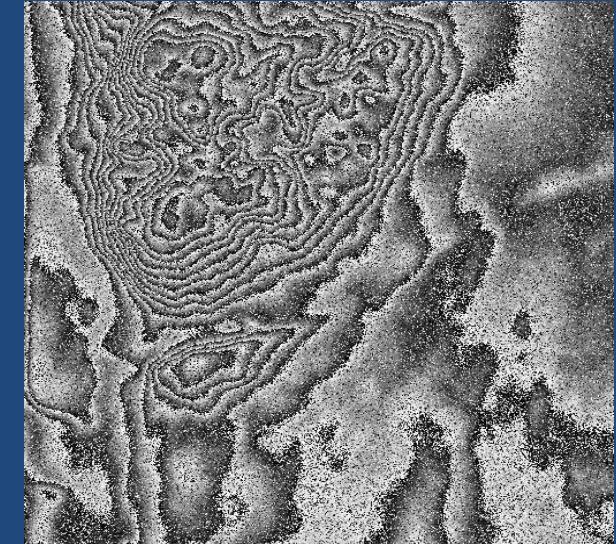


Absolute Phase



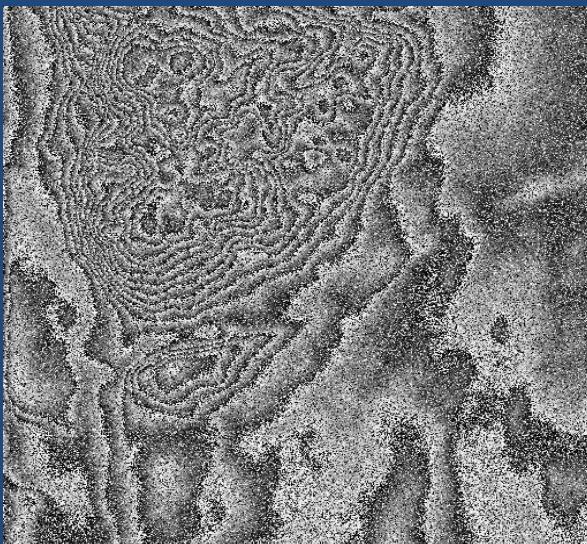
Coherence=1.0

Looks=1



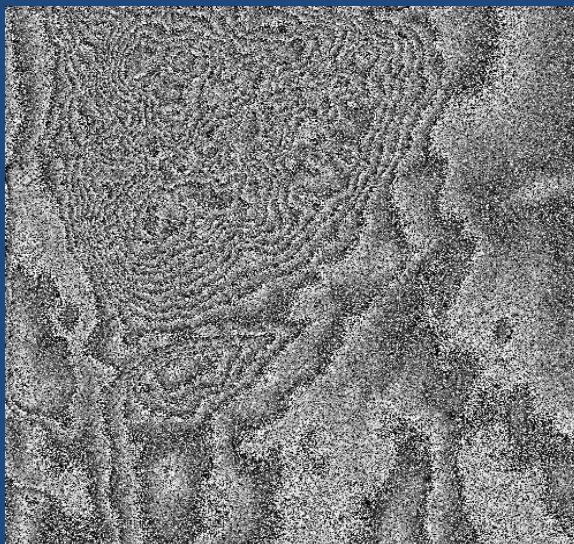
Coherence=0.8

Looks=1



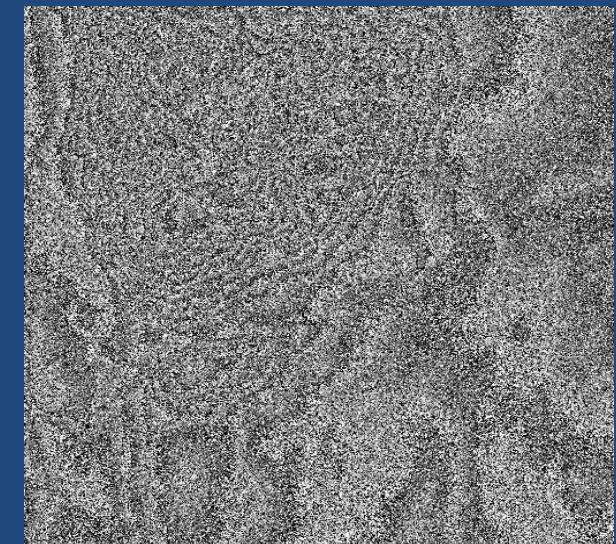
Coherence=0.6

Looks=1



Coherence=0.4

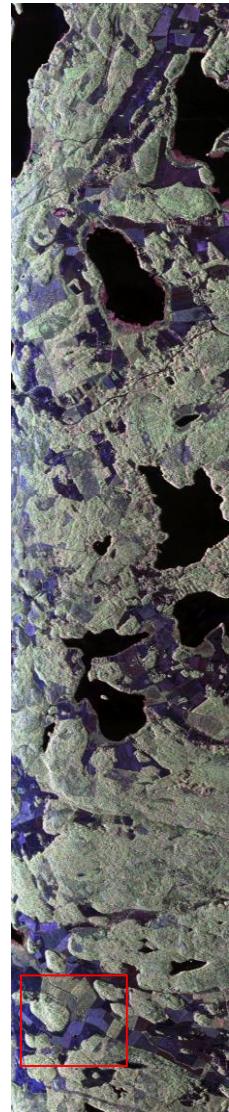
Looks=1



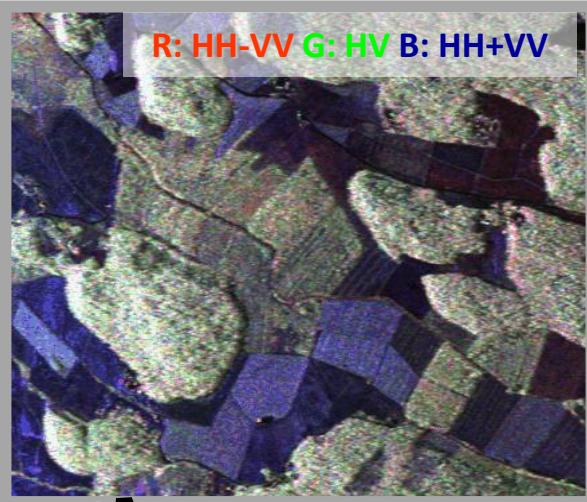
Coherence=0.2

Looks=1

# Why is Interferometry important for Volume Scatterers?



E-SAR / Test Site: Helsinki, Finland



R: HH-VV G: HV B: HH+VV



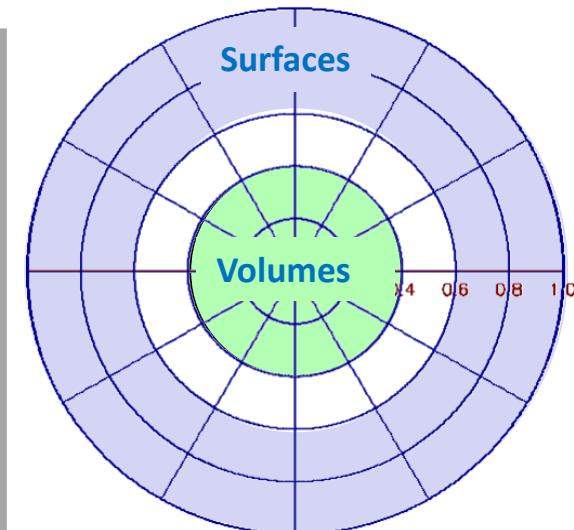
HH-HH Coherence



HH-VV Coherence



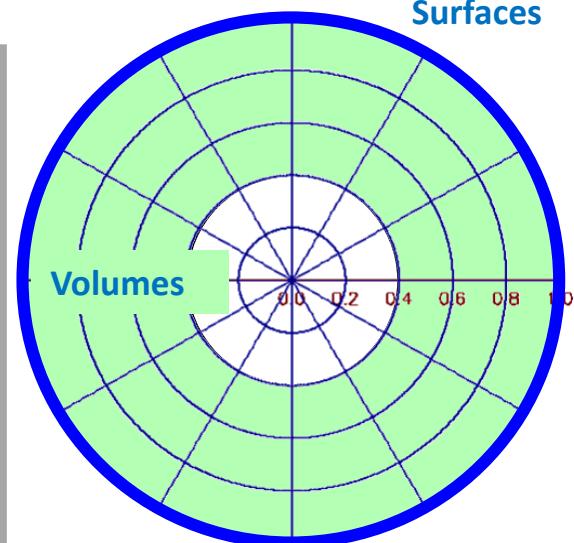
HH-HH Coherence



Surfaces

Volumes

Surfaces



Volumes

Surfaces



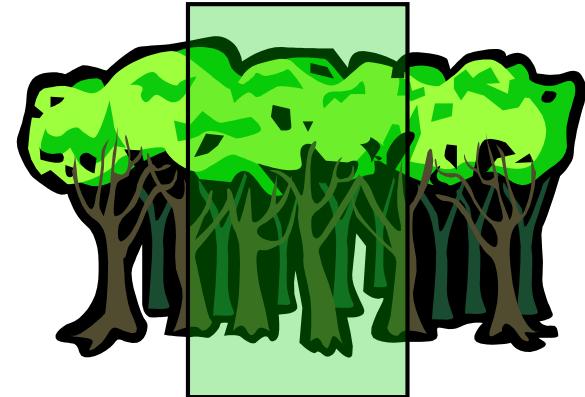
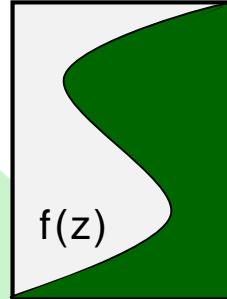
Interferometric  
Coherence

$$\tilde{\gamma}(S_1, S_2) = \frac{< S_1 S_2^* >}{\sqrt{< S_1 S_1^* > < S_2 S_2^* >}}$$

## SAR Interferometry for Volume Structure

Volume  
Coherence

$$\tilde{\gamma}_{Vol}(f(z), k_z) = e^{ik_z z_o} \frac{\int_0^{h_v} f(z) e^{ik_z z} dz}{\int_0^{h_v} f(z) dz}$$



$f(z)$  ... vertical reflectivity function

$$\tilde{\gamma} = \tilde{\gamma}_{Temporal} \gamma_{SNR} \tilde{\gamma}_{Vol}$$

- $\tilde{\gamma}_{Temporal}$  ... temporal decorrelation
- $\gamma_{SNR}$  ... additive noise decorrelation
- $\tilde{\gamma}_{Volume}$  ... geometric decorrelation

$$\text{Vertical Wavenumber: } k_z = \frac{\kappa \Delta \theta}{\sin(\theta_0)}$$



 $S_1$  $S_2$ 

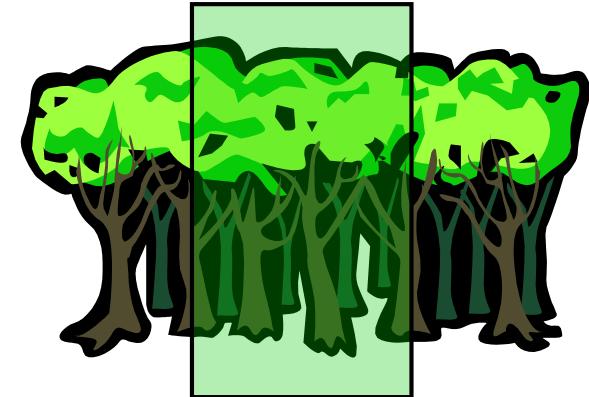
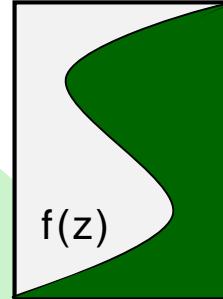
### Interferometric Coherence

$$\tilde{\gamma}(S_1, S_2) = \frac{< S_1 S_2^* >}{\sqrt{< S_1 S_1^* > < S_2 S_2^* >}}$$

## SAR Interferometry for Volume Structure

**Volume Coherence**

$$\tilde{\gamma}_{Vol}(f(z), k_z) = e^{ik_z z_0} \frac{\int_0^{h_v} f(z) e^{ik_z z} dz}{\int_0^{h_v} f(z) dz}$$



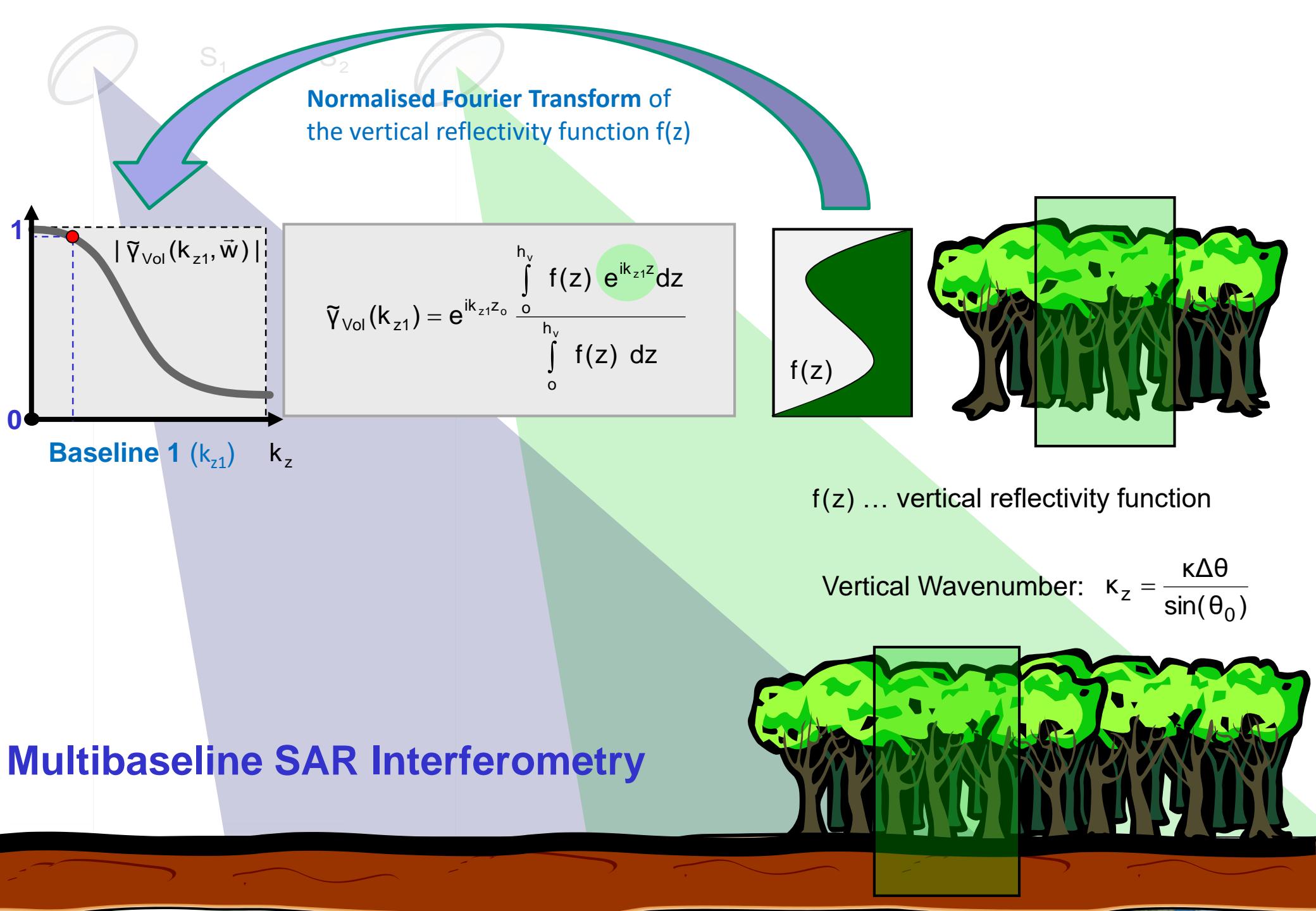
$f(z)$  ... vertical reflectivity function

$$\tilde{\gamma} = \tilde{\gamma}_{Temporal} \gamma_{SNR} \tilde{\gamma}_{Vol}$$

- $\tilde{\gamma}_{Temporal}$  ... temporal decorrelation
- $\gamma_{SNR}$  ... additive noise decorrelation
- $\tilde{\gamma}_{Volume}$  ... geometric decorrelation

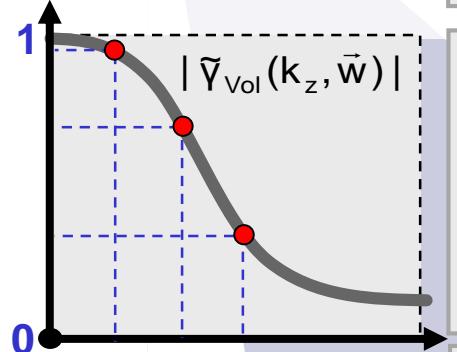
$$\text{Vertical Wavenumber: } k_z = \frac{\kappa \Delta \theta}{\sin(\theta_0)}$$

SAR interferometry allows to reconstruct the vertical reflectivity function  $f(z)$  of a volume scatterer by means of interferometric (volume) coherence measurements at different vertical wavenumbers  $k_z$ , i.e. at different spatial baselines.



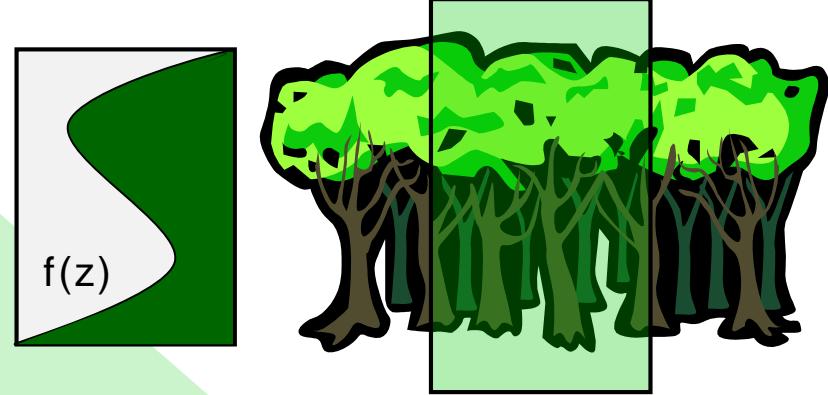
  $S_1$   
**Baseline 3 ( $k_{z3}$ )**

$$\tilde{\gamma}_{\text{Vol}}(k_{z3}) = e^{ik_z z_o} \frac{\int_0^{h_v} f(z) e^{ik_{z3} z} dz}{\int_0^{h_v} f(z) dz}$$



**Baseline 2 ( $k_{z2}$ )**

$$\tilde{\gamma}_{\text{Vol}}(k_{z2}) = e^{ik_z z_o} \frac{\int_0^{h_v} f(z) e^{ik_{z2} z} dz}{\int_0^{h_v} f(z) dz}$$



$f(z)$  ... vertical reflectivity function

Vertical Wavenumber:  $\kappa_z = \frac{\kappa \Delta \theta}{\sin(\theta_0)}$

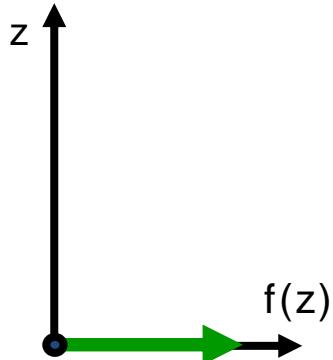


## Multibaseline SAR Interferometry

Multi-baseline measurements allow to sample the spectrum of the vertical reflectivity  $\text{FT}\{f(z)\}$  @ different (spatial) frequencies ( $k_z$ ).

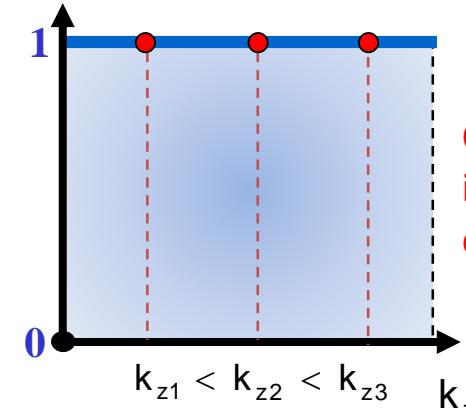
## Vertical Reflectivity Function $f(z)$

Surface Scatterer



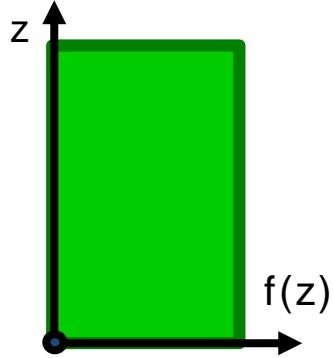
$$|\tilde{\gamma}_{\text{Vol}}(k_z)| = \frac{\left| \int_0^{h_v} f(z) e^{ik_z z} dz \right|}{\int_0^{h_v} f(z) dz}$$

## InSAR Volume Coherence $|\tilde{\gamma}_{\text{Vol}}(k_z)|$

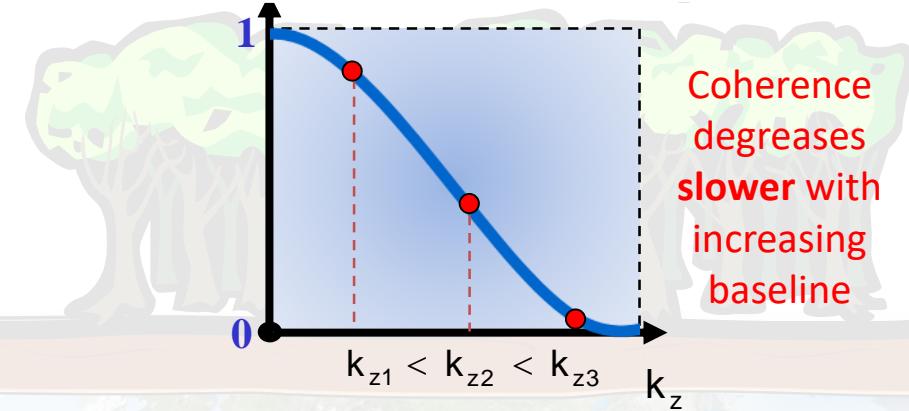
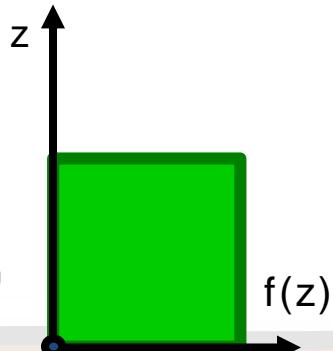


Coherence is independent of baseline

Tall Vegetation



Short Vegetation



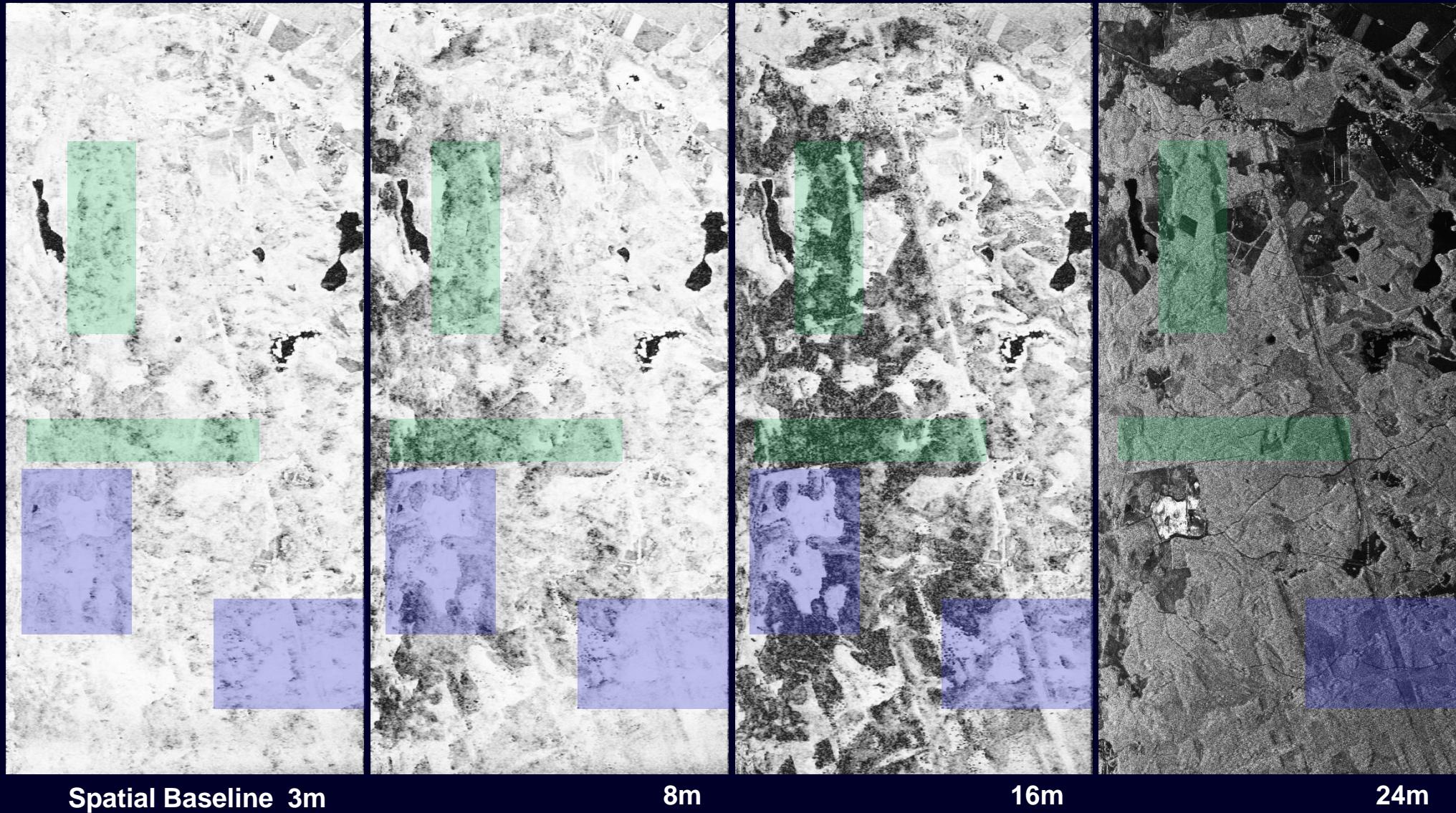
Coherence decreases slower with increasing baseline

# Amplitude Image



Amplitude Image HH

# Interferometric Coherence: Volume Decorrelation

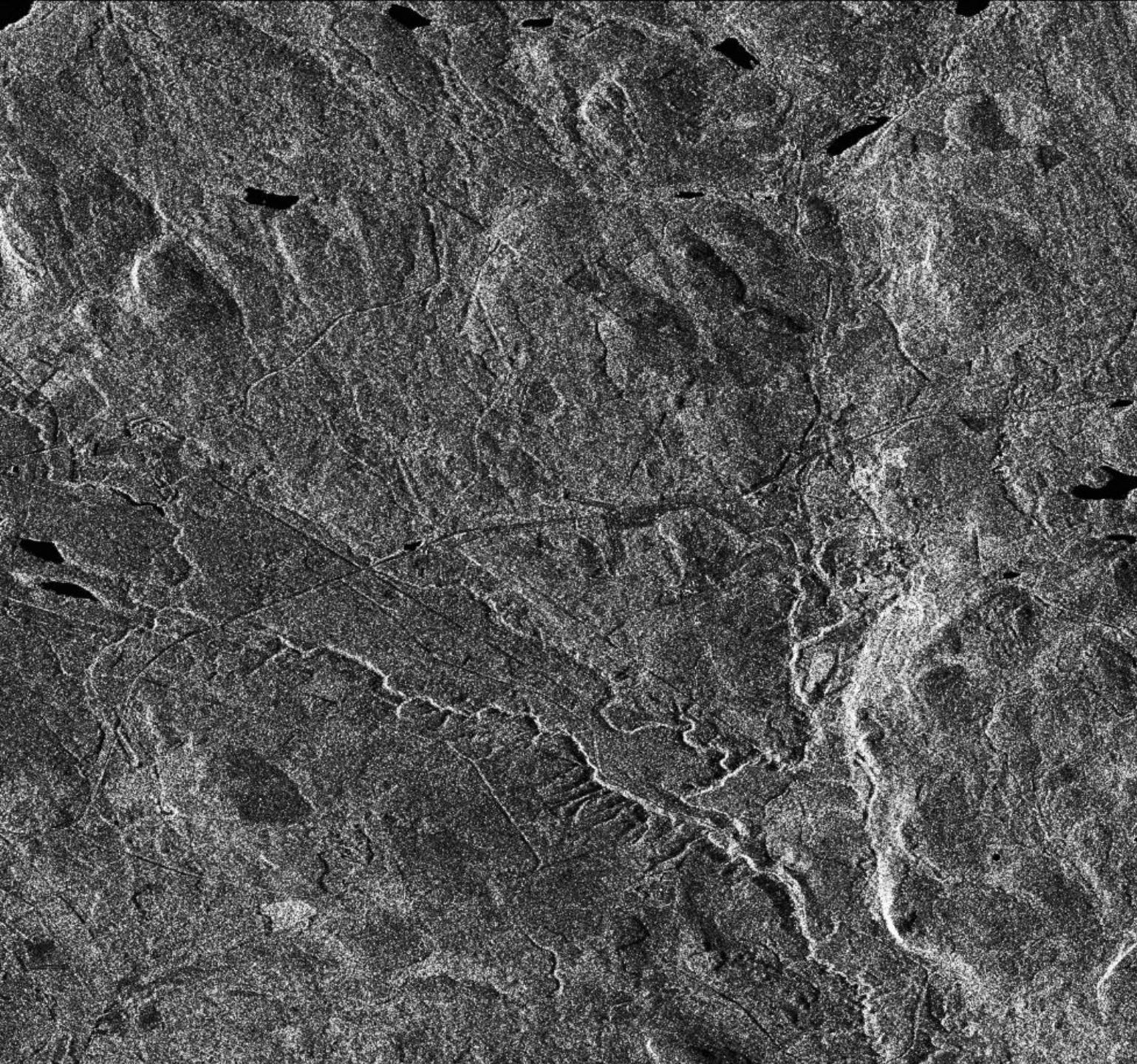


Spatial Baseline 3m

8m

16m

24m

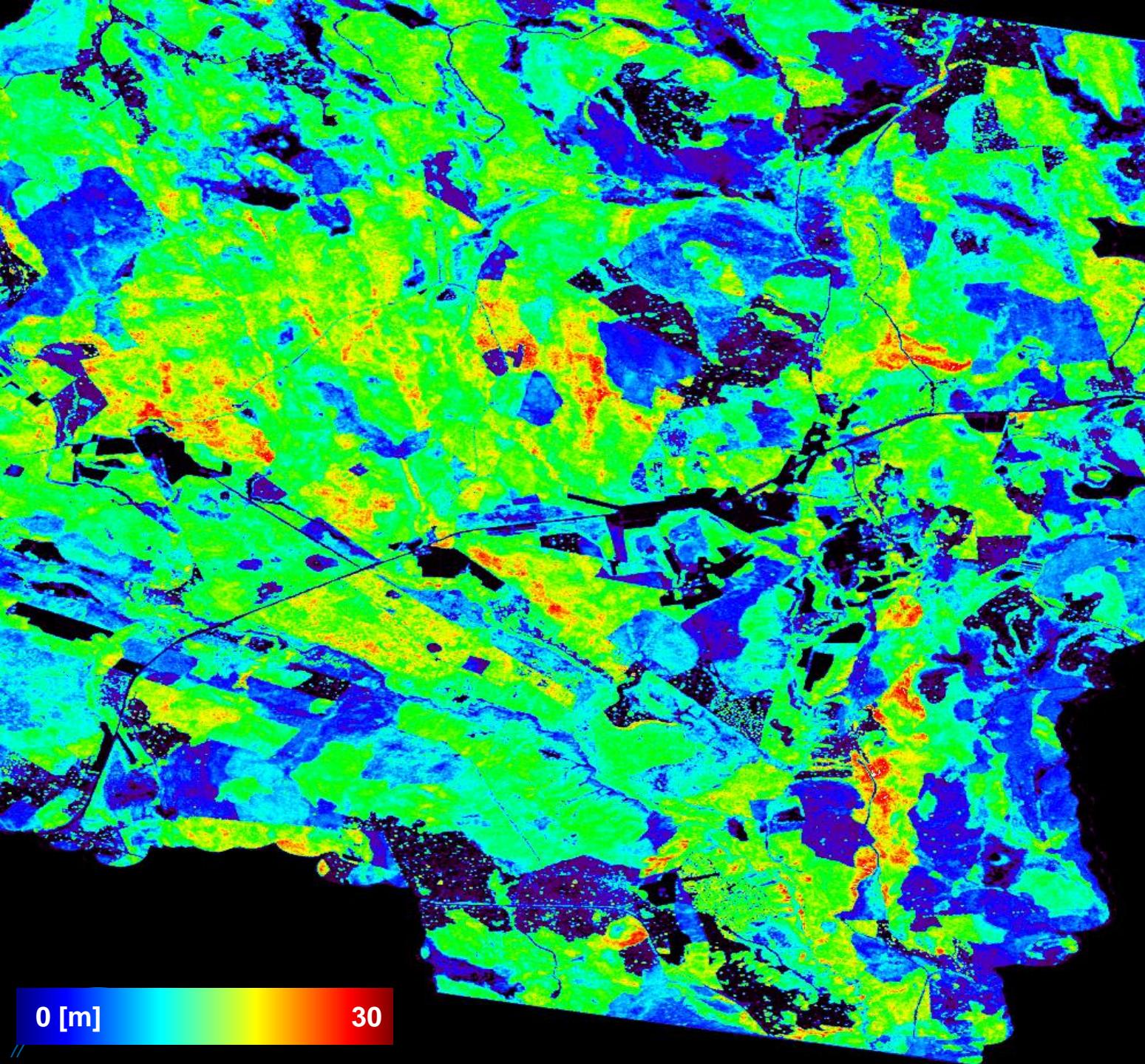
A high-resolution radar backscatter image showing a complex landscape. The terrain is characterized by numerous linear features, likely representing vegetation or soil patterns, set against a dark, textured background. Several large, irregularly shaped dark patches are scattered across the scene, possibly indicating water bodies or dense forest areas.

**Test Site: Krycklan,  
Sweden**

**Radar  
Backscatter**

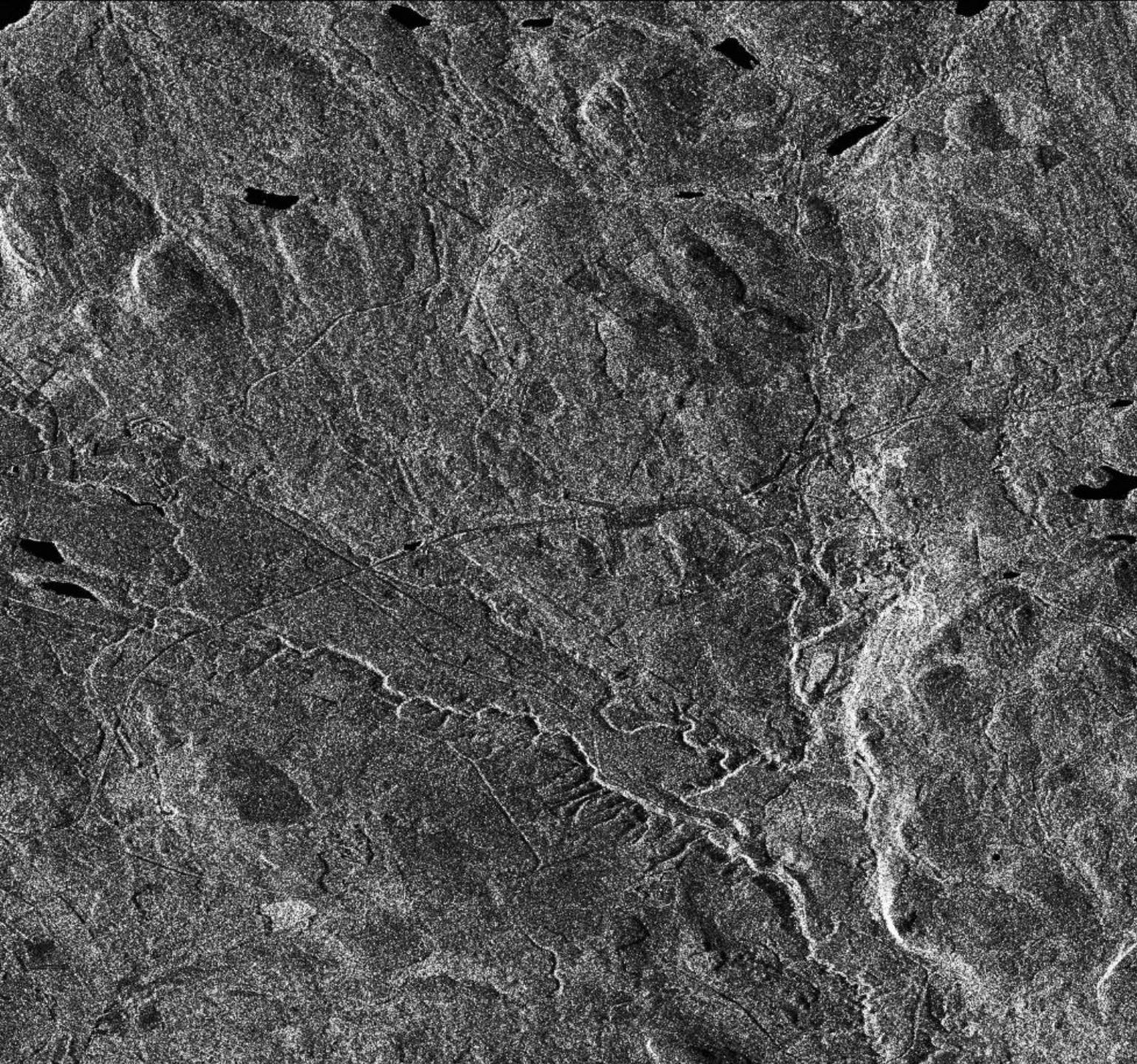
Test Site: Krycklan,  
Sweden

Forest  
Height



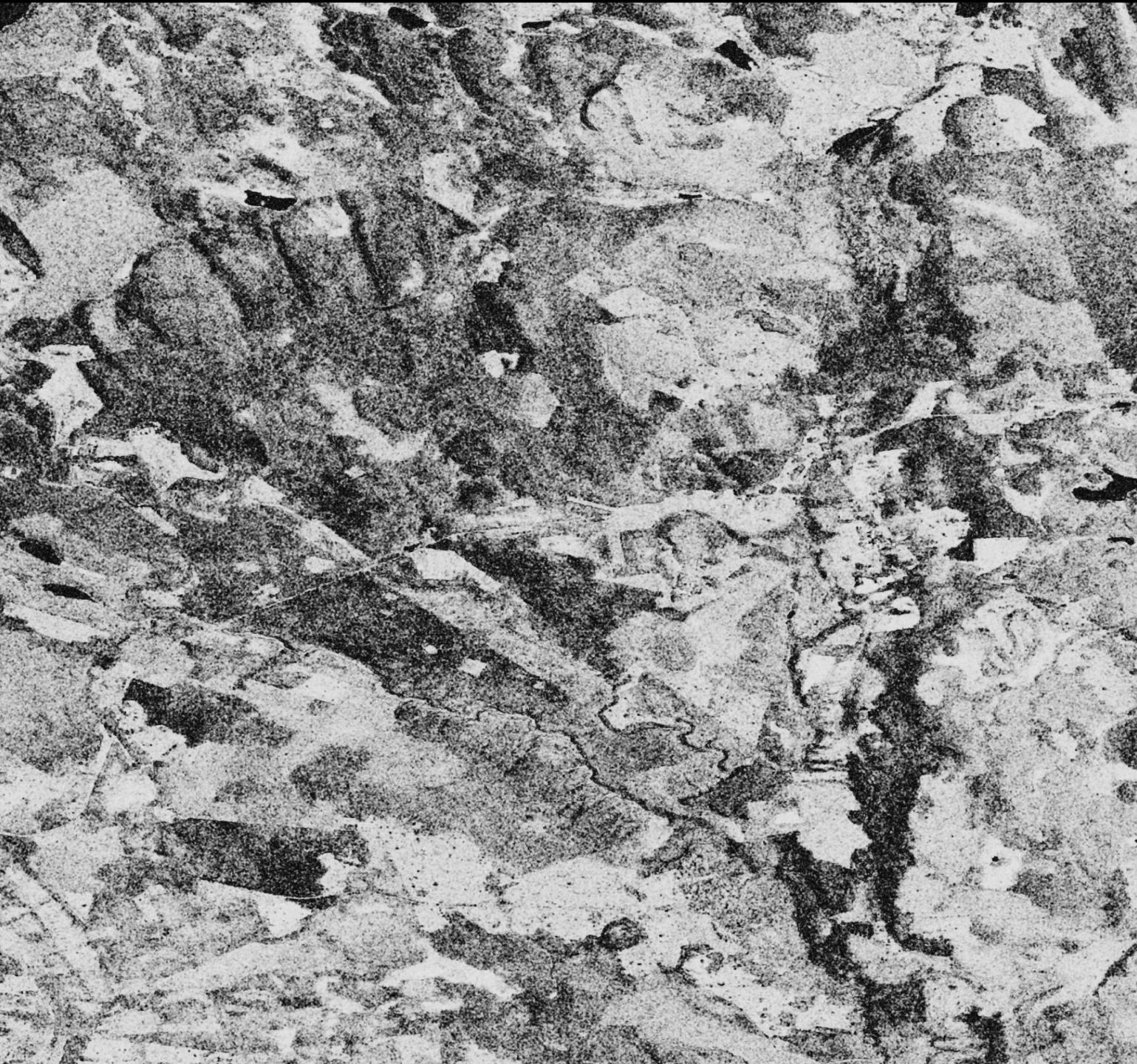
0 [m]

30

A high-resolution radar backscatter image showing a complex landscape. The terrain is characterized by numerous linear features, likely representing vegetation or soil patterns, set against a dark, textured background. Several large, irregularly shaped dark patches are scattered across the scene, possibly indicating water bodies or dense forest areas.

**Test Site: Krycklan,  
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**Radar  
Backscatter**

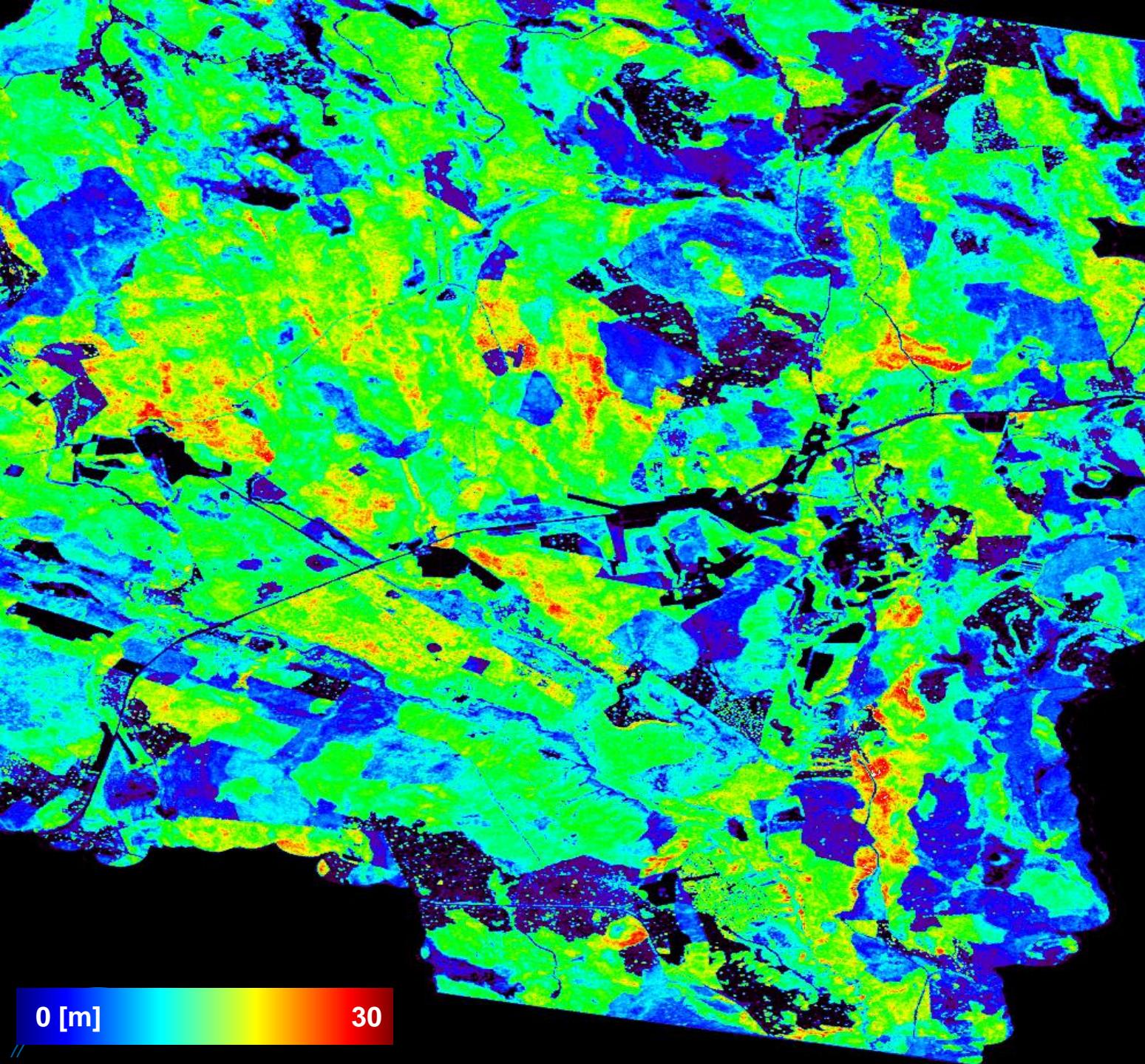


**Test Site: Krycklan,  
Sweden**

**InSAR  
Coherence**

Test Site: Krycklan,  
Sweden

Forest  
Height



0 [m]

30

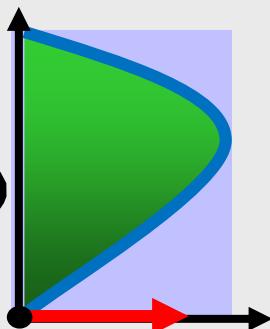
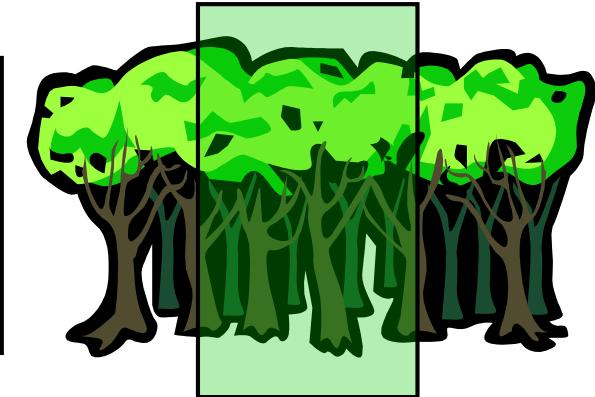
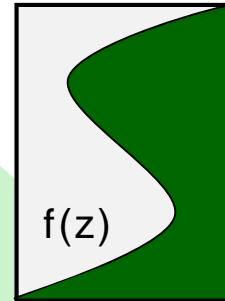


## Interferometric Coherence

$$\tilde{\gamma}(S_1 S_2) = \frac{< S_1 S_2^* >}{\sqrt{< S_1 S_1^* > < S_2 S_2^* >}}$$

Volume Coherence

$$\tilde{\gamma}_{Vol}(f(z)) = e^{ik_z z_o} \frac{\int_0^{h_v} f(z) e^{ik_z z} dz}{\int_0^{h_v} f(z) dz}$$



Volume Layer Ground Layer

$$f(z) = m_V f_V(z) + m_G \delta(z - z_0)$$

## 2 Layer Inversion Model

$$\tilde{\gamma}_{Vol}(\vec{w}) = \exp(i\phi_0) \frac{\tilde{\gamma}_V + m(\vec{w})}{1 + m(\vec{w})}$$

$f_V(z)$  ... volume reflectivity function

Volume Coherence

$$\tilde{\gamma}_V = \frac{I}{I_0} \quad \left\{ \begin{array}{l} I = \int_0^{h_V} \exp(i\kappa_z z') f_V(z') dz' \\ I_0 = \int_0^{h_V} f_V(z') dz' \end{array} \right.$$

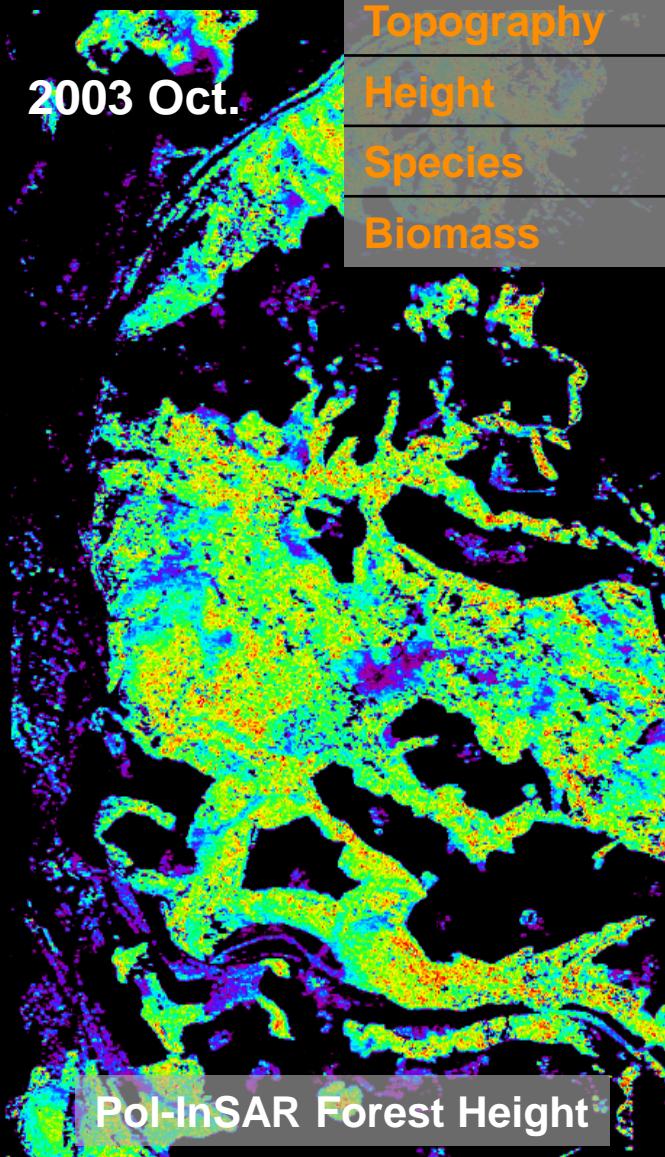
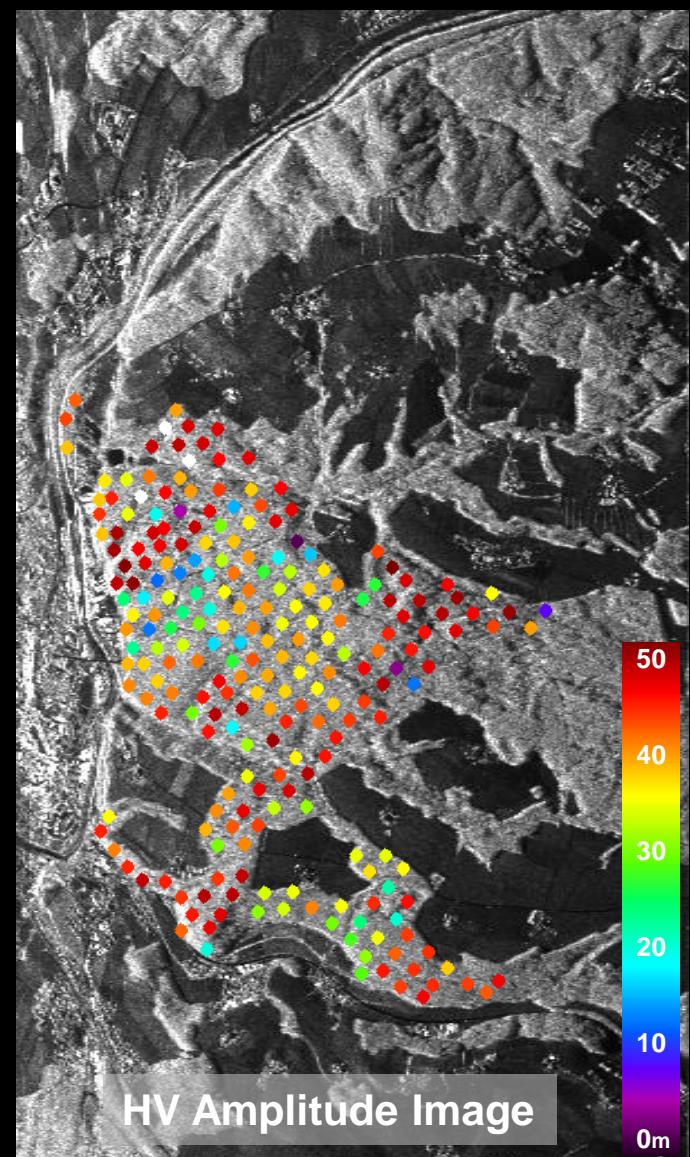
$$m(\vec{w}) = \frac{m_G(\vec{w})}{m_V(\vec{w}) I_0}$$

$$\kappa_z = \frac{\kappa \Delta \theta}{\sin(\theta_0)}$$

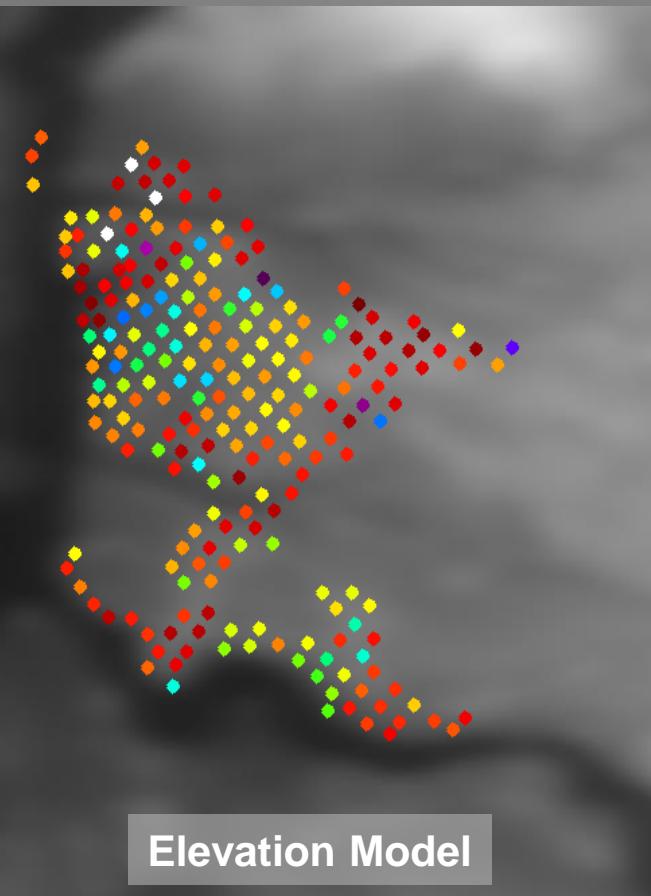
$f_V(z)$  has to be parameterised (N param)  
 Volume Height  $h_V$   
 Topography  $\phi_0$   
 G/V Ratio  $m(\vec{w})$

3+N Unknowns

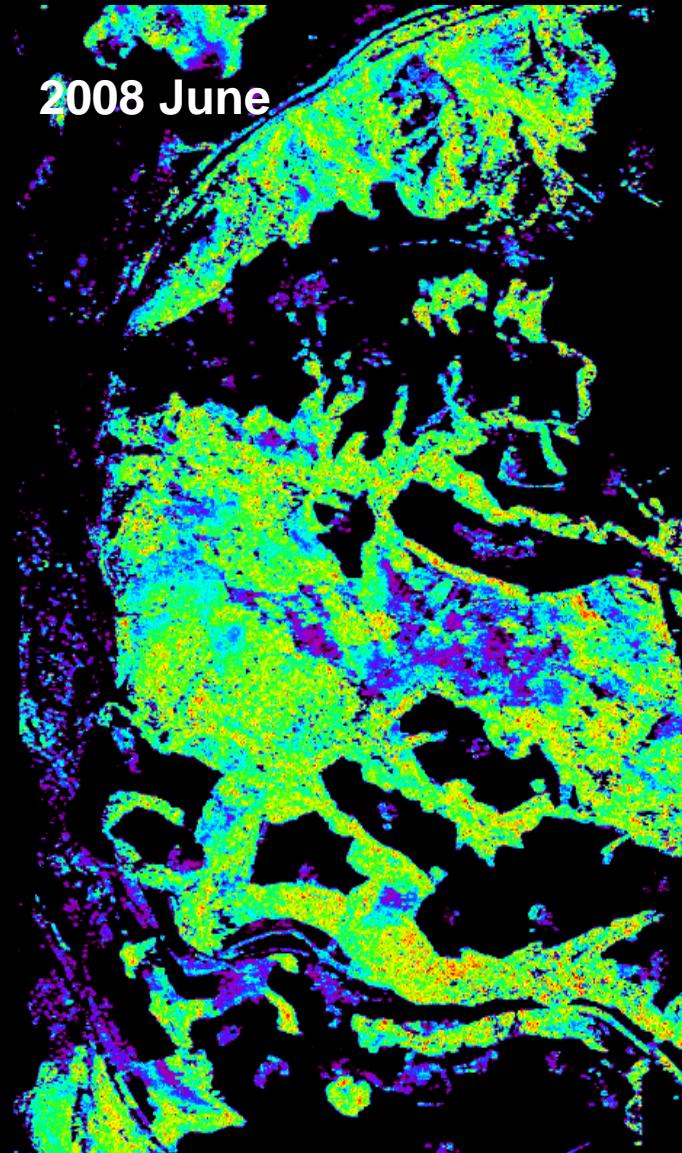
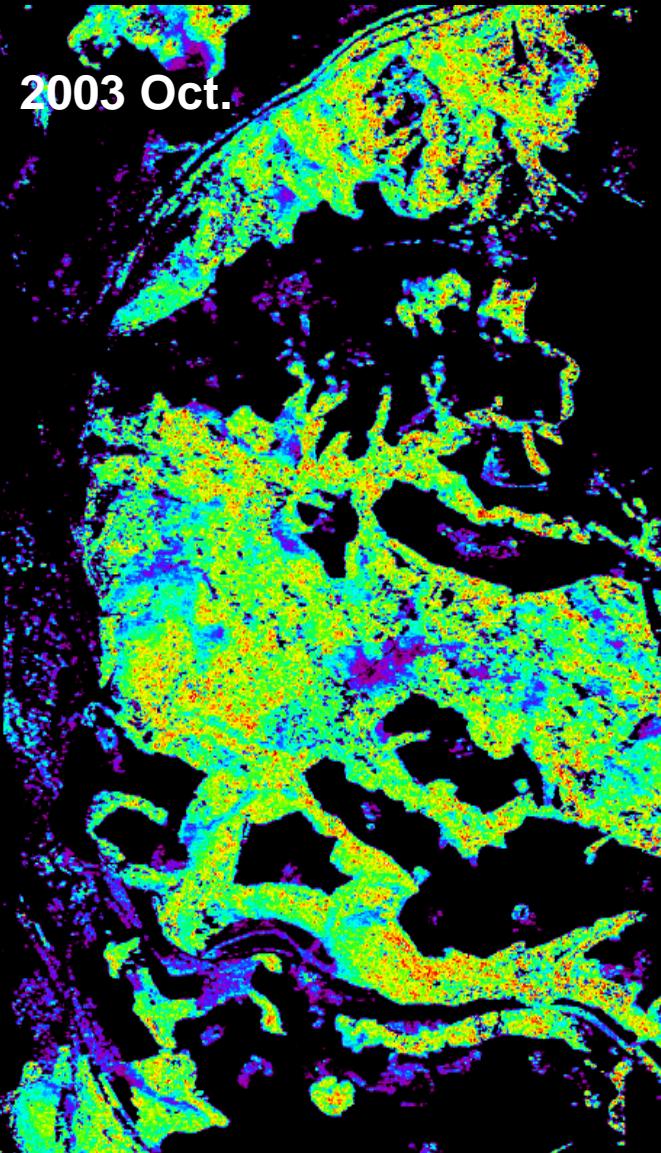
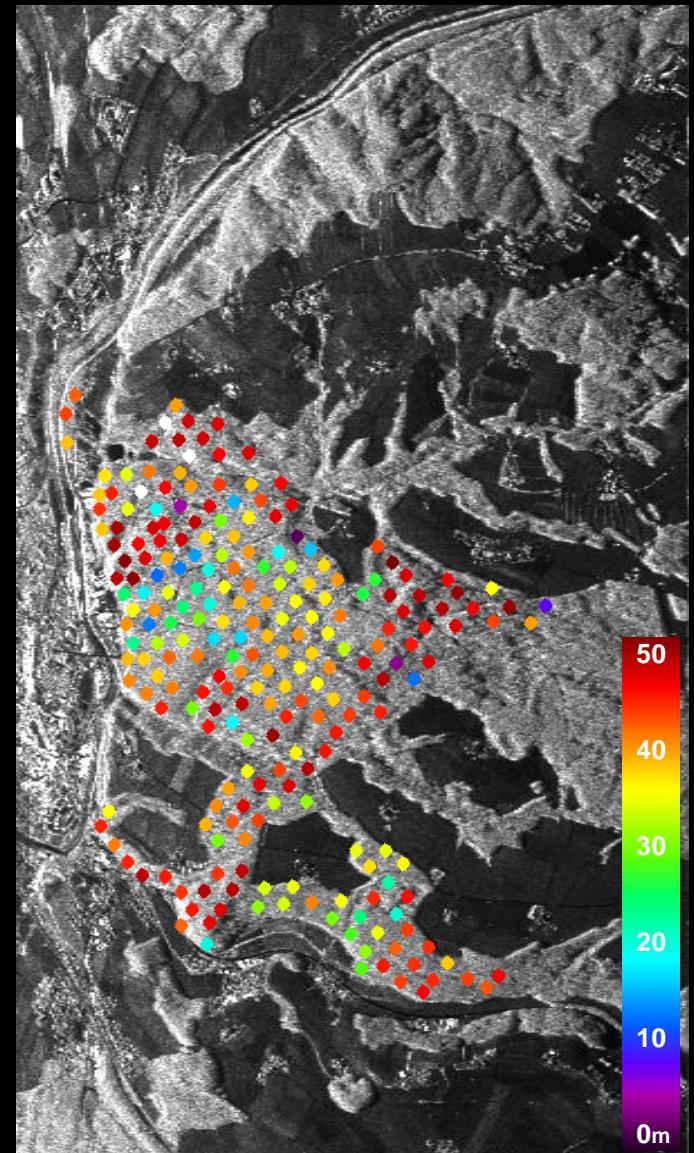
# Traunstein Test Site



Forest type	Temperate
Topography	Moderate slopes
Height	25 ~ 35m
Species	N. Spruce, E. Beech, White Fir
Biomass	40 ~ 450 t/ha



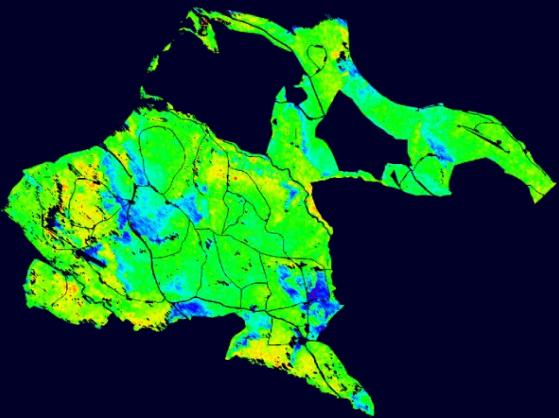
# Traunstein Test Site



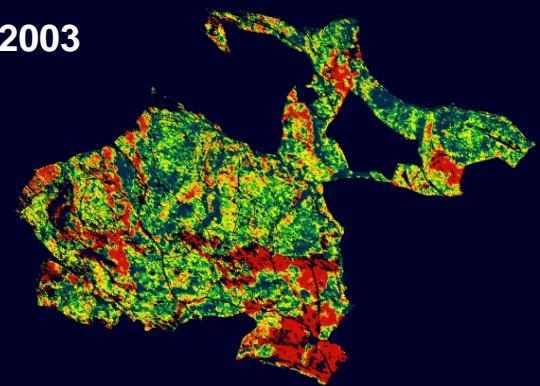
2003



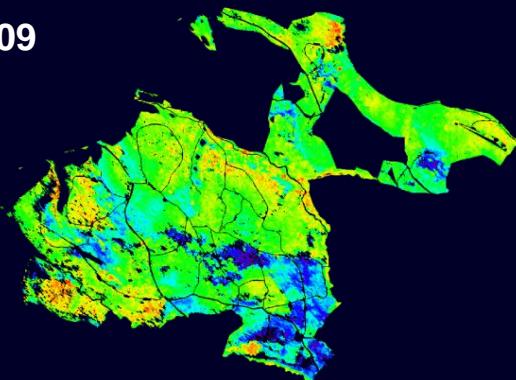
2008



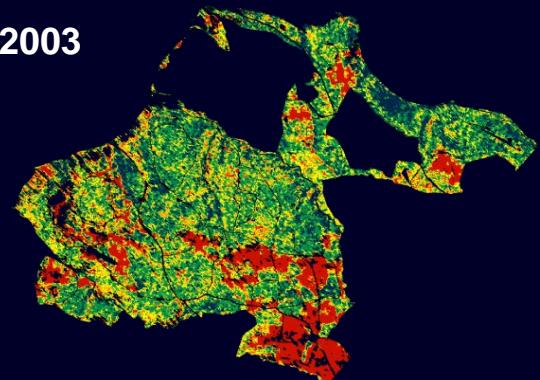
2008-2003



2009

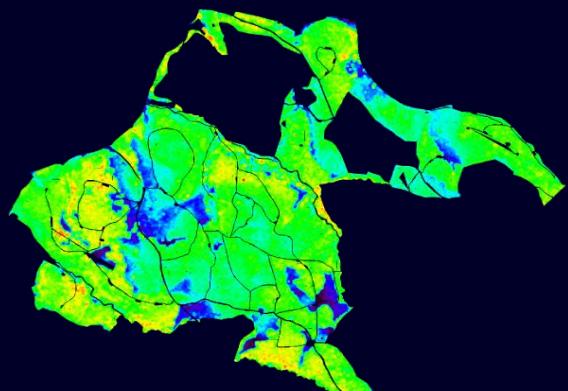


2009-2003

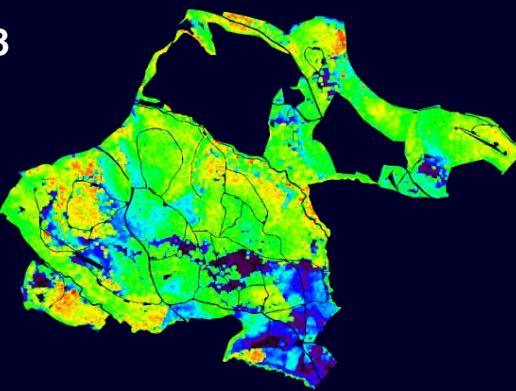


Pol-InSAR Height (H100) Estimates / L-band / Traunstein, Germany     $\Delta H$  Classes: [-10,-5],[-5,-2],[-2,2],[2,5],[5,10]

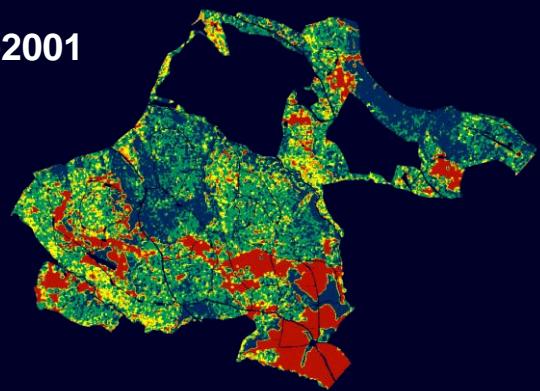
2001



2008

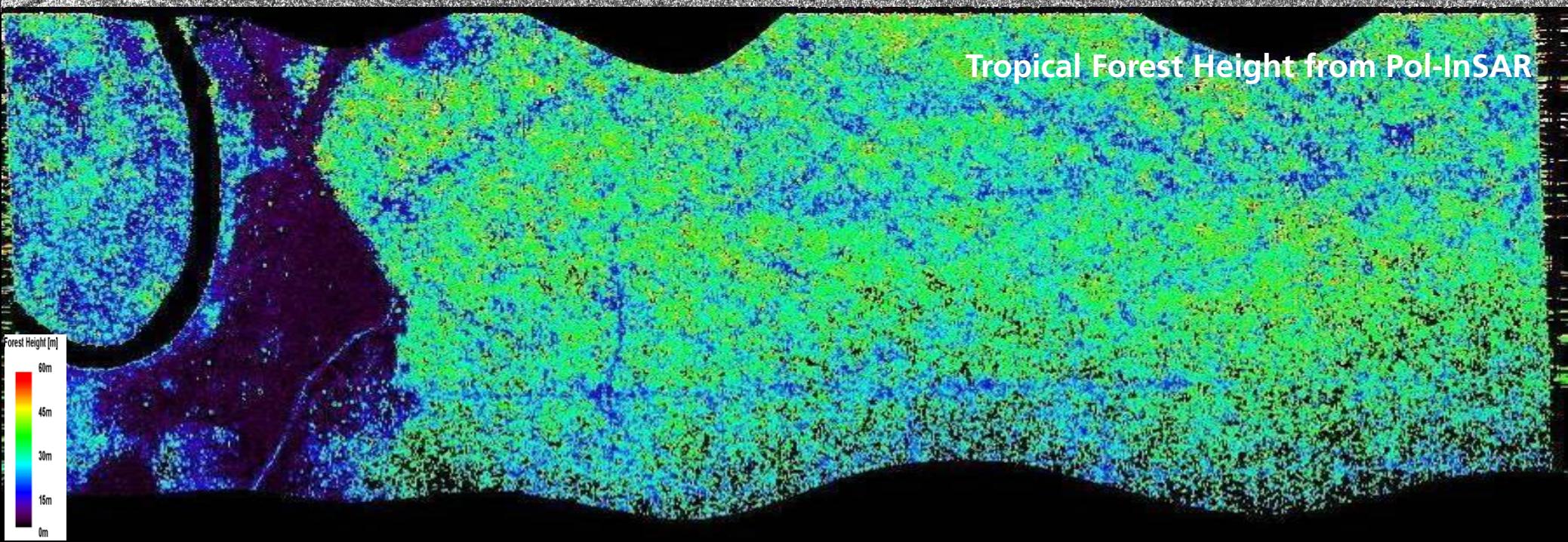
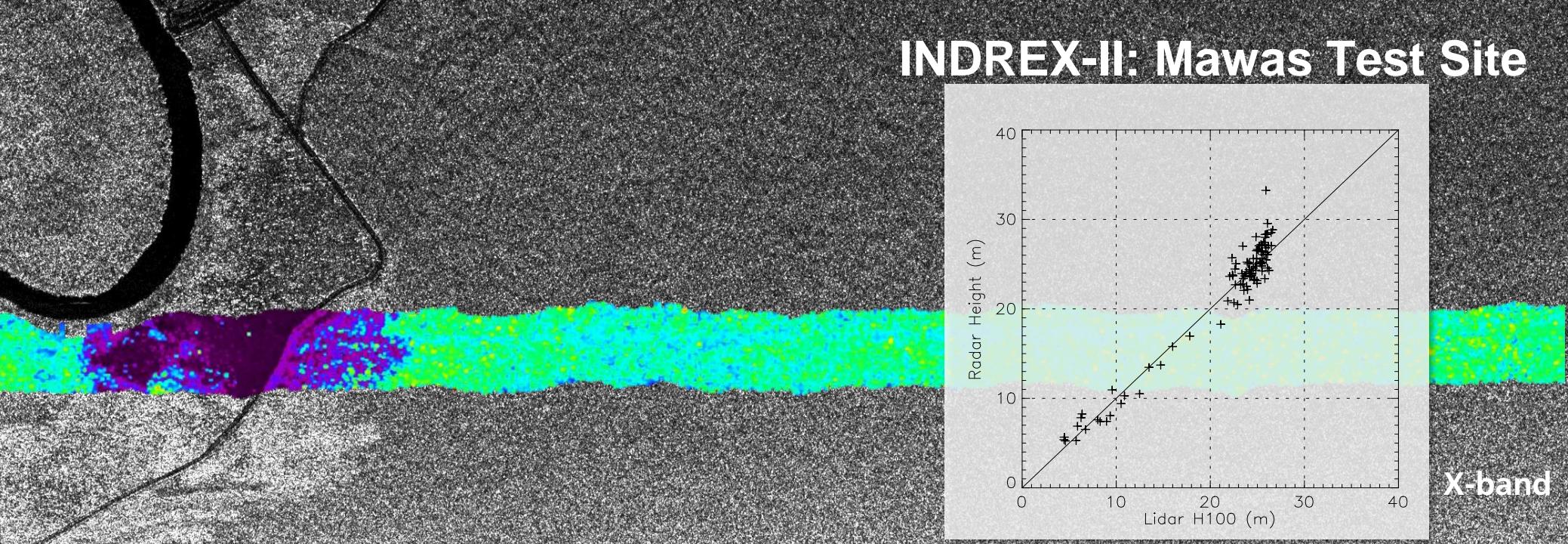


2008-2001



Airborne Lidar Height (H100) Estimates / L-band / Traunstein, Germany

# INDREX-II: Mawas Test Site

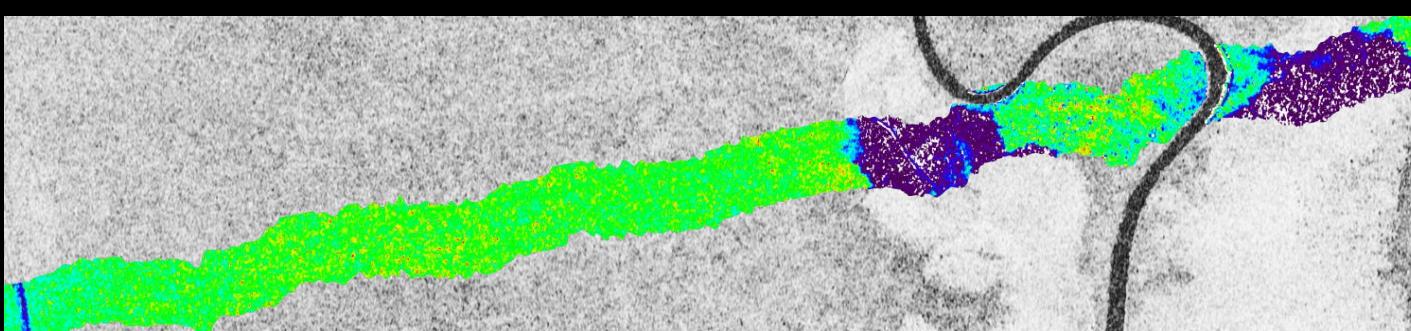
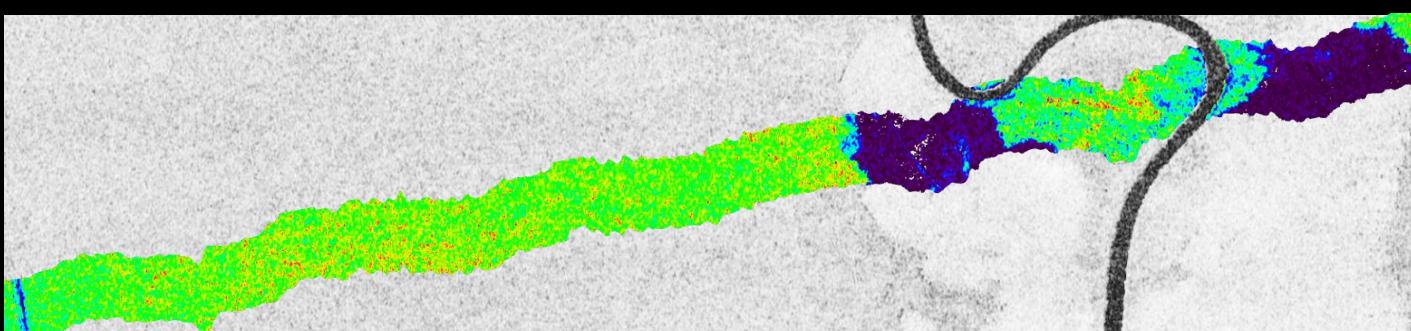
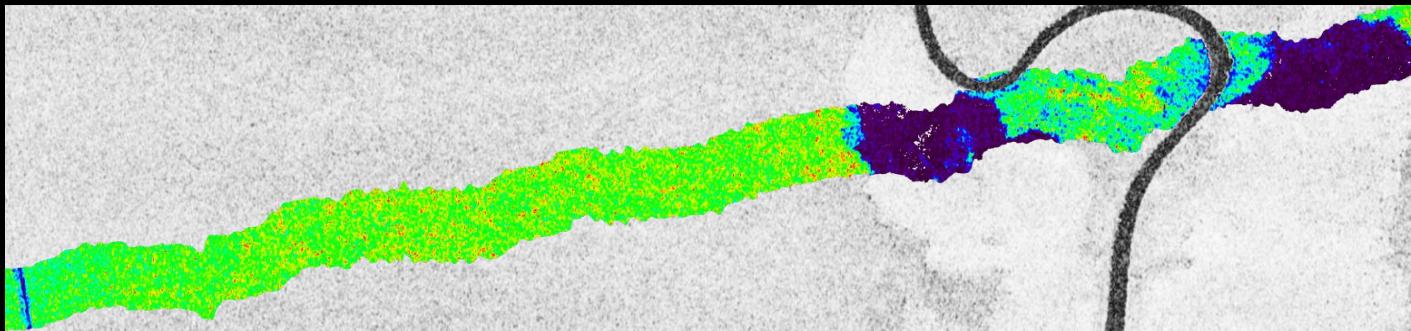
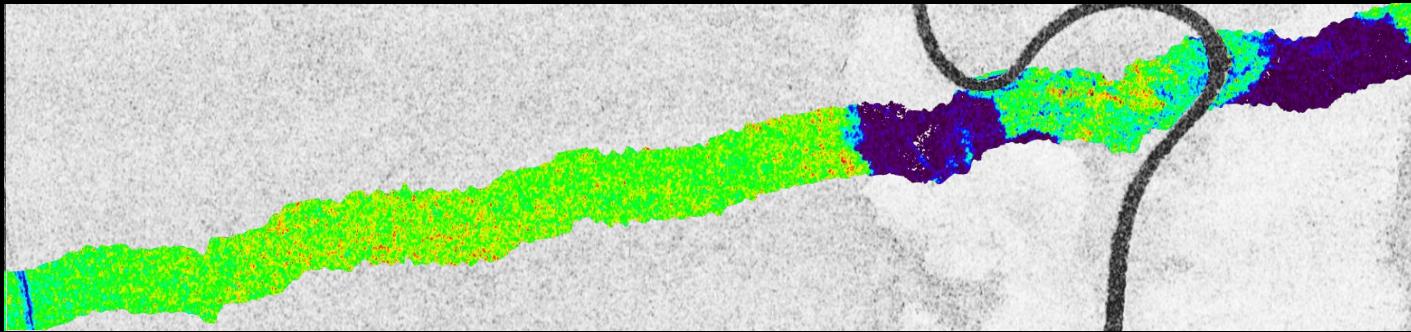
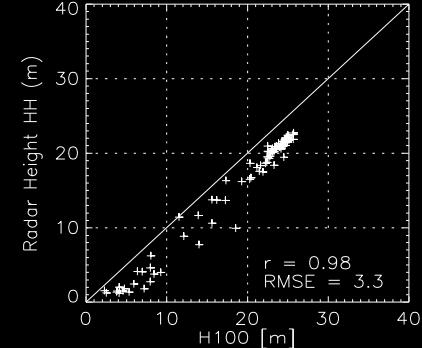
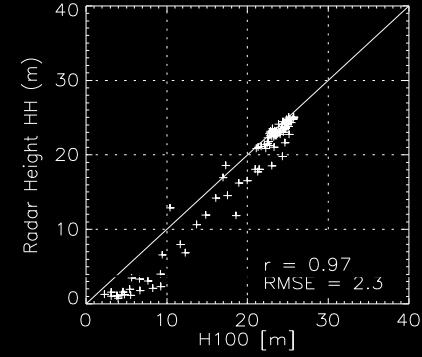
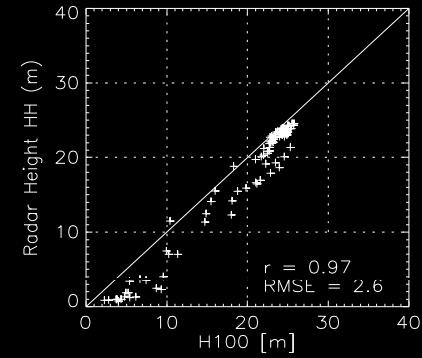
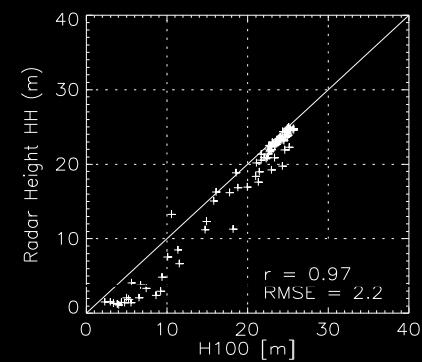


04.01.2011

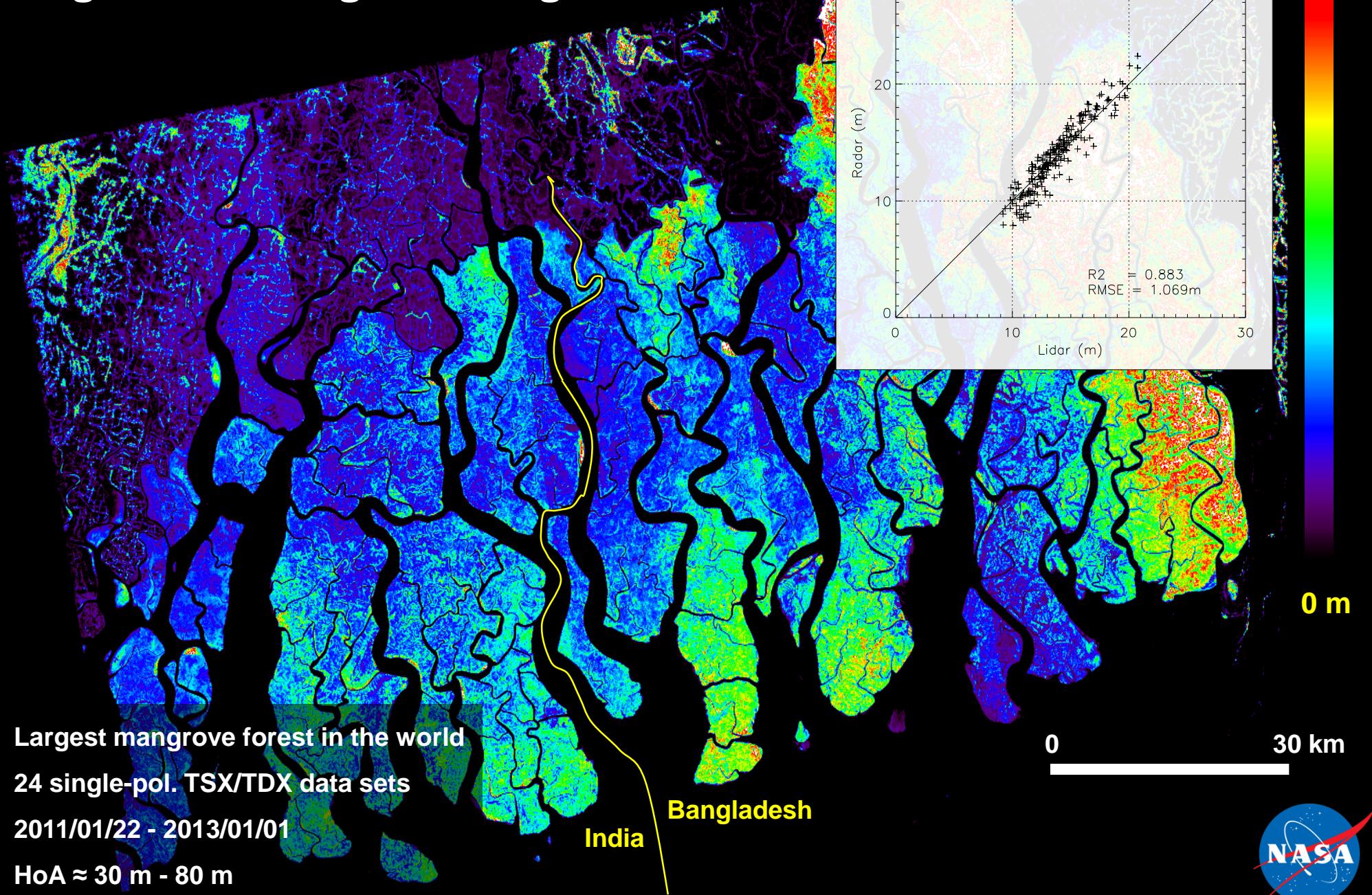
24.12.2011

13.12.2011

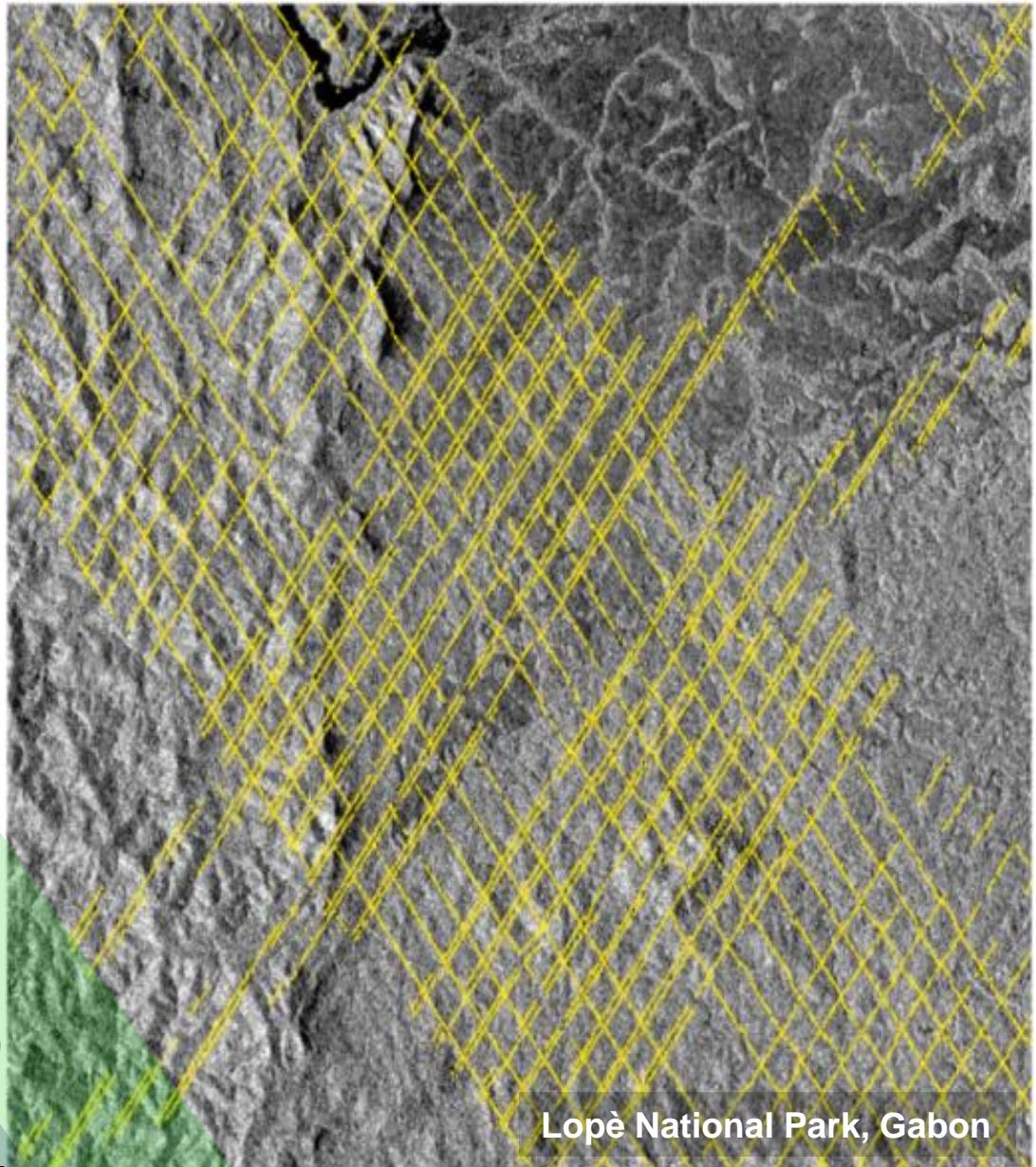
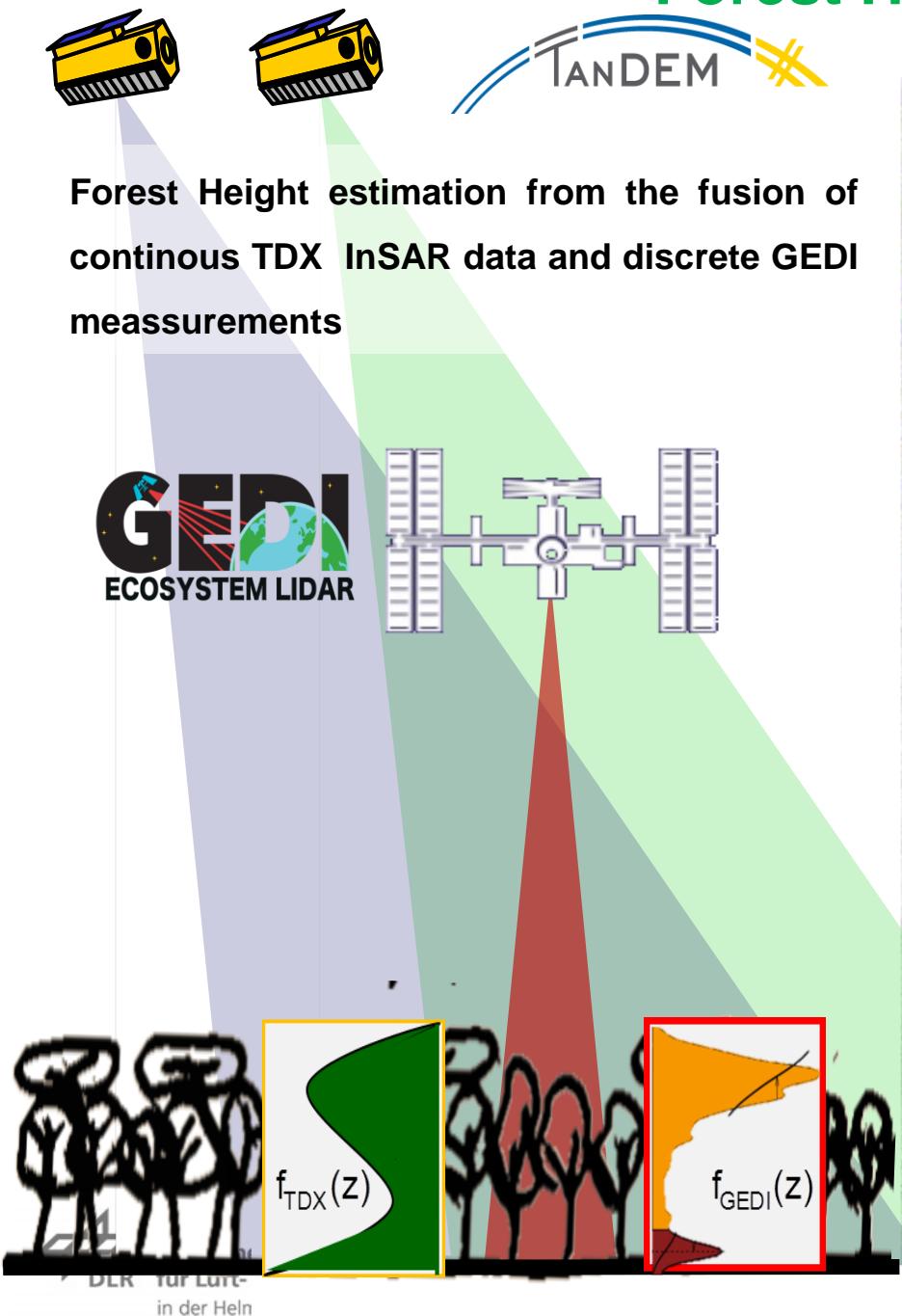
25.08.2012



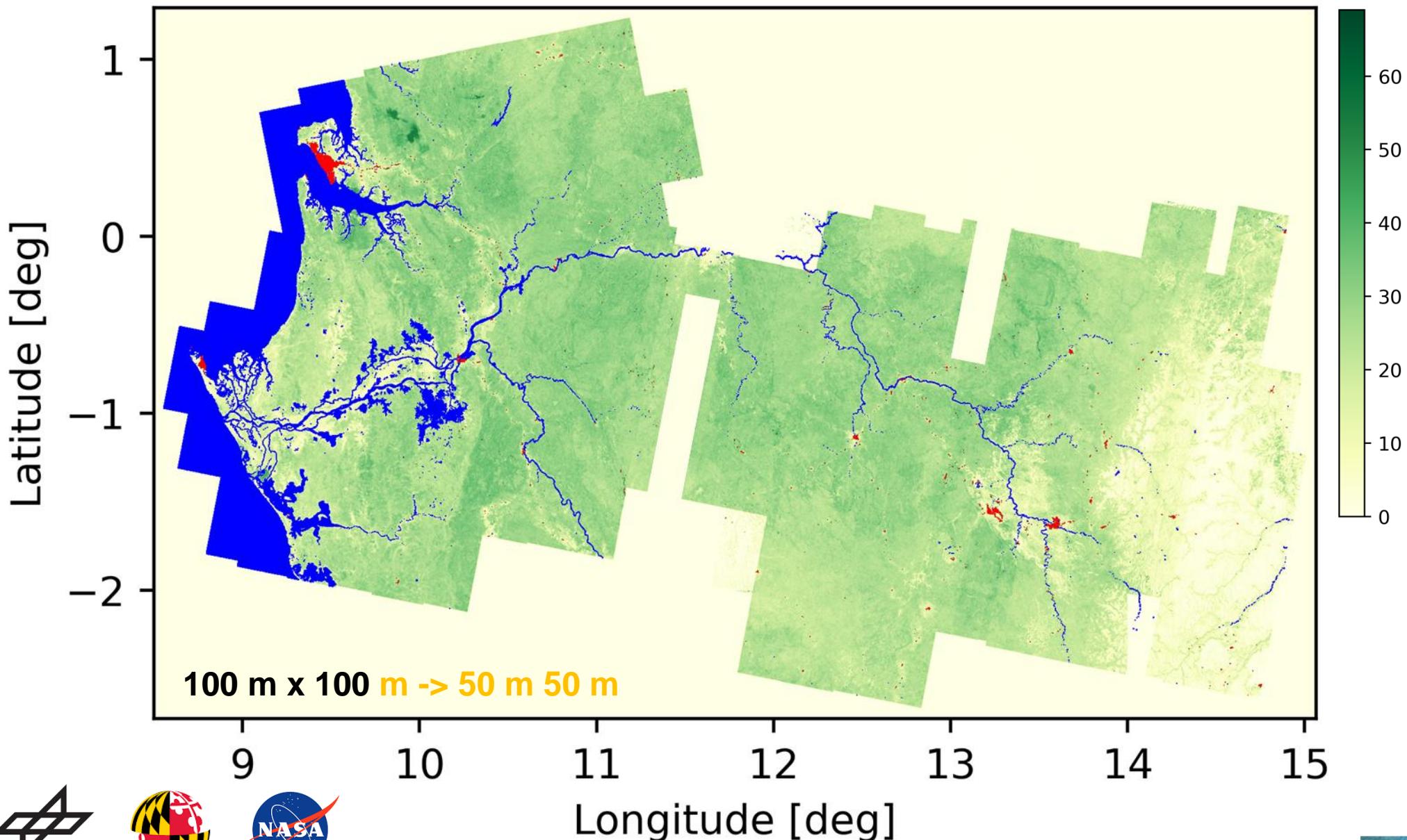
# Bangladesh Mangrove Height

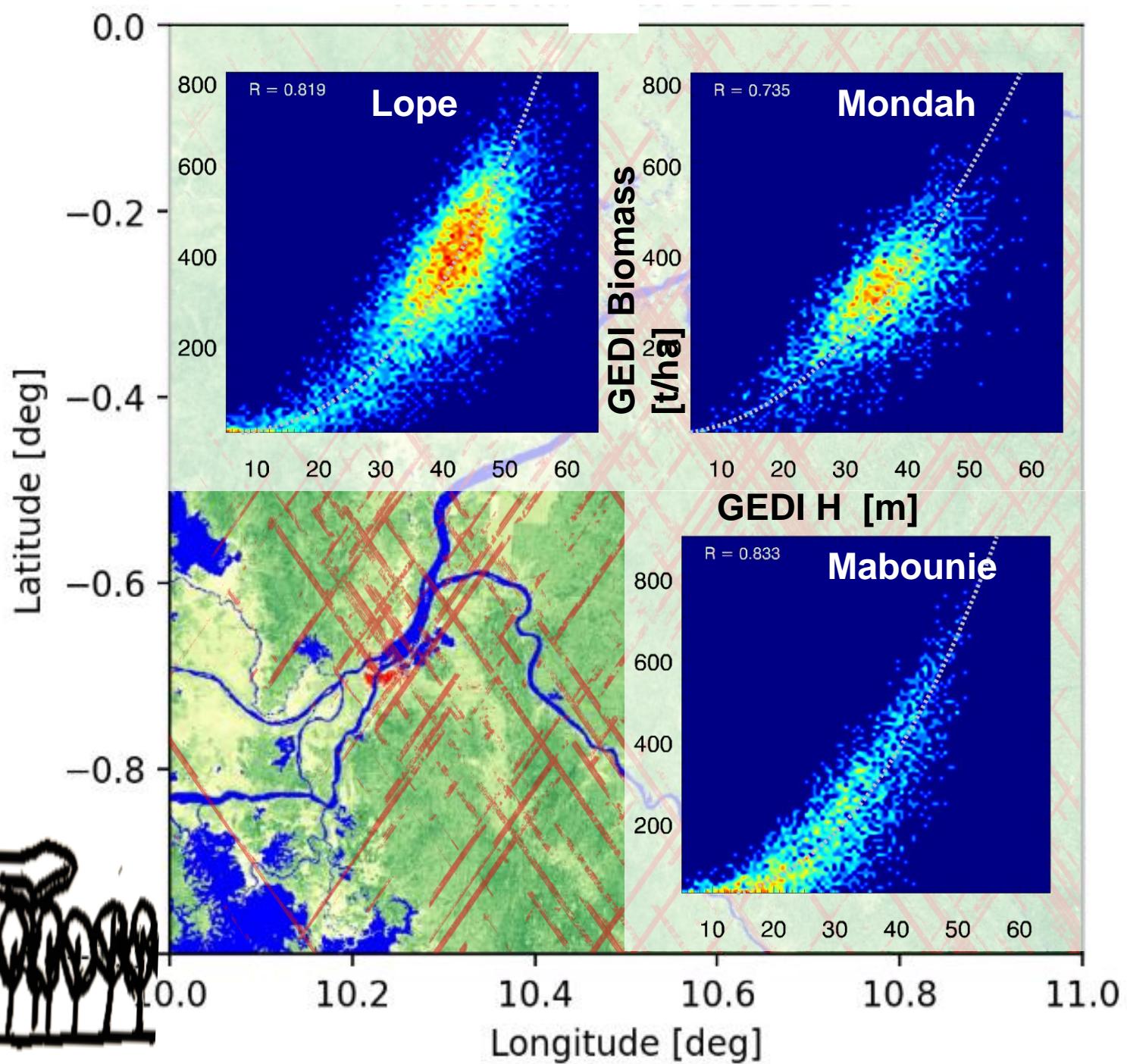
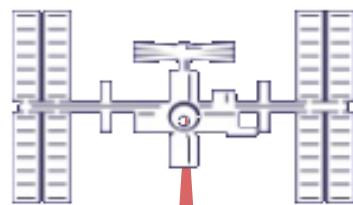


# Forest Height from TD-X / GEDI Data Fusion



# Forest Height Map Gabon: 200 TanDEM-X Scenes + 35K GEDI Footprints

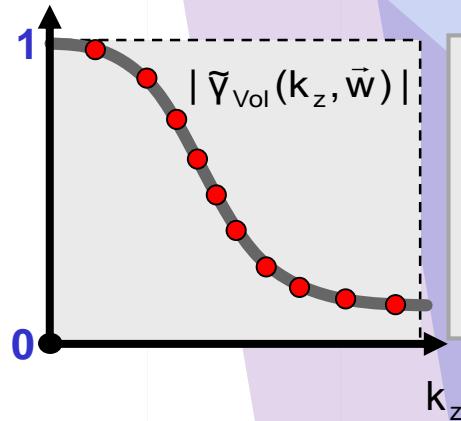




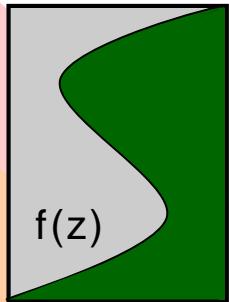
# SAR Tomography



$f(z)$  ... vertical reflectivity function

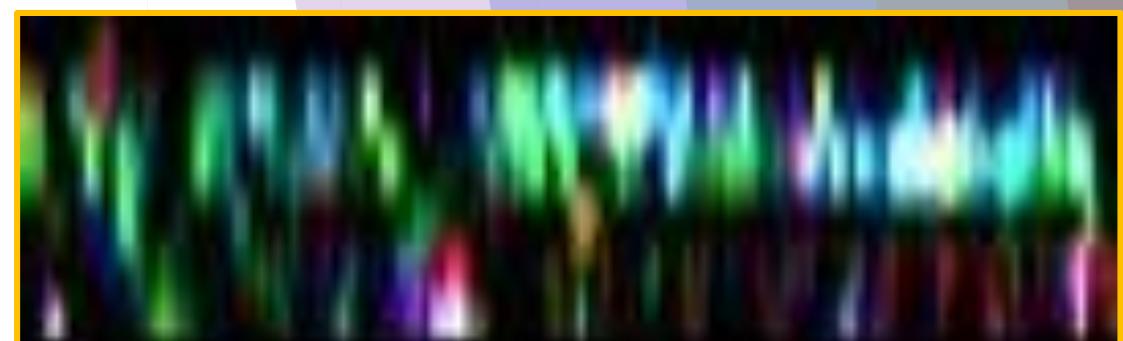


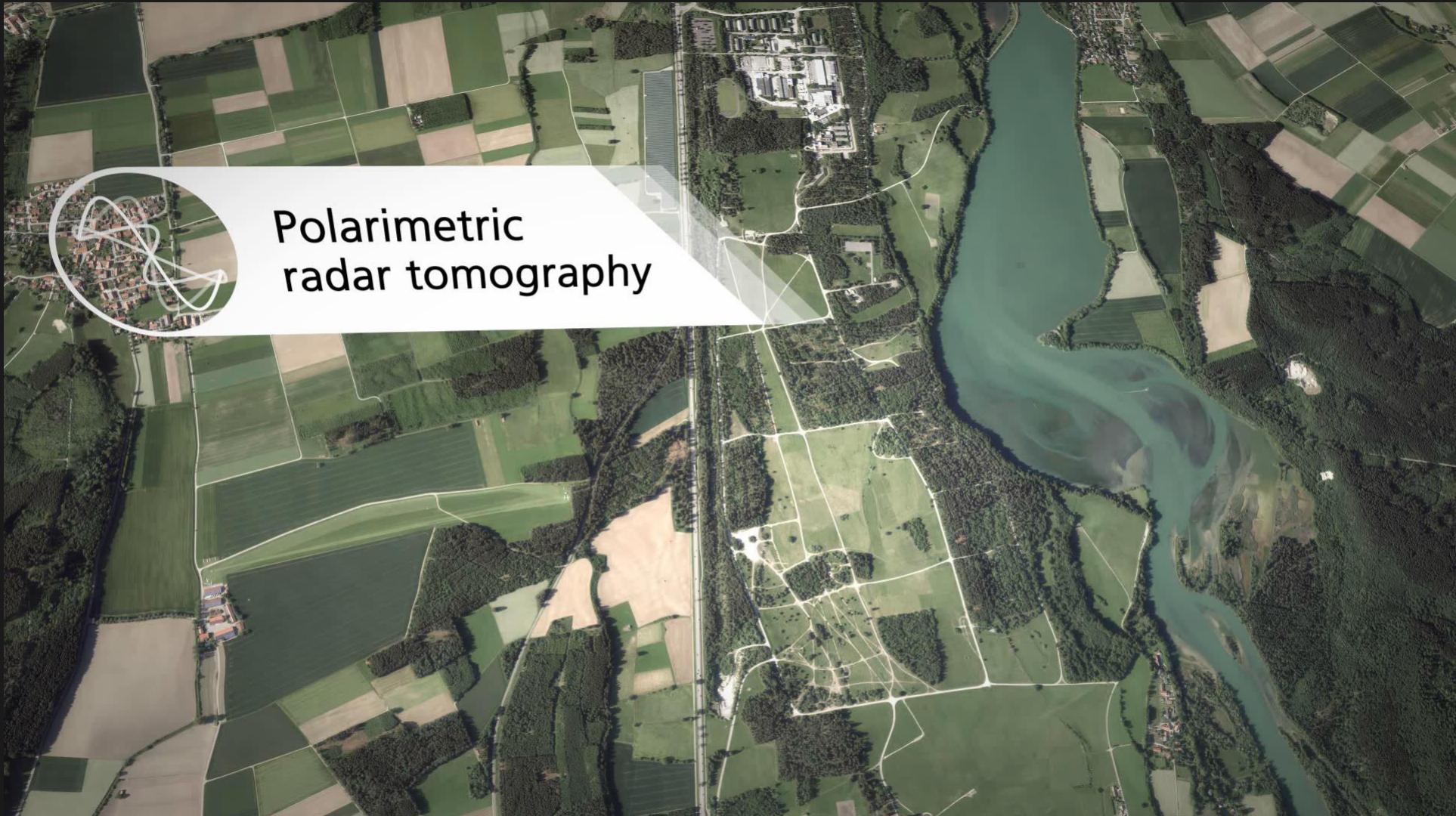
$$\tilde{\gamma}_{\text{vol}}(f(z)) = e^{ik_z z_o} \frac{\int_{z_o}^{h_v} f(z) e^{ik_z z} dz}{\int_{z_o}^{h_v} f(z) dz}$$



$f(z)$  ... vertical reflectivity function

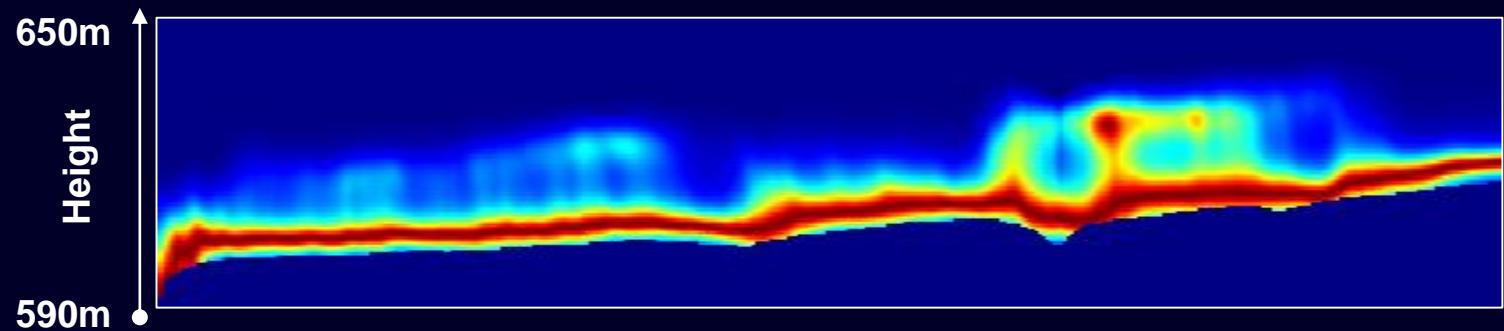
Vertical Wavenumber:  $\kappa_z = \frac{\kappa \Delta \theta}{\sin(\theta_0)}$



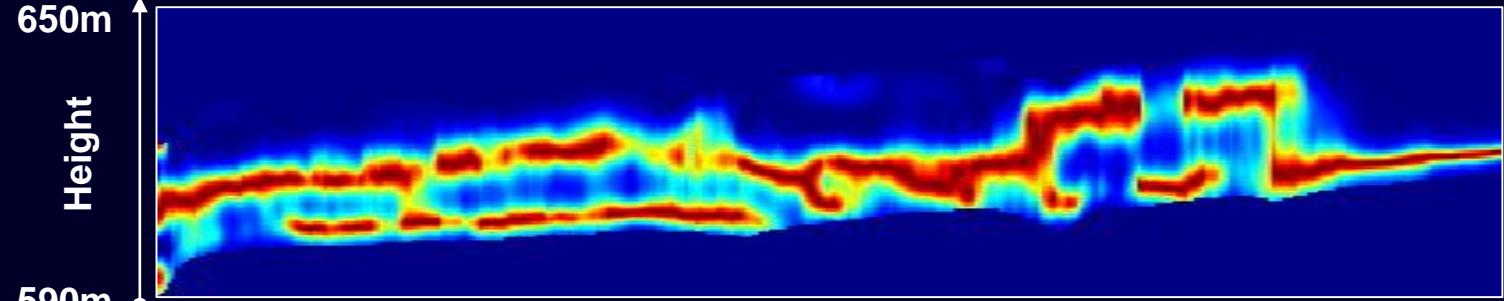


Polarimetric  
radar tomography

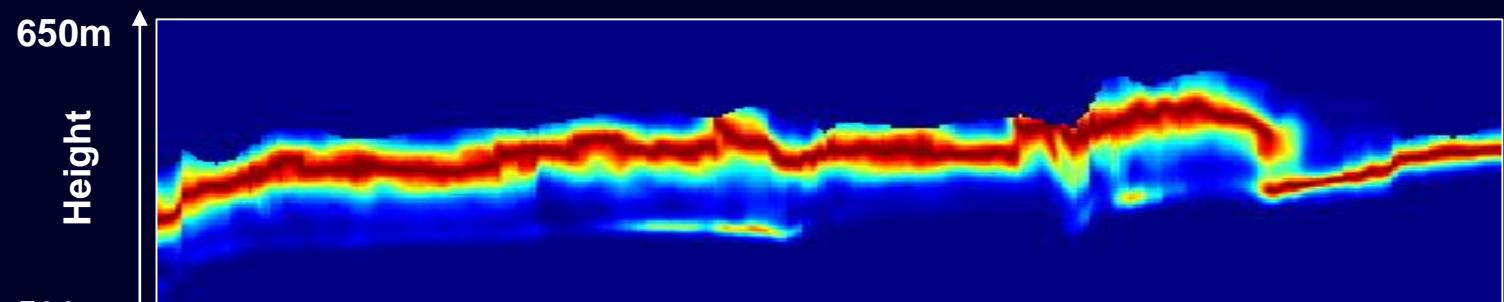
**P-band**



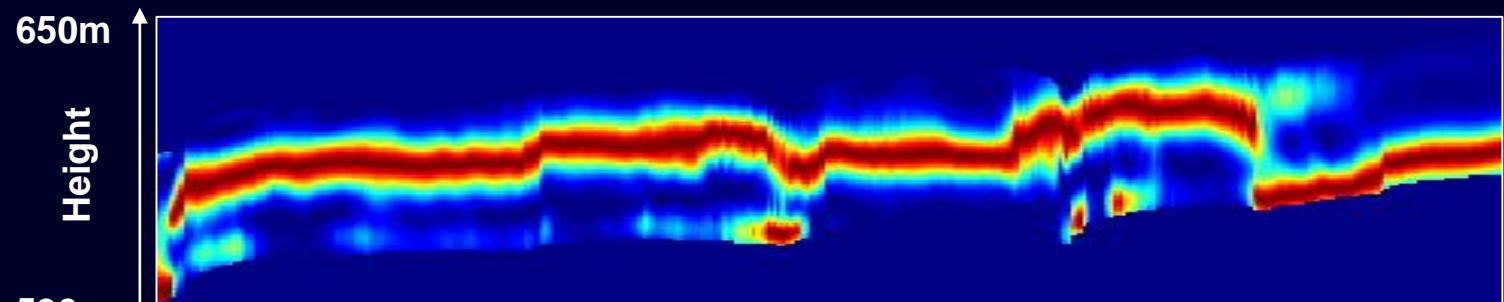
**L-band**



**S-band**

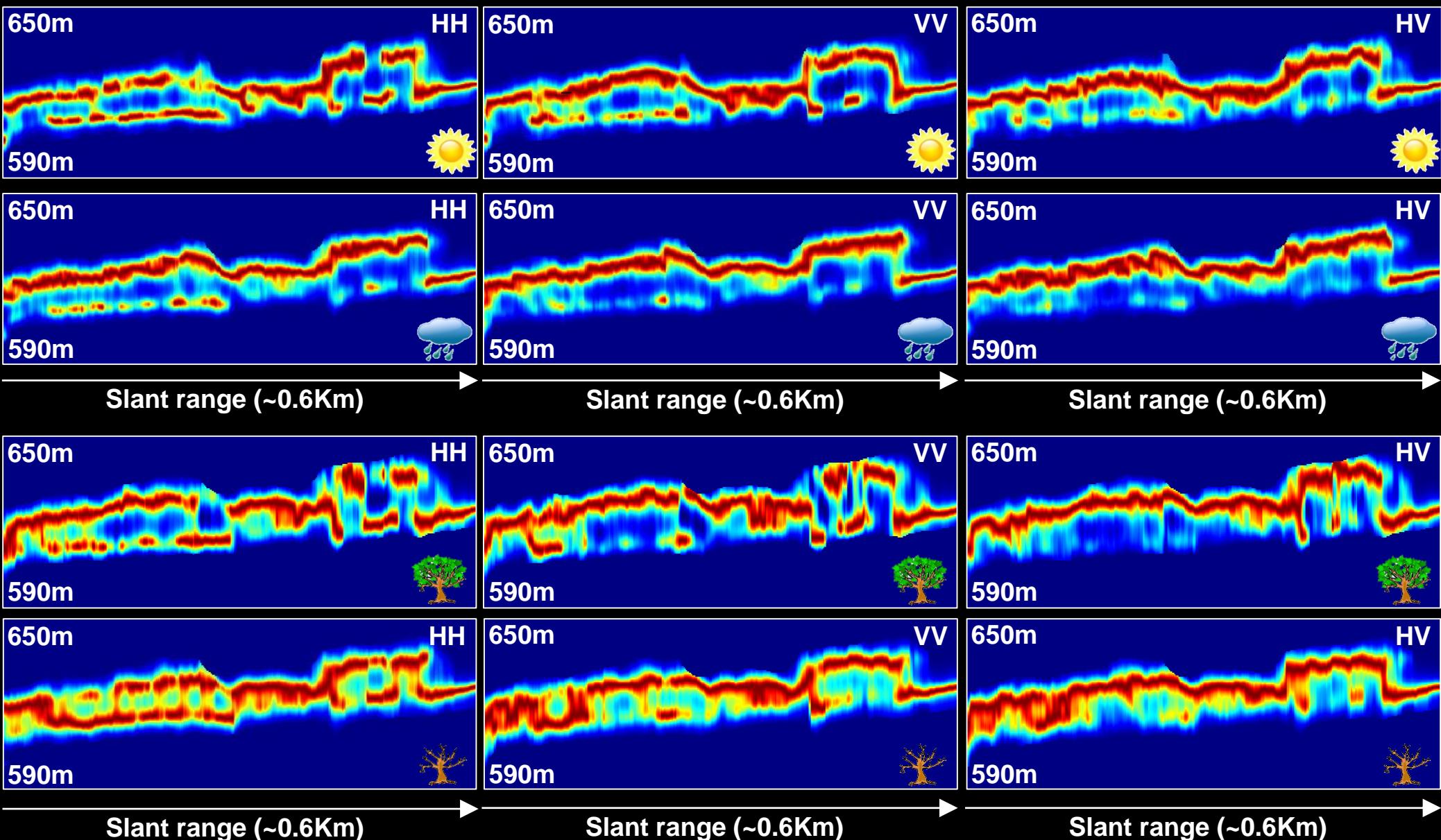


**X-band**



Slant range (0.6Km)

# Temporal variations at L-band (Capon)

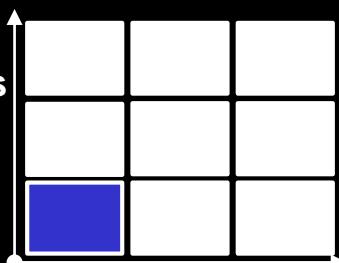
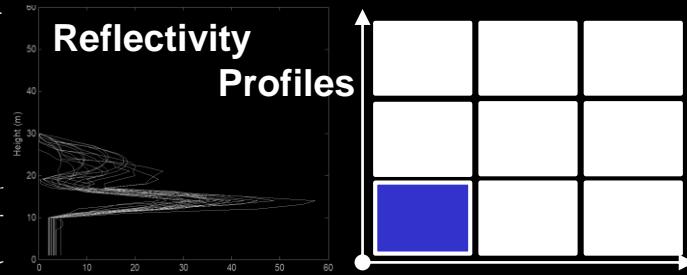
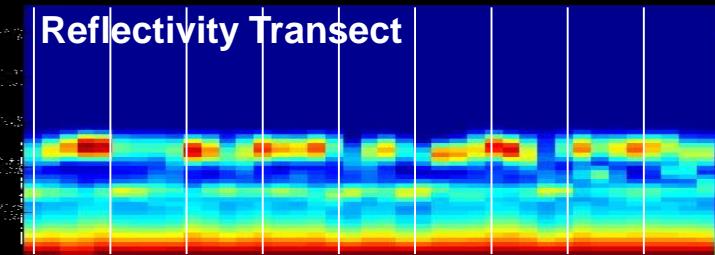
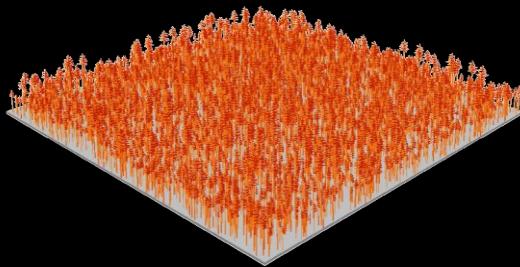


# Forest Structure Characterisation

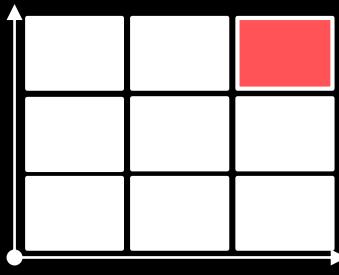
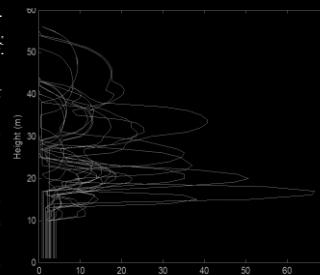
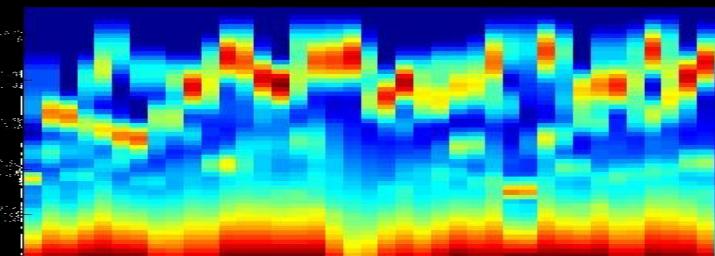
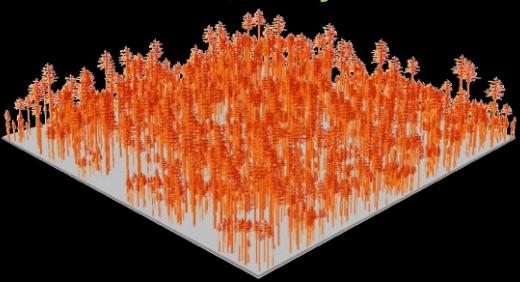


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Remote Sensing and Earth System Dynamics

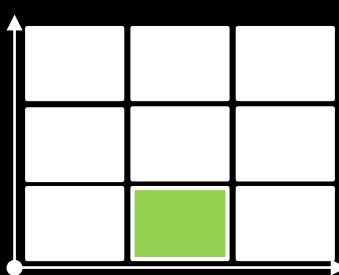
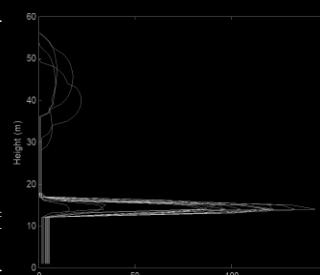
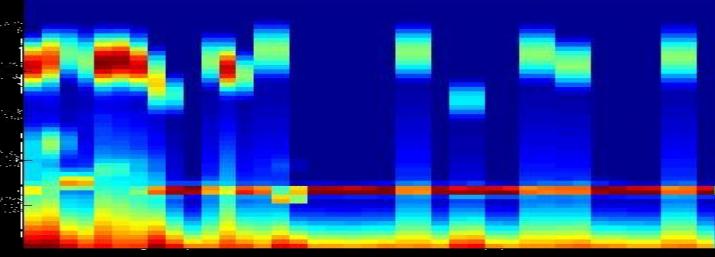
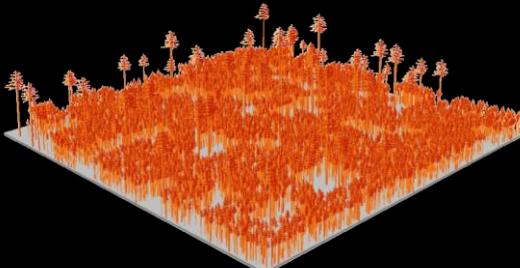
## ► Young forest, 50 years old



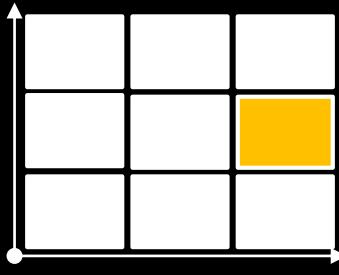
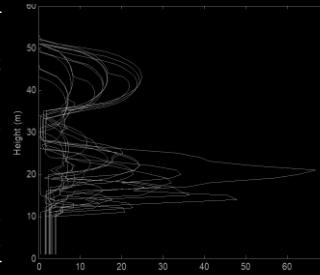
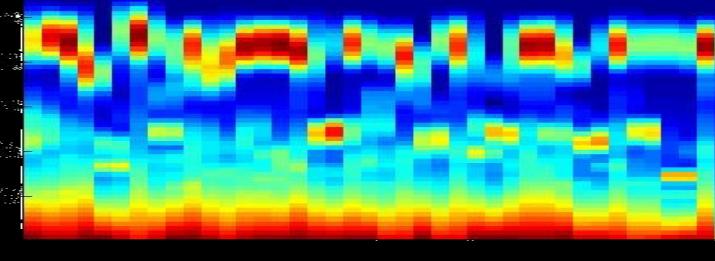
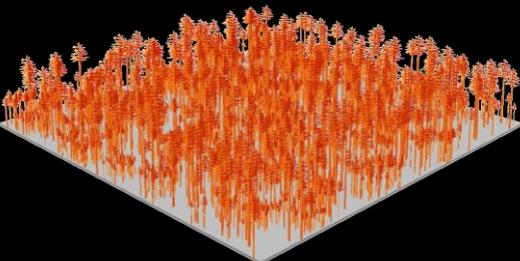
## ► Old forest, 500 years old

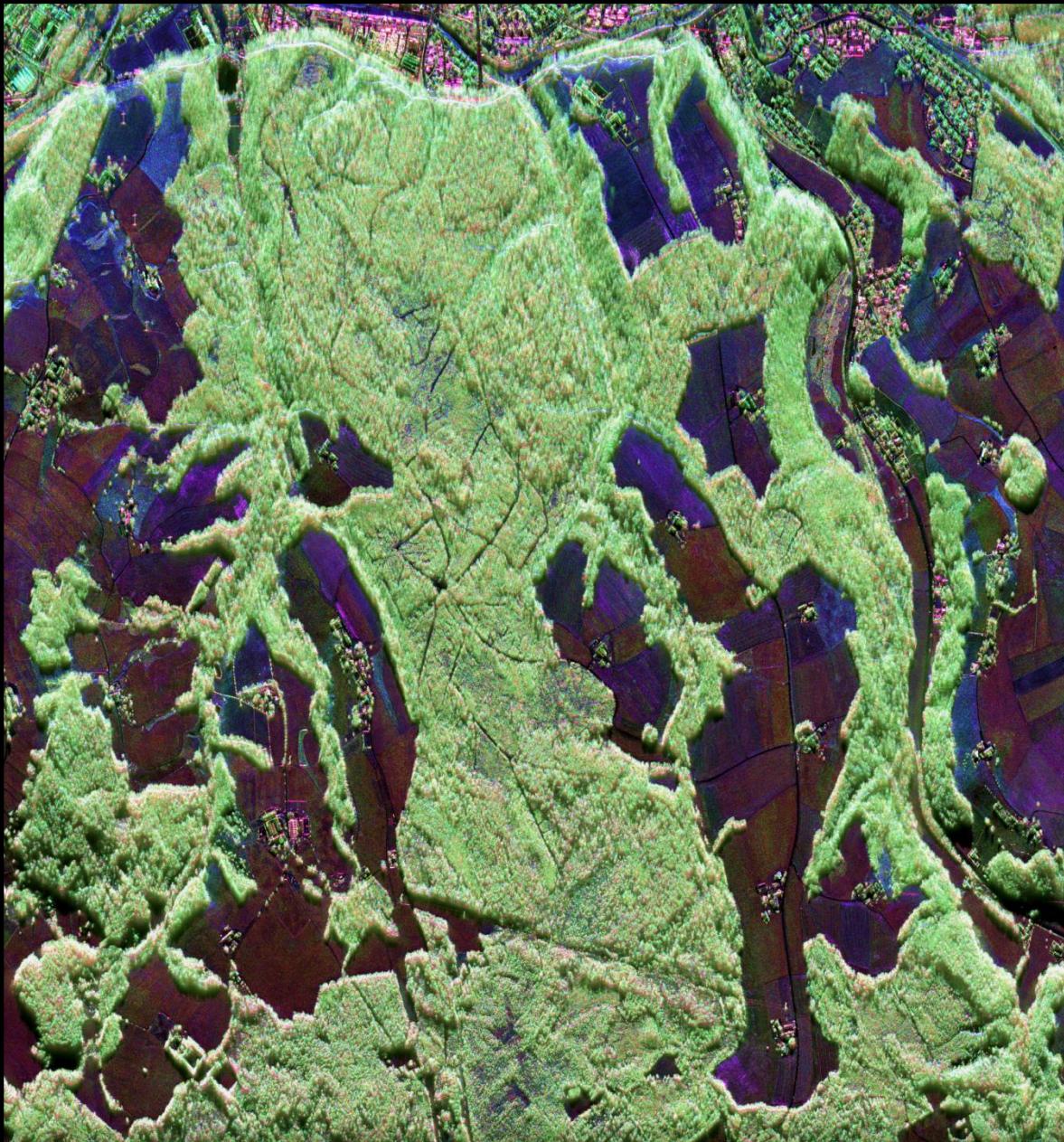


## ► Old forest, 10 years after a fire event



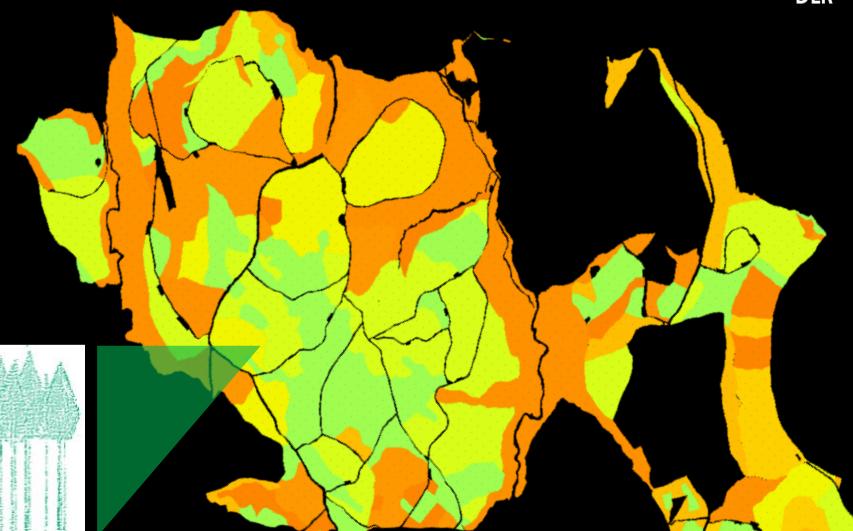
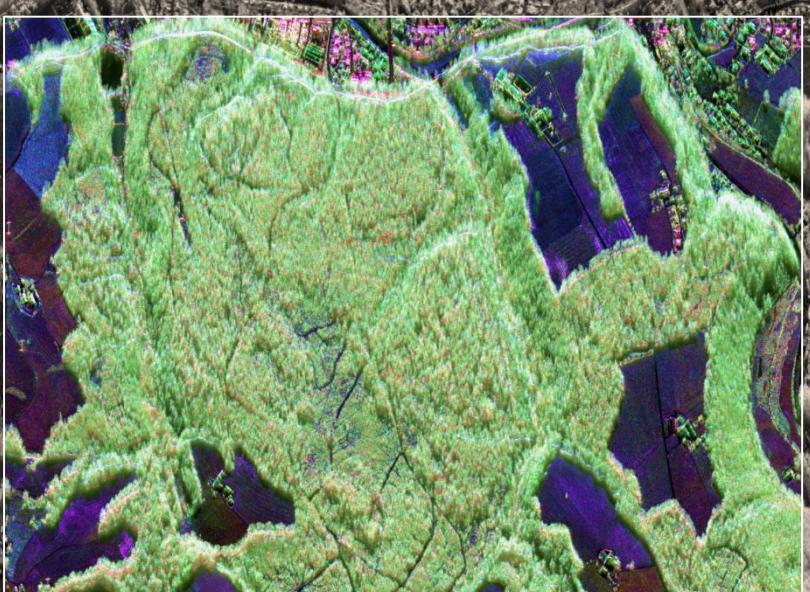
## ► Old forest, 200 years after a fire event





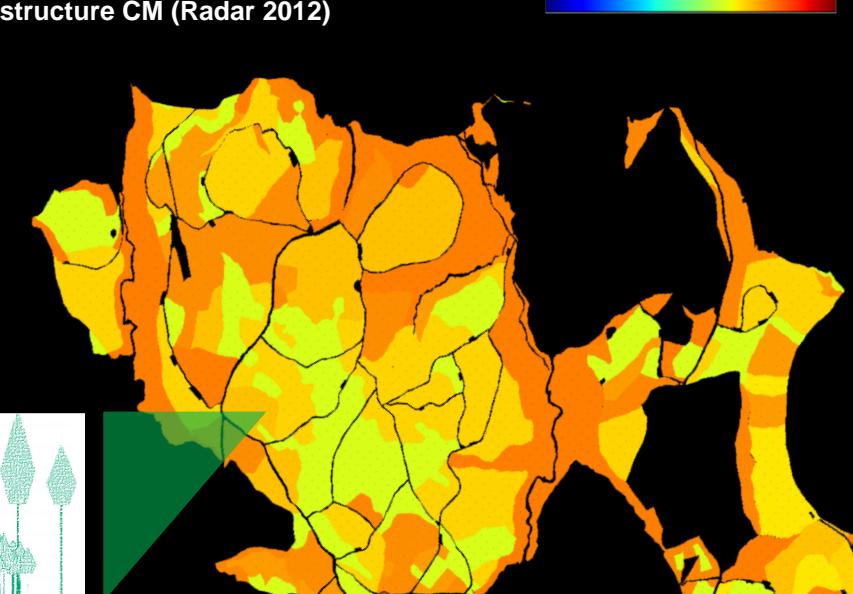
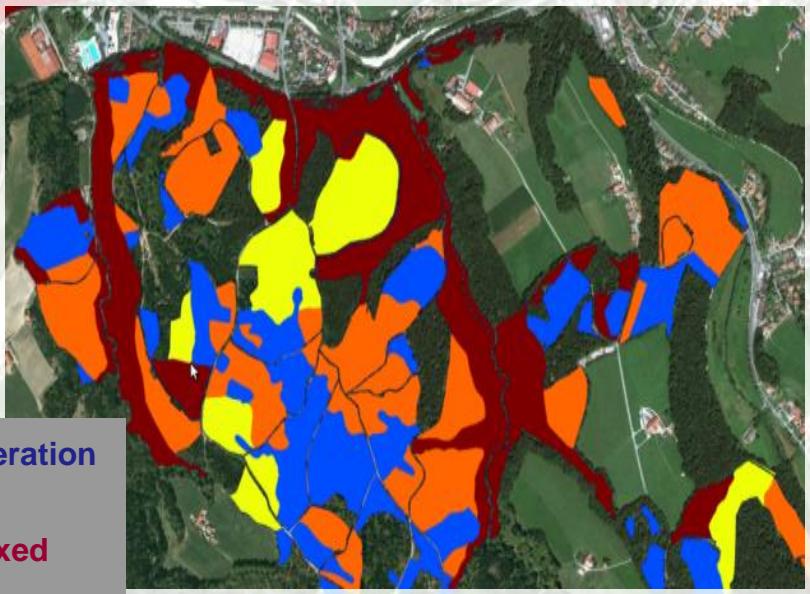
**Forest Structure Classification (25x25 m): Traunstein, Germany, 2008 / 2012**

Vertical structure CM (Radar 2008)



0 1

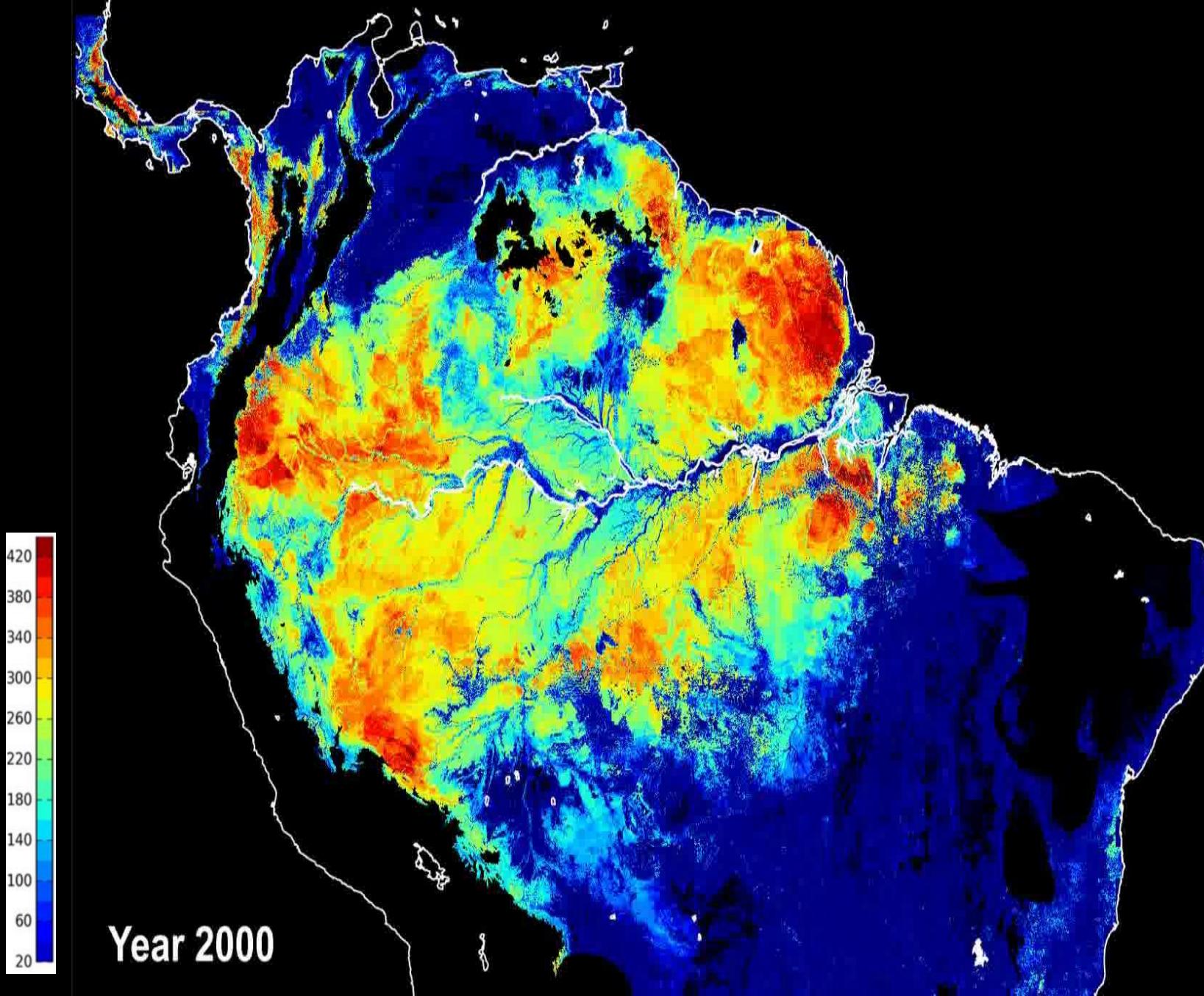
Vertical structure CM (Radar 2012)

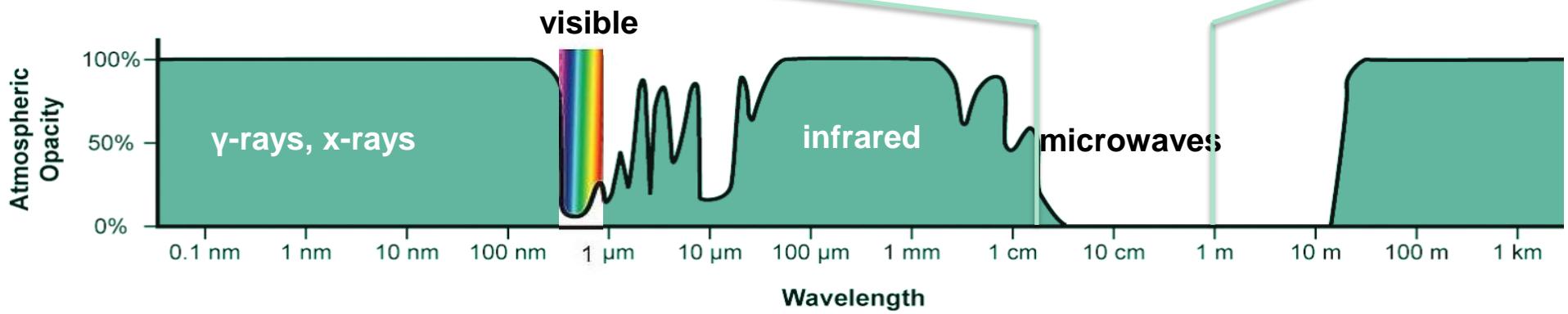
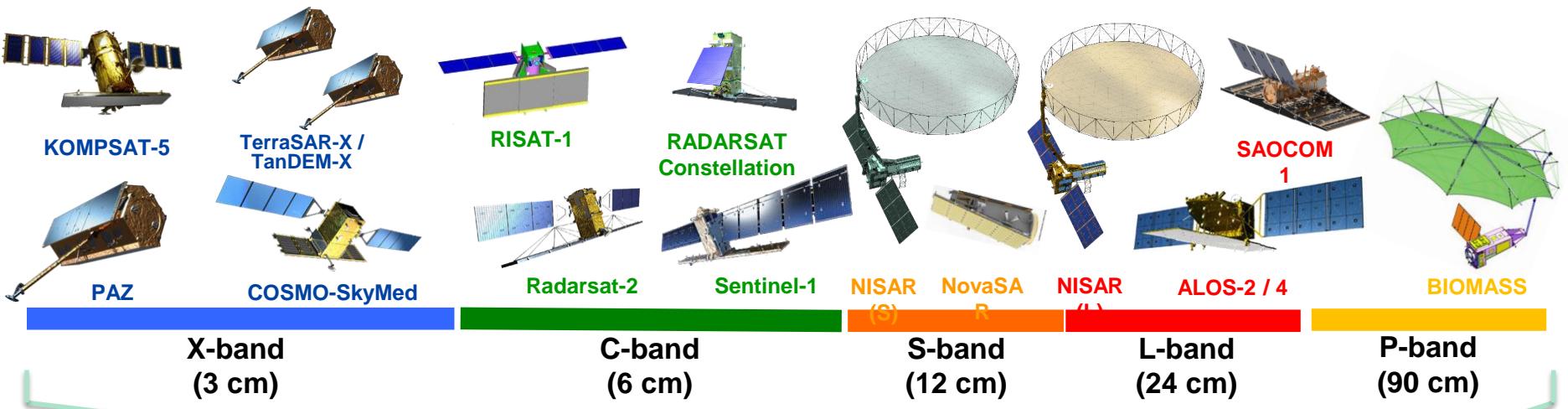


Regeneration  
Mature  
Old-mixed  
Young

Forest Structure Classification (25x25 m): Traunstein, Germany, 2008 / 2012

# Prediction of biomass dynamics



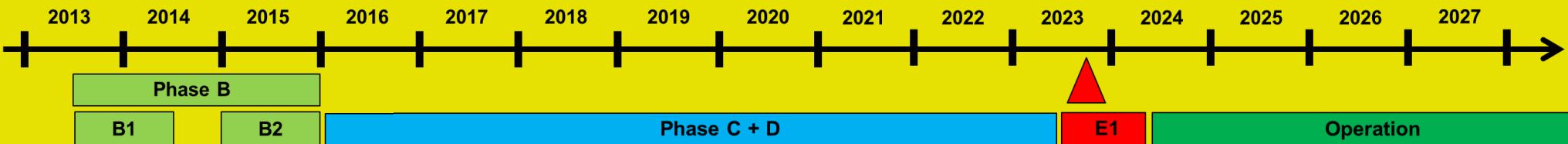
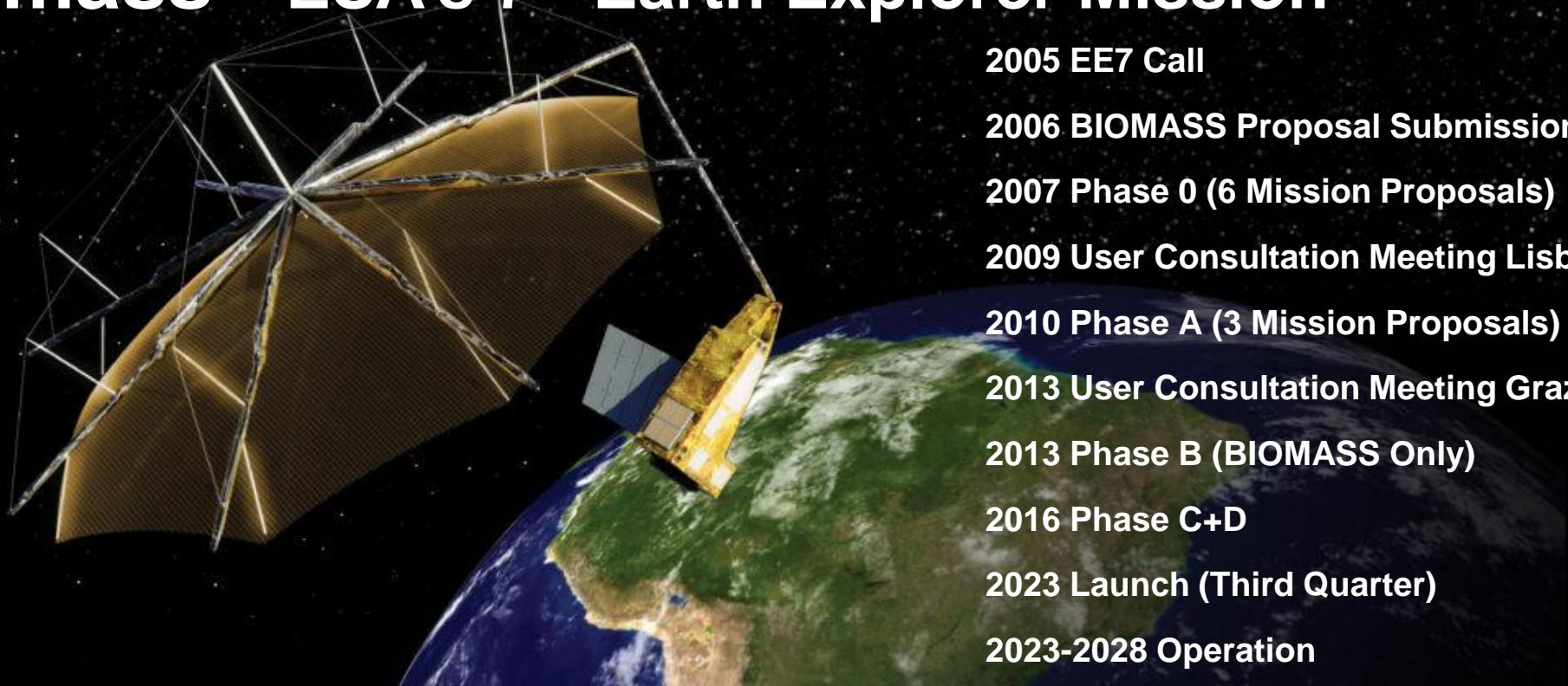


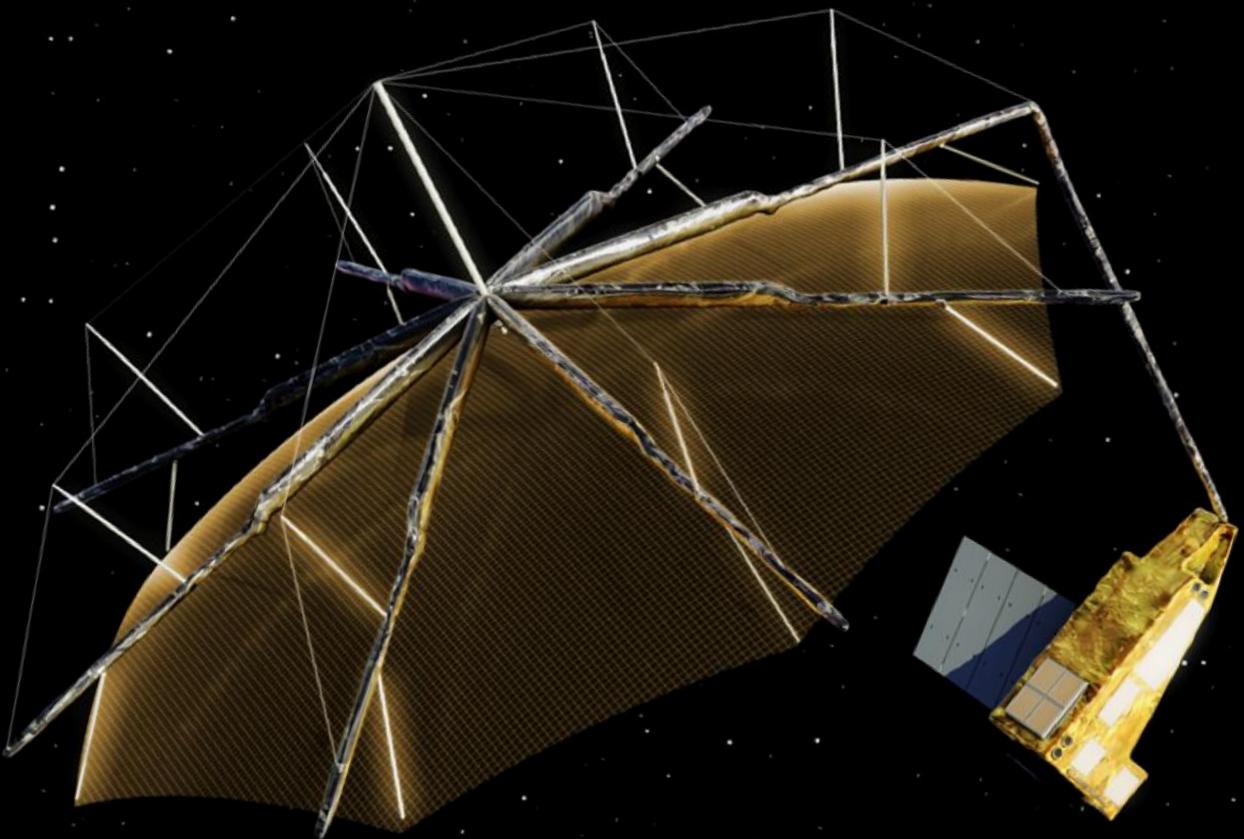
We do not know how to combine multifrequency measurements in a model framework !

We do not know how to combine measurements at different spatial (temporal) scales !



# biomass - ESA's 7th Earth Explorer Mission





- ✓ Single satellite, operated in a polar sun-synchronous orbit
- ✓ **Full polarimetric P-band (435 MHz,  $\lambda=69\text{cm}$ ) SAR (Synthetic Aperture Radar) with 6 MHz bandwidth**
- ✓ Two mission phases: **Tomography** (year 1), **Interferometry** (year 2-5)
- ✓ Multi-repeat pass interferometry (3 passes in nominal operations) with a 3 days repeat cycle
- ✓ Global coverage in 7.5 months (228 days) on both asc. and des. passes
- ✓ 5 years lifetime

# BIOMASS Mission Products

Level 2 Product	Definition	Information Requirements
Forest biomass	Above-ground biomass expressed in $t\ ha^{-1}$ .	<ul style="list-style-type: none"><li>• 200 m resolution</li><li>• RMSE of 20% or <math>10\ t\ ha^{-1}</math> for biomass <math>&lt; 50\ t\ ha^{-1}</math></li></ul>
Forest height	Upper canopy height defined according to the H100 standard	<ul style="list-style-type: none"><li>• 200 m resolution</li><li>• RMSE better than 30% for trees higher than 10 m</li></ul>
Severe disturbance	Map product showing areas of forest clearance	<ul style="list-style-type: none"><li>• 50 m resolution</li><li>• detection at a specified level of significance</li></ul>

- **1 near-global map of biomass and height from tomography in the first 14 mission months;**
- **updated biomass and height maps from polarimetry and interferometry every 7.5 months for the rest of the 5-year mission;**
- **annual maps of deforestation.**



# BIOMASS Mission Algorithm & Analysis Platform (MAAP)

Virtual research environment:



- ✓ Ease of data access and sharing
  - Remote sensing data from ESA science missions (and complementary/similar missions)
  - Ground data from ESA campaigns (field data and Cal/Val)
- ✓ Allow data processing (product generation)
- ✓ Allow joint code / algorithm development (**Product Algorithm Laboratory**), addressing intellectual property rights issues
- ✓ Enable interoperability of data/code/algorithms
- ✓ Support transparency in research, development and validation
- ✓ Ease information sharing and networking



**ESAMAAP**

# Multi-baseline Polarimetric SAR Interferometry: Forest Applications.

